



Method of Constructing p-rep Designs

Vinay Kumar¹, Cini Varghese¹, Seema Jaggi², Eldho Varghese³, Mohd Harun¹, Sayantani Karmakar¹, Devendra Kumar¹

ABSTRACT

Background: Early generation breeding trials (EGBTs) are very important in plant breeding programmes. In most cases, a large number of breeding lines are to be tested, often with very few available resources and it is also required to repeat these trials in a number of environments. For such trials, an alternative is to use partially replicated designs, where a proportion of the test lines are replicated at each environment. **Methods:** Here, a general method of constructing a series of efficient partially replicated designs for EGBTs in equal block sizes, through initial blocks is developed. **Result:** Taking all environments together, the designs obtained are equi-replicate and are partially balanced. They are cost effective in terms of resources as they require lesser replications. **Key words:** Early generation breeding trials, Multi-environmental trials, Partially balanced, Partially replicated designs.

10.18805/BKAP561

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Introduction

Early generation breeding trials (EGBTs) are very important in plant breeding programmes. In most cases, a large number of breeding lines are to be tested, often with very few available resources and it is also required to repeat these trials in a number of environments. For such trials, an alternative is to use partially replicated designs, where a proportion of the test lines are replicated at each environment. Here, a general method of constructing a series of efficient partially replicated designs for EGBTs in equal block sizes, through initial blocks is developed. Taking all environments together, the designs obtained are equi-replicate and are partially balanced. They are cost effective in terms of resources as they require lesser replications.

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How to cite this article: Vinaykumar, L.N., Varghese, C., Jaggi, S., Varghese, E., Harun, M., Karmakar, S. and Kumar, D. (2023). A Method of Constructing p-rep Designs. *Bhartiya Krishi Anusandhan Patrika*. DOI: 10.18805/BKAP561.

Submitted: 13-07-2022 **Accepted:** 02-06-2023 **Online:** 04-10-2023

ykbZuka dks, d l kfk nkgjkus dsfy, vi ; klr gks l drh gS vksj bl l s {ks= dh deh gks l drh gA dbZ 'kkdkrkdZka us i kni & çtuu dk; Deka ea fxM&ly, V vfHkdYi ukvka ds mi ; kx ij tkj fn; k gA osi ä&LrHk vfHkdYi uk, agS tks Kkr 0; kol kf; d fdLeka dh çfr—fr dk mi ; kx djrh gS fdLeka, oafcuk çfr—fr okys ijH{k.k dh ykbZuka dh tkp djrs gS 1/2 dEi Vu] 1982]A fxM&ly, V vfHkdYi ukvka ds fodYi ds : i e] dfyl bR; kfn 1/2006½ usgy fd, x, i ä&LrHk vfHkdYi ukvka dks çLrfor fd; k] ftl gamlgk us vka'kd : i l s çfr—fr vfHkdYi uk, a dgk] tgka ijH{k.k ykbZuka dh p% dks tkp fdLeka dks çfrLFkfi r djus dsfy, çfr—r fd; k tkrk gA

