

# rh u i fr—fr; kaokyh vl eku [k.M vkdkjkaeal ek/ks vka'kd l rfy r viwk [k.M 1/2vfhkdYi ukvka dh , d ubz Jdkyk vf[kysk >k] fl uh oxh ] l hek tXxh] eks gk: u , oanobnz ddkj

Hkk—vuqj -&Hkkjrh; —f'k l ka [ ; dh vuq dkku l d.Fkku] ykbcjh , ob; ; ubzfnYyh&110 012] Hkkjr

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Lohdr% vxLr 2018

## Lkjrk

bl 'kksk i = earhu i fr—fr; kaokyh viwk [k.M vfhkdYi ukvka dh , d ubz Jdkyk l Lrkfor dh xbz gA ; svfhkdYi uk , a vka'kd i d j . k l rfy r gS tks , d l eug HkkT; l kgp; ; l ; kst uk dk ikyu djrh gA ; gka i j i k l r vfhkdYi uk , avl eku [k.M vkdkjkaokyh gSvks vl ery Hkkie ea i j h { k . k d j u s g r q m i ; D r g A b l d s v f r f j D r } ; svfhkdYi uk , a l ek / k s g S t k s , d s { k s = k a e a v u q j z k x { k e r k d k s l c y c u k r h g S t g k a i j , d g h L F k k u i j l H k h i f r — f r ; k a d k s l e k ; k s t r d j u k d f B u g k A

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## A new series of resolvable PBIB (2) designs in unequal block sizes with three replicates

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### ABSTRACT

In this paper, a new series of incomplete block designs with three replications has been proposed. These designs are partially variance balanced following a group divisible association scheme. The designs obtained here are with unequal block sizes and are suitable for experimentation in uneven land. Furthermore, these designs are resolvable, which enhances their application potential in regions where it may be difficult to accommodate complete replications at one place.

### idrlouk

tc i gkMla {ks=kaqrqubzi ks} ksf d; ka dk eW; ka lu d j u s d h v k o ' ; d r k g k s r c b u d k e W ; k a l u i g k M l a { k s = k a e a c u s g q i j h { k . k v u q d k k u d l b n k a i j g e g k l d r k g A b l i d k j d s { k s = k a e a } — f ' k ; k k ; H k k i e v D l j A p h & u h p h v k s i F k j h y h g k s h g A v f / k d o " k k z o k y s L F k k u k a i j } c M t 1 / 2 t y c g k o d h l H k k f o r f n ' k k e a y E c k b z d h v k j c u k , t k r s g S D ; k a d H k k i e v l e r y g k s h g S b l f y , v l e k u v k d k j d s [ k . M k a o k y h v f h k d Y i u k , a o k a n r g A , d g h L F k k u i j l H k h i f r — f r ; k a l f g r i j h { k . k d s f y , l r r { k s = f e y u s e a d f B u k b z g k s h g S b l f y , l e k / k s [ k . M v f h k d Y i u k v k a e p n k s ; k n k s l s v f / k d [ k . M k a d k s , d i w k z i f r — f r c u k u s d s f y , f e y k ; k t k r k g S f t l e a i R ; d V n V e W d k s c j k c j l d ; k e a i f r — r f d ; k t k r k g A

