मृदा परीक्षण फसल अबुक्रिया सह-सम्बन्ध (एस.टी.सी.आर.) पर अरिलल भारतीय समन्वित अनुसंधान परियोजना से सम्बंधित परीक्षणणों का नियोजन, डिजाइनिंग और विश्लेषण

## PLANNING, DESIGNING AND ANALYSIS OF EXPERIMENTS RELATING TO AICRP ON SOIL TEST CROP RESPONSE CORRELATION

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## प्राक्कथन

फसल उत्पादब बढ़ाने के लिए विस्तारित रिंचाई सुविधाओं के वहत उच्च उपजशील किसमों और गहब बहु फसल प्रणाली के आने सो मृदा परीक्षण मानों पर आधारित संतुलित उर्वरक के गहलत्व कों भारतीय विएसानों ने भली-भांति समझा है । संतुलित उर्वरक की सिंफारिशों के लिए मृद्वा परीक्षण मानों और फुसल अनुक्रिया के बीच एक सम्बन्ध विकरित करने के विचार से भारतीय कृषि अनुसंधान परिषद ने सब् 1967-68 के दौराज मृदा परीक्षण फसाल अनुक्रिया सहसान्बनहा (Soil Test Crop Response Correlations) पर एक अरिवल भारतीय समन्वित अनुसंधाजन परियोजना (All India Coordinated Research Project) शुरू किया । इस परियोजना आँरा विवित 35 वर्षों मों लक्ष्षित उपज प्राप्त करने के उद्देश्य से भिन्न-भिन्न फसलों की उर्वरक्क अनुसचियां निर्धारित करने के लिए अनेक्क उर्वरक समायोजन सर्मीक्कण(fertilizer adjustment equations) एवं अंशांकन चार्ट(calibration charts) वैयार किए जाते रहे हैं । विगत वषों यो यह देखा गया है कि किसी एक अनुराधान केन्द्र पर किसी एक फसल की उर्वरक समायोजज समीकरण पर आधारित रिफारिशें संगत(consistent) नही हैं । इसके अलावा अधिकंशश मामलों मे बहु-समाश्रायण (multiple regression) विधि की सहायता से उर्वरक पोषकों की अनुकूल खुराके प्राप्त नही की जा सकी हैं ।

मृदा परीक्षण फसल अबुक्रिया सहसम्बन्ध पर अरिवल भारतीय समन्वित अनुरांधाज परियोजना के परियोजना समन्वयके (Project Coordinator), भारतीय मृदा विज्ञाज संसथाज (I.I.S.S.) भोपाल, इज सम्स्याओं के साथ भारतीय क्षषि सांरिव्यकी अनुसंधान संरथान, नई दिल्ली में आए और एक लम्बे विचार-विमर्श के बाद आपस में सहमति हुई कि भारतीय कृषि सांखि्यकी अनुराधाना सांस्थाज में एक परियोजना शुरू की जाएगी वाकि इन समसयाओं के समाधान की संभावनाओं को तलाशा जा राके और नई विश्लेषणात्मक तकनीकों का विकास करने के साथ-सातथ परीक्षाण करजो की बई डिज़ाइनों को सुझाया जा सके । विगत वर्षो के दौरान इस परियोजबा कों भारी मत्रा! में आंकड़े एकत्रित किए गए जिराक लिए इस परियोजना में एक डटर--बोस् बजाने की भी जरूरत थी । परिणाम स्वरूप दिनांक 01 मार्च, 2000 को भा.क्ट.सां.अभ. सं. में मृदा पर्रीक्षण फसल अनुक्रिया सहसम्बन्ध पर अखिल भारतीय समन्वित, अनुसंधान परियोजबा से सम्बंधित परीक्षणों का नियोजन, डिज़ाइनिंग और विश्लेषण"(Planning, designing and analysis of experiments relating to AICRP on Soil Test Crop Response Correlations) बामक एक सहयोगी परियोजना शुरू की गई ।

इस परियोजना के तहत अनुक्रिया अन्तरापृष्ठ (response surface) पद्धति की सहायता से उर्वरक पोषकों को अजकूलतम गानों को प्राप्त करने के लिए विश्लेषणात्मक तकनीक विकरित की गई है । इस पद्धुति को किसी एक विशेष सथान के मृदा परीक्षण मानों के नियत रैट के लिए उर्वरक पोषकों कीं अनुकूलतम जरूरत प्राप्त करने के लिए लागू किया जा सकता है । आंकड़ो मे आँउटलायरो (outliers) का पता लगाने के लिए विभिन्न समाश्रियण निदाब (regression dliagnostics) भी लागू किए गए और संभव उपचारों पर विचार किया गया है ।

विशिमन्न डिजाइब बिन्दुओं वाली अनेक बई डिजाइइनों का प्रस्ताव रखा गया है 1 कुछ ऐसी डिजाइने भी तैयार की गई जिनके उपचार संयोजनों में कार्बनिक और अकार्बनिक उर्वरक शमिल है । इब डिजाइनों पर भा.क्स.सां.अ.सं. में विचार-विमर्श करने के लिए एक बैठक की उई । इस बैठक में डा. जे.एस. सामरा, उप-महानिदेशक (एन.आर.एम.), डा.एन.एन.गोस्वामी और डाज्जी.एस.शेखों के अलावा जाने-माने मृदा वैज्ञानिको, परियोजना समन्वयक (एस.टी.सी. आर), एवं भाट.कृ.सां.अ.सं. और भा.मृ.वि.रां. के वैब्ञानिको के भाग लिया ।