vka'kd : i l s çfr—fr vfHkdYi uk, a fxM&ly, V vfHkdYi ukvka dh riyuk ea çtuu ykbZuka ds p; u grq l Vhdrk ea l qkj djrs gA gky ds o'kkä e] 'kkdkrkdZka us i kni çtuu dk; Deka ea vka'kd : i l s çfr—fr vfHkdYi ukvka ds mi ; kx ij tkj fn; k gA vukt dh xqkoUkk ijH{k.k dsfy,] fLeFk bR; kfn 1/2009½ us vka'kd : i l s çfr—fr vfHkdYi uk dk çLrko fn; kA ; g vukt dh mi t vksj vukt dh xqkoUkk dsy{k.k k] nksuka dsfy, n{k fefJr e, My fo'ysk.k ds mi ; kx dks l {ke cukrk gA DykdZvksj LVQkukok 1/2011½ }kjk çkjHkd ih<h dsçtuu ijH{k.k dsfy, b"Vre vfHkdYi uk ftl eafcuk çfr—fr ; k dby vka'kd : i l s çfr—fr ijH{k.k jçkk, j l fEefyr gS fodfl r fd, x, FkA fofy; El bR; kfn 1/2011½ }kjk n{k vka'kd : i l s çfr—fr vfHkdYi uk dsfy, , d l j puk çfØ; k çkjEHk dh xbz gS tksa- l j.kh l s vo; oka dks gvkus ij vk/kfjr gA fofy; El bR; kfn 1/2014½ us vka'kd : i l s çfr—fr vfHkdYi ukvka ds puko ea vf/kd yphyi u dh vuqfr nusokys vka'kd : i l s çfr—fr vfHkdYi ukvka ds vf/kd 0; ki d oxZ dh l j puk djus dsfy, bl —f"Vdks k dks vksj vksx c<k; kA bl ds vfrfjä] ekqfjak bR; kfn 1/2014½ us VrbfVdy vksj eDdk ds çkjHkd ih<h dsçtuu ijH{k.k vka'kd : i l s çfr—fr vfHkdYi uk ds çn'kZu dk v/; ; uA fi, Qks bR; kfn 1/2016½ us n'kkZ k gS fd ds s LFkffud fopj.k&l çl j.k l j pukvka dk mi ; kx vka'kd : i l s çfr—fr vfHkdYi ukvka l fgr l eku vksj vl eku : i l s çfr—r vfHkdYi ukvka dsfy, ijs {ks= ea mi pkj çfr—fr ds vf/kd l eku forj.k dks çl r djus dsfy, fd; k tk l drk gA gk: u bR; kfn 1/2016a]b½ us ijH{k.k

cuke uo&fufe- ykbZuka, oai jH{k.k ykbZuka ds chp eW; kadu grqi wkZ, oavka'kd f=&i Fk Ø, l vfHkdYi ukvka dh fuekZk fof/k fodfl r dh gA gky gh e] dfyl bR; kfn 1/2020½ us 34 'kh?kz pj.k ds ijH{k.k kka dk , d dd LVMh çLrfor fd; kA bl ds çkn] l e] juh bR; kfn 1/2020½ us çkjHkd ih<h dsçtuu ijH{k.k dsfy, vka'kd : i l s çfr—fr vfHkdYi uk rS kj dj ijH{k.k kRed fLFkfr; kadh , d foLr Jçkyk dsfy, e tcr vfHkdYi ukvka dh igpku djus dsfy, vuq irk ijH{k.k fd; kA bl y[k eage çkjHkd ih<h dsçtuu ijH{k.k dsfy, n{k vka'kd : i l s çfr—fr vfHkdYi ukvka dh , d Jçkyk cukus dsfy, , d i) fr çLrfor djrs gA bu vfHkdYi ukvka ds eki nMka dk Hkh v/; ; u fd; k x; k gA

çkjHkd

bl [k.M ea l j puk fof/k ds çkjse appkZ djus l sigys dN egROI wkZ i f j Hk'kk, j , oa çkjHkd tkudkj nh xbz gA

fpä i) fr

eku yhf t, fd , d ijH{k.k dbZ okrkoj . kka ea çfr—r fd; k x; k gA ; gk ç; e] l ds ru fuEufyf [kr gS 3/4 ykbZuka dh l ç; k] e 3/4 i ; kbj .k dh l ç; k] b 3/4 [k.Mka dh l ç; k] r 3/4 çfr—fr dh l ç; k vksj k 3/4 vi wkZ [k.Mka dk väre vkdkj A