i S j l u , o a f o f y ; E l 1 / 4 9 7 6 1 / 2 } k j k v = p q V n V e W t g r q l e k / k s v f h k d Y i u k d h , d l e k k u ; J d k y k i L r r d h x b z f t l s a - v f h k d Y i u k d g k t k r k g A b u v f h k d Y i u k v k a g r q v / q , d i w k k d g k s k p k f g , t S h v i f j g k ; l c k / k k d s v f r f j D r [ k . M v k d k j k a i j d k b z v k s i f r c a k u g h a g A d k x s k e k 1 / 4 9 8 8 1 / 2 u s v f u ; f e r [ k . M v k d k j k a o k y h , Q k b u l e k / k s [ k . M v f h k d Y i u v k a d h d n J s . k ; k a d k o . k u f d ; k g A t k s b r ; k f n 1 / 4 9 9 9 1 / 2 u s a - v f h k d Y i u k v k a l s v l e k u [ k . M v k d k j k a o k y h d n l e k / k s [ k . M v f h k d Y i u k , a o ; q i l u d h v x o k y b r ; k f n 1 / 2 0 1 6 1 / 2 u s , Q k b u l e k / k s l r f y r v i w k [ k . M 1 / 2 h - c h - v k b z c h - 1 / 2 v f h k d Y i u k v k a v k s , Q k b u l e k / k s v k ; r k d k j i d k j d s v k a ' k d l r f y r v i w k [ k . M 1 / 4 h - c h - v k b z c h - 1 / 2 v f h k d Y i u k v k a d s l t u d h d n i ) f r ; k i l r k f o r d h f t u e a k k r , Q k b u l e k / k s 1 / 2 h - v k b z c h - 1 / 2

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**Hkjrh; d'k vuq dku if=dk**

vfhkdYi ukvka ds 0; ki drk vk0; ij vk/kkfjr vfu; fer vkdkj ds [k.M FkA

j k?kojko 1/4 962 1/2 usl eferh; vl eku [k.M 1/4 l - ; wch-1/2 0; oLFkk dsl 'tu , oaf0'ySk.k d k o.ku fd; k ft l ea nks vl eku vkdkj ds [k.M nks l a p r i h-ch-vkbZch-vfhkdYi ukvka , oa, Qkbu l ek/ks ch-vkbZch-vfhkdYi ukvka l sfy; sx, gA dly JSB bR; kfn 1/4 972 1/2 usnks vyx&vyx vfhkdYi uk, a VhVeh/4 dh l eku l d; k ds l kfk iz, kx fd; s rkd vl eku ifr-fr; ka ea vfu; fer vkdkj ds [k.M kaokys l rfy r f} xqkh vks f=xqkh vfhkdYi uk, ai klr gks tk, A l j d k 1/4 976 1/2 us ?kVr&c<fs [k.M vkdkj ea l eifr-fr l rfy r [k.M vfhkdYi ukvka dsl 'tu dh , d i) fr iLr r dhA xlrk , oa tkW 1/4 983 1/2 us l eifr-fr] f} xqkh i l j.k l rfy r dsl kfk&l kfk l e g HkT; 1/4 th-Mh-1/2 vfhkdYi ukvka dk mi ; kx d jrs gq vl eku [k.M vkdkj okys n{krk l rfy r [k.M vfhkdYi ukvka dsl 'tu ds fy, i) fr fodfl r dhA fl Ugk bR; kfn 1/4 996 1/2 us th-Mh- , oa f=dks kh; 1/4 h-ch-vkbZch-1/2 vfhkdYi ukvka da mi ; kx d jrs gq vl eku ifr-fr; kaokyh dN vufpr i l j.k l rfy r vfhkdYi uk, anhA >k bR; kfn 1/2 018 1/2 us vfn' kRed l gokl h i Hkkoka gsrq l rfy r l ek/ks [k.M vfhkdYi uk, j gsrwdk; Z fd; kA

; gka ij vl ery Hkie ij ijh{k.k gsrq vl eku [k.M vkdkj ka ea l ek/ks vkf'kd l rfy r viwkZ [k.M vfhkdYi ukvka dsl 'tu dh , d i) fr dk o.ku fd; k x; k gA l e fpr mnkgj .kka l fgr bl Jskh dh vfhkdYi ukvka dks i klr d j us gsrq l 'tu dh , d l keku; i) fr ij i f j p p k z dh x b z gA u h p s n h x b z l k g p ; Z ; k s t u k dh Hk 0; k [ ; k dh x b z gA