vka'kd : i l s çfr—fr vfHkdYi uk, a

vka'kd : i l s çfr—fr vFkok p-rep vfHkdYi uk, a , d h vfHkdYi uk, agksh gS ftuea çtuu ijH{k.k l fEefyr gksh gS vksj ftl gä ijsi ; kbj .k ea çfr—r fd, tkus dh vko'; drk gksh gS vksj çR; d i ; kbj .k ea ykbZuka ds p çfr'kr dks çfr—r fd; k tkrk gA tç e ifjos k gkrs gS rks dksZ, d ifjos k ea çfof"V; ka ds 1/6 1/2 oa Hkx dks bl çdkj çfr—r fd; k tk l drk gS fd çR; d çfof"V dk ijH{k.k e ifjos kka ea l s , d ea nks çfr—fr ds l kfk fd; k tkrk gA bu vfHkdYi ukvka l s vl; vfHkdYi ukvka dh riyuk ea çtuu ykbZuka ds p; u dh l Vhdrk ea l qkj gkus dh l Hkkouk gA e, My , oai jH{k.k kRed fol; kl

vka'kd : i l s çfr—fr vfHkdYi ukvka dh fLFkfr dks /; ku eaj [krsgq] , d svfHkdYi ukvka dsfy, ijH{k.k kRed e, My dks bl çdkj fn; k tk l drk g% tgkami pkj ds vuq i voykdu g%

$$y_{ij} = \mu + \tau_i + \beta_j + \epsilon_{ij}$$

tgk
 $y_{ij} = j \text{os } \frac{1}{4} [1 \ 2] \dots] \ b \frac{1}{2} [k.M \ \text{ea} \ i \ \text{os } \frac{1}{4} [1 \ 2] \dots] \ v \frac{1}{2} \text{ mi pkj}$
 ds vuq i voykdu g
 $\mu =$ l keku; ek/; çHkko g
 $\tau_i =$ i ok mi pkj çHkko g
 $\beta_j =$ j ok [k.M çHkko g
 $\varepsilon_{ij} =$; k-fPnd =v ?kVd gS tks iidN %0 $\sigma^2 \frac{1}{2}$ dk vuq j.k
 djrk gA bl vky[k ds ckn ds [kM ep 'kCn bykbZuB , oa
 mi pkj l eku : i l smi ; kx fd , x , gA

I jupuk fof/k

bl vuq dkku i) fr dk fodkl o"lz 2021&2022 eaHkkE—E
 vEi & Hkkjrh; —f" k l k[; dh vuq dkku l k.FkkU] ubZfnYyh
 ds ijh{k.k vfHkdYi uk foHkkx eafd; k x; k FkA

mi pkj I jupuk $v \frac{3}{4} s \ \frac{1}{2} ds$ l kFk çkjHkd i h<h ds
 çtuu ijh{k.k ds fy, vkf'kd : i l s çfr—fr $\frac{1}{p}$ —rep $\frac{1}{2}$
 vfHkdYi uk dh , d J[kyk uhpsfn, x, pj.kkadk mi ; kx
 djdsçklr dh tk l drh g%

çfle pj. $k \frac{1}{2} s^2$ mi pkjka ij fopkj djg tgkas ≥ 5 vo; oka
 ds l kFk , d fo"ke vHkkT; ; k $\frac{1}{4} [2] \dots] \ s \frac{1}{2}$ vo; oka dh
 vHkkT; ?krk gA rc] çkjHkd i ä; kadk mi ; kx djrs gq]
 $s \times s$ vkdkj ds $\frac{1}{2} \& \frac{1}{2}$ oxZ l kjf.k; ka dh I jupuk çkjHkd
 i ä; kadk mi ; kx djds fuEkuq kj dj%

i. çk—frd Øe eas vo; oka dh igyh çkjHkd i ä yA
 ii. igyh çfof"V dks vijofr j [krsgq] fi Nyh çkjHkd
 i ä; kadscn dh çR; d vkusokyh çfof"V; ka ea Øe'k%
 mod s ds l kFk $1 [2] \dots] \ s \& 1$ dh of) t kM/A

iii. bu çkjHkd i ä; ka dks pØh; : i l s $\frac{1}{2}$ mod $s \frac{1}{2}$ ds l kFk
 fodfl r djarkfd çR; d dsfy, $s \times s$ vkdkj dh $\frac{1}{2}$ — $1 \frac{1}{2}$
 oxZ l kjf.k; k çklr dh tk l dA

fjrh; pj. $k \frac{1}{2} s^2$ mi pkjka dks $s \times s$ l kj.kh ea 0; ofLFkr dja
 v[bl spj.k 1 eafodfl r (s-1) l kjf.k; ka ij vf/kjksi r dja
rrh; pj. $k \frac{1}{2}$ ç/kr sosLrEHk eaçfof"V; kads: i eafdl h
 fo'kSk sos çrhd ds fy, l keku; mi pkj l [; kvka ij
 fopkj djdspj.k 2 ea vkjksi r l kj.kh l $s \times s$ Øe dh , d
 v[$\frac{1}{2} \& 1 \frac{1}{2}$ ubZ l kj.kh fodfl r dja

prkzpj. $k \frac{1}{2}$ pj.k 3 ea çklr l kjf.k; ka l s s^2 mi pkjka ds
 v[re s vo; okaokyh i ä dks gV k nA

ipe pj. $k \frac{1}{2}$ vr ep pj.k 4 ea $\frac{1}{2} \& 1 \frac{1}{2}$ l kjf.k; ka l s Øe'k%
 igyh nw jh] —] $\frac{1}{2} \& 1 \frac{1}{2}$ ha i ä dks gVkdj v[igy $\frac{1}{2} - 1 \frac{1}{2}$ dks
 i ; kbj.k 1 l [; v['kSk i ; kbj.k 2 l s t kM/dj ifj.kkeh

vkf'kd : i l s çfr—fr vfHkdYi uk, a çklr dja l ç/kr
 l jf.k; ka dh i ä; k; eki nM/ka $v \frac{3}{4} s \ \frac{1}{2}$ mi pkjka dh l [; k]
 çR; d mi pkj dks 3 çkj çfr—r fd; k tkrk gSvFkkZr] $r \frac{3}{4} [3]$
 $e \geq 2$ i ; kbj.k dh l [; k] [k.M vkdkj $k \frac{3}{4} s \& 2$ okys $b \frac{3}{4} s$
 $\frac{1}{2} \& 1 \frac{1}{2}$ [k.Mka dh l [; k; k ds l kFk ifj.kkeh vfHkdYi ukvka ds
 [k.M cukrh gA

fp=. $k \frac{1}{2}$ eku yhft , $s \frac{3}{4} [5] \ v \frac{3}{4} 25$ mi pkjka dks tle nrk gA
 $s \times s$ Øe dh pkj l kjf.k; ka dh I jupuk pØh; : i l s 4
 çkjHkd i ä; $k \frac{1}{4} [2] [3] [4] [5] \ \frac{1}{4} [3] [5] [2] [4] \ \frac{1}{4} [4] [2] [5] [3] \ v [5] [4] [3] [2] \ \frac{1}{2}$
 dks fodfl r djds bl çdkj dh xbz g%

1	2	3	4	5	1	3	5	2	4	1	4	2	5	3	1	5	4	3	2
2	3	4	5	1	2	4	1	3	5	2	5	3	1	4	2	1	5	4	3
3	4	5	1	2	3	5	2	4	1	3	1	4	2	5	3	2	1	5	4
4	5	1	2	3	4	1	3	5	2	4	2	5	3	1	4	3	2	1	5
5	1	2	3	4	5	2	4	1	3	5	3	1	4	2	5	4	3	2	1

pkj l kjf.k; ka dks fodfl r djus ds mi jkar] 5×5 l kjf.k; ka
 ea $v \frac{3}{4} 25$ mi pkj dh 0; oLFkk uhpsfn, x, vuq kj dj%

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
21	22	23	24	25

vc] fi Nyh pkj l kjf.k; ka ij 25 mi pkjka dh 5×5 l kj.kh
 dks l çj bEi kst djds t[k fd pj.k 3 ea çrk; k x; k g
 vll; pkj ubZ l jf.k; k; fodfl r djg bl suhpsfn; k x; k g%