**Lkexh , oai jh{k.k fof/k**

b [k.M kaev VhVeh/4 gsrq, d [k.M vfhkdYi uk yhft, tgka b<sub>s</sub> [k.M ka dk i R; d mil e g k<sub>s</sub> (2 ≤ k<sub>s</sub> ≤ v; 1 ≤ s ≤ b) vkdkj ds gA ; fn [k.M vfhkdYi uk l ek/ks gS [k.M ifr-fr; ka euhfMf gA eku yhft, r i wkz i fr-fr; ka gS ftuea i R; d VhVeh/4 l eku l d; k eami flFkr gA eku yhft, y<sub>ijm</sub>, moE (m = 1, 2, ..., r) ifr-fr euhfMf] j oa e j = 1, 2, ..., b) [k.M e p i o a i = 1, 2, ..., v) l y k W i j v u f p ; k gS rc , d l ek/ks [k.M vfhkdYi uk gsrq; kx kRed j s k h; vpy i Hkko ekW y u h p s b l i z k j f n ; k x ; k g A

$$y_{ijm} = \mu + \tau_i + R_m + \beta_{j(m)} + e_{ijm}$$

ekW y ea μ l keku; ek/; gS τ<sub>i</sub>] i os VhVeh/4 dk i Hkko gS R<sub>m</sub>, m oE i fr-fr cukusdk i Hkko gS β<sub>j(m)</sub>, moE i fr-fr eaj os [k.M dk i Hkko gS vks e<sub>ijm</sub> 'k; ek/; , oa σ<sup>2</sup> i l j.k okyh l keku; r%forfjr Loræ ; knfPNd =QV; ka gA A i Lrkfor Jskh l s l e d /kr l Hk vfhkdYi ukvka gsrq fofHku VhVeh/4 ds  $\bar{V}(\tau_i \hat{=} \tau_j) \sigma^{-2}$  l h/ks i Hkko ds dUVRV l ds eW; ka du ds ek/; i l j.k dh x.kuk d j us ds fy, PROC IML ea, d SAS i k s e fy [k k x; k 1/4 y k k l a d s i k l mi y C/k gS A l p u k vk0; g 1/4 2008 1/2 dh x s & 'k; vk b k u eku ds (1/r) xqk l q x r ek/; } j k l eku l d; k okys mRi knka ds vk; rh; vfhkdYi uk ds l ki k mRi knka ds l h/ks i Hkkoka ds i nka ea i Lrkfor vfhkdYi uk ds i k e f . k d n {krk xqkka dh x.kuk dh x b z t g a i j r i Lr r vfhkdYi uk ea l h/ks i Hkkoka dh i fr-fr; ka dh l d; k d k s n' k k z k g A

**vfhkdYi ukvka dk l 'tu:** vl eku [k.M vkdkj ka ea l ek/ks [k.M vfhkdYi ukvka dh , d Jskh ftuea i kpy] VhVeh/4 dh l d; k (v) = 3t (t > 1), [k.M ka dh l d; k 1/4 b = b<sub>1</sub> + b<sub>2</sub>, b<sub>1</sub> [k.M k<sub>1</sub> vkdkj ds vks b<sub>2</sub> [k.M k<sub>2</sub> vkdkj ds gS 1/2 = 3 + 3 = 6, i fr-fr; ka dh l d; k (r) = 3, k<sub>1</sub> = 2t, k<sub>2</sub> = t, [k.M ka dh l d; k ftuea i Eke nks l gpj l kfk&l kfk mi flFkr gkrsgS(λ<sub>1</sub>) = 3, [k.M ka dh l d; k ftuea nks f} rh; l gpj l kfk&l kfk mi flFkr gkrsgS(λ<sub>2</sub>) = 1, i Eke l gpj ka dh l d; k (n<sub>1</sub>) = t - 1 f} rh; l gpj ka dh l d; k (n<sub>2</sub>) = 2t fuEu fyf [kr i z k j l s [k.M ka ev VhVeh/4 dks 0; oLFkr dj i klr dh tk l drh gA

ifr-fr;ka	[.M	VhVeh/4
I	i 1 4 7	... 1+(t-1)3 3 6 9 ... 3+(t-1)3
	ii 2 5 8	... 2+(t-1)3
II	iii 1 4 7	... 1+(t-1)3 2 5 8 ... 2+(t-1)3
	iv 3 6 9	... 3+(t-1)3
III	v 1 4 7	... 1+(t-1)3
	vi 2 5 8	... 2+(t-1)3 3 6 9 ... 3+(t-1)3