1	2	3	4	5	1	4	2	5	3	1	3	5	2	4	1	5	4	3	2
10	6	7	8	9	8	6	9	7	10	9	6	8	10	7	7	6	10	9	8
14	15	11	12	13	15	13	11	14	12	12	14	11	13	15	13	12	11	15	14
18	19	20	16	17	17	20	18	16	19	20	17	19	16	18	19	18	17	16	20
22	23	24	25	21	24	22	25	23	21	23	25	22	24	21	25	24	23	22	21

çR; d l kj.kh l sv[re i ä gV k, av[i q% l ç/kr pkj
 l kj.kh l si gyh] nw jh] rhl jh v[p[k i ä; kadks gV k, A
 i ä; ka dks [k.M ds : i ea n[krsgq] igyh nks l kjf.k; ka
 dks i ; kbj.k 1 v[vll; nks l jf.k; ka dks i ; kbj.k 2 l s
 l ç) djarkfd çkpy $v \frac{3}{4} 20$ e $\frac{3}{4} [2]$ b $\frac{3}{4} [20]$ r $\frac{3}{4} [3]$ v[$k \frac{3}{4} [3]$
 l kFk vkf'kd : i l s çfr—fr $\frac{1}{p}$ —rep $\frac{1}{2}$ vfHkdYi uk uhps
 fn [kk; s vuq kj çklr dh tk l d%

i ; kbj.k & 1

B1	B2	B3	B4	B5	B6	B7	B8	B9	B10	B1	B2	B3	B4	B5	B6	B7	B8	B9	B10
1	2	3	4	5	1	4	2	5	3	1	3	5	2	4	7	6	10	9	8
10	6	7	8	9	8	6	9	7	10	12	14	11	13	15	13	12	11	15	14
14	15	11	12	13	17	20	18	16	19	20	17	19	16	18	19	18	17	16	20

i ; kbj.k & 2

mi jka vfHkdYi ukvka dk v[r fopj.k v[d[ksudy
 n[krk dkjd Øe'k% 1-2923 v[0-5158 gA t[& t[s
 l [; k j[k, ac<Fh g[vfHkdYi ukvka dh d[ksudy n[krk

dkjd Hkh c<fha gA mnkgj.k ds fy,] d&ksfudy n{krk dkjd ¼20 ykbuka ds fy, 0-5152 vksj ¼42 ykbuka ds fy, 0-7943 gA

ifjppk

çkj&Hkd ih<h ds çtuu ijh{k.k ep fofHkUu okrkoj.k ka ea cMh I ç; k ea ¼ 1000½ çtuu ykbuka ; k çfof"V; ka dk eV; kadu I eku; r% 4 vksj çR; çd i; k&oj.k ea çfr—fr ds I kfk 2 I sde djusdh vko'; drk ghrh gA I d k/kukavksj chh dh deh t\$ h I hek i; k&oj.k vksj çR; çd çtuu j\$kk dsfy, HkV[kb/ka dh I ç; k de dj nrh gA , d h fLFkfr; kaep vka'kd : i I s çfr—fr vfHkdYi ukvka ea vPNh vuç; ksx {kerk ghrh gsvksj bl dk ykHkçn mi ; ksx fd; k tk I drk gA bl çdkj dh vfHkdYi ukvka grq, d I çpuk çfØ; k fofy; EI bR; kfn ¼2011] 2014½ }kjk nh xbl tks tfVy vksj I e; yas okyh FkhA ; gk& vka'kd : i I s çfr—fr vfHkdYi uk dh I çpuk grq, d ubzi) fr çLrkfor dh xbl g\$ tks mudh vuç; ksx {kerk eaof) djrs gq] fofy; EI bR; kfn ¼2011] 2014½ }kjk nh xbl i) fr dh rgyuk ea vkl ku gA

I UnHk

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