; g n s k k t k l drk gS fd ; g i) fr mi i fr-fr; ka vks nks fofHku i z k j ds [k.M vkdkj ka ea l n b l ek/ks h [k.M vfhkdYi uk, a l ftr d j rh gS A

I kgp; L; kst uk: mijkDr eaof.kr i) fr }kjk i ktr dh xbz vfhkdYi uk, avkáf'kd i d j.k l r f yr gáf tks, d l ey HkkT; I kgp; L; kst uk dk ikyu djrh gSft l ea VhVehVt fuEu dh Hkkar 3 drkj vkj t LrHka ea0; ofLFkr g%

1	4	7	...	3t - 2
2	5	8	...	3t - 1
3	6	9	...	3t

; gkaij nks VhVehVt i gysl gpj gáf; fn osvko; g dh , d gh drkj eagá vU; Fkk] os, d&nl js dsf}rh; I gpj gáf bl I kgp; L; kst uk ds ikpy bl idkj g%

$$v = 3t, n_1 = t - 1, n_2 = 2t, P_1 = \begin{bmatrix} t-2 & 0 \\ 0 & 2t \end{bmatrix}, \text{ oa}$$

$$P_2 = \begin{bmatrix} 0 & t-1 \\ t-1 & t \end{bmatrix}$$

; g fl ) djuk vkl ku gSfd I kgp; L; kst uk ds I Hkh ikpyd l d kka ds l kFk&l kFk vfhkdYi ukvka dh mijkDr Jskh dsfy,

(i)  $\sum_{i=1}^2 n_i = v - 1$

(ii)  $\sum_{k=1}^2 p_{jk}^i = n_j - \delta_{ij}; \delta_{ij} = \begin{cases} 0, & i \neq j = 1, 2 \\ 1, & i = j = 1, 2 \end{cases}$

(iii)  $n_i p_{jk}^i = n_j p_{ik}^j = n_k p_{ij}^k; i, j, k = 1, 2$

(iv)  $vr = \sum_{j=1}^m b_j k_j; j = 1, 2$

(v)  $\sum_{i=1}^2 n_i \lambda_i = \sum_{l=1}^2 (k_l - 1)$

vfhkdYi uk, a l r f yr gáf

mngj .k 1%eku yhf t, v=9 (v=3x3) VhVehVt gáf t gka t = 3 gáf mijkDr i) fr dk mi; ks djrs gq 6 vkj 3 vkdkj ds nks fofhkuUk [k.M vkdkjka ea, d l ek/ks [k.M vfhkdYi uk uhps nh xbz g%

ifr-fr;ka	[k.M	VhVehVt					
I	i	1	4	7	3	6	9
	ii	2	5	8			
	iii	1	4	7	2	5	8
II	iv	3	6	9			
	v	1	4	7			
III	vi	2	5	8	3	6	9

9 VhVehVt uhps fn; s x; s vk0; g ea0; ofLFkr fd; s tk l drsgáf t gkaij dkbZ Hkh VhVehVt i Fke l gpj gáf; fn osvko; g dh , d gh drkj eagá vU; Fkk f}rh; I gpj gáf

1	4	7
2	5	8
3	6	9

I kj .kh 1: ukSVhVehVt dsl Hkh i Fke , oaf}rh; I gpj kadh l ph gáf

VhVehVt	ife l gpj	f}rh; l gpj
1	4, 7	2, 3, 5, 6, 8, 9
2	5, 8	1, 3, 4, 6, 7, 9
3	6, 9	1, 2, 4, 5, 7, 8
4	1, 7	2, 3, 5, 6, 8, 9
5	2, 8	1, 3, 4, 6, 7, 9
6	3, 9	1, 2, 4, 5, 7, 8
7	1, 4	2, 3, 5, 6, 8, 9
8	2, 5	1, 3, 4, 6, 7, 9
9	3, 6	1, 2, 4, 5, 7, 8

dUMLVt dsl af.kr i d j.k vkadyu n{krk xqkkad , oa v, b<sub>p</sub>, b<sub>2</sub>, r, k<sub>p</sub>, k<sub>2</sub>, λ<sub>1</sub>, λ<sub>2</sub>, n<sub>p</sub>, n<sub>2</sub> tš s ikpy vkj i jh(k.k bdkb; kadh dgy l d; k N (< 100) I kj.kh 2 eanh xbz gáf I kj.kh 2 ea vfhkdYi ukvka ds i ktr fofhkuUk ikpyka dsl kFk&l kFk (N) < 99 VhVehVt ds dUMLVt dsl af.kr i d j.k vkadyu ek/; fn; s x, gáf

; g n[kk tk l drk gSfd n{krk xqkkad (E.F.) cgr vf/kd gSvkj ; g v dsc<e usds l kFk c<Fk gáf tš sgh v, 99 ij i gprk gSn{krk xqkkad 0.98 gks tkrk gáf

**ifj .kfe , oafoopuk**

; gka vl eku [k.M vkdkj okyh l ek/ks [k.M vfhkdYi ukvka ds l tu grq, d l kelU; i) fr fodfl r

Ilg .lh 2: vfhkdYi ukvka dh l ph

$\emptyset$ LA	V	$B_1$	$B_2$	R	$K_1$	$K_2$	$\lambda_1$	$\lambda_2$	$N_1$	$N_2$	N	$\bar{v}(\tau_i \Delta \tau_j) \sigma^{-2}$	E.F.
1	6	3	3	3	4	2	3	1	2	4	18	0.9333	0.7143
2	9	3	3	3	6	3	3	1	3	6	27	0.8333	0.8000
3	12	3	3	3	8	4	3	1	4	8	36	0.7879	0.8462
4	15	3	3	3	10	5	3	1	5	10	45	0.7619	0.8750
5	18	3	3	3	12	6	3	1	6	12	54	0.7451	0.8947
6	21	3	3	3	14	7	3	1	7	14	63	0.7333	0.9091
7	24	3	3	3	16	8	3	1	8	16	72	0.7246	0.9200
8	27	3	3	3	18	9	3	1	9	18	81	0.7179	0.9286
9	30	3	3	3	20	10	3	1	10	20	90	0.7126	0.9355
10	33	3	3	3	22	11	3	1	11	22	99	0.7083	0.9412

dh xbzgSA fodfl r vfhkdYi uk, arhu ifr—fr; kavks N% [k.M eav = 3t (t > 1) VNVeW l j puk grqgft l earhu [k.M 2t vdkj dsvkj 'ksh rhu t vdkj dsgA [k.M dk , d ; e iR; d 2t vkj t vdkj dk l kfk feydj , d iwkz ifr—fr cukrsgq ekuk tkrk gft l eaiR; d VNVeW Bhd , d ckj mi fLFkr jgrsgA ; svfhkdYi uk, avka'kd il j.k l rfyrgStksf}&l gpj Jskh l egg HkkT; l kgp; l; kstuk dk ikyu djrgh gA bl ds vfrfjDr] ; svfhkdYi uk, a l ek/ks gStks, d s{ks=kaevuqz, kx {kerk dks l cy cukrh gStgkaij , d gh LFku ij l Hkh ifr—fr; kadks l ek; kstr djuk dfBu gA

**fu"d"lz**

bl 'ksh i = earhu ifr—fr; kaokyh viwkz [k.M vfhkdYi ukvka dh , d ubz J[kyk iLrkfor dh xbzgStks vka'kd il j.k l rfyrgA ; g vfhkdYi uk, avl eku [k.M vdkjkaokyh gsvkj vl ery Hkfe ea ijh{k.k djus grq mi ; q r gA bu vfhkdYi ukvka dk igkMh {ks=ka ea ijh{k.k l pkyr djusean{krki wkz mi ; kx fd; k tk l drk gA

**vkhkj**

Lukrdkrj fo|ky; i h- th- Ldwy&Hkk—vuq l a ubzfnYyh }kjk i Fke ys[kd dks iklr foUkh; l gk; rk dk vkhkj 0; Dr fd; k tkrk gA

**l nHkz**

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