मृदा परीक्ष्रण फहराल अनुक्रिया सहसम्बन्ध पर अरिवल भारतीय समज्वित अनुसंधान परियोजना की अणगाठनी कार्षशाला वमी विचार-विमर्श और तदन्वर परीक्षण के लिए सुझाए गए डिजाइडनों मो सो एवं डिज़ाइन को लिया जा रहा है । परीक्षणात्मक आंकड़ों और इसकी सहायक सचनायं एक्तित करने के लिए एक छोटा सा डाटा बेस भी तैयार किया गया है ।

मौ, भारतीय कृषि सांखिव्यकी अनुसंधान संरथान, नई दिल्ली और भारतीय मृदा विज्ञान संस्थान, भोपाल के वैज्ञाजिकों के प्रयासों की सराहना करता हूं जिन्होंने बड़े ही मनोयोग से इसे तैयार किमया है । आशा करता हूं कि इस परियोजना के परिणामों से मृदा परीक्षण फसल अजुक्रिसा सहसम्बन्ध के क्षेत्र में कान कर रहे कृषि कर्मियों को लाभ मिलेगा । मैं, यह की कामना करता हूं कि यह सहयोग भविष्य में और सुदृढ़ होगा ।


## FOREWORD

With the introduction of high yielding varieties and intensification of multiple cropping under expanded irrigation facilities, the importance of balanced fertilization based on soil test values was well recognized by the Indian farmers for increased crop production. With a view to develop a relationship between soil test values and crop response to fertilizer for balanced fertilizer recornmendations, the Indian Council of Agricultural Research launched the All India Coordinated Research Project on Soil Test Crop Response Correlation during the year 1967-68. This project over the last 35 years has generated numerous Fertilizer Adjustment Equations and calibration charts for prescribing fertilizer schedules for different crops for obtaining targeted yields. However, these fertilizer equations vary widely over the years for a crop at a particular centre. Moreover, at most of the time the optimal doses of the fertilizer nutrients could not be obtained using multiple regression method.

The Project Coordinator AICRP on STCR, Indian Institute of Soil Science, Bhopal approached IASRI, New Delhi with these problems. It was mutually agreed that a project would be taken up at IASRI to explore the possibility of solving these problems and to develop new analytical techniques and suggest new designs for carrying out experiments. As over the years, large amount of data have been gathered under the project, the creation of a database under the project was also solicited. Consequently, a Collaborative project entitled "Planning, Designing and Analysis of experiments relating to AICRP on soil test crop response correlation" was under taken at IASRI with effect from $1^{\text {st }}$ March 2000.

Under the project, an analytical technique has been developed for obtaining the optimal values of the fertilizer nutrients using Response Surface Methodology. This methodology can be applied usefully for obtaining optimal requirement of fertilizer nutrients for a given set of soil test values of a particular site. Various regression diagnostics to detect the outliers in the data were also applied and possible remedies were discussed.

A number of new designs have been proposed with various design points. Also,some designs were generated in which the treatment combinations included organic and inorganic fertilizers. These designs were discussed in a meeting held at IASRI in which Dr JS Samra, DDG (NRM); Dr NN Goswami and Dr.G.S.Sekhon, prominent Soil Scientists, Project Coordinator of STCR and Scientist of IASRI and IISS took part. One of the designs is going to be taken up for discussion and subsequent experimentation, in the next workshop of the AICRP on STCR. A small database was also created to store the experimental data and its ancillary information.

II appreciate the efforts of the Scientists of IASRI, New Delhi and IISS, Bhopal for bringing out this report. It is hoped that the agriculture workers in the field of Soil Test Crop Response Correlation shall be benefited by the findings of the project. I also wish that this collaboration would be strengthened in future.

(S.D. SHARMA) DIRECTOR

## आमुख

भारत्वीय कृषि अनुरांधान परिषद दारा 1967-68 के दौरान फसलों की उच्च पैदावार देने वाली किरमों के साथथ-साथ गहन खेती की दशाओं के लिए मृदा परीक्षण अंशांक्तन का विकास करने के उद्देश्य सो मृदा पर्रीक्षण फसल अनुक्रिया सहसंबंध(Soil Test Crop Response Correlations) पर एके अरिवल भारतीय समन्वित अनुसंधान परियोजना(All India Coordinated Research Project)शुरू की गई थी । फिलहाल, देश के विभिन्न सरय जलवायवीय क्षेत्रो (agro climatic zones) में इसके 16 केन्द्र है । गत 35 सालों के दौरान इस परियोजना मों अंकड़ों का बृहत् खण्ड तैयार किया गया है । विगत वर्षों में यह देखा गया कि किरी खास केन्द्र पर किसी एक फसल की उर्वरक समायोजन समीकरण(fertilizer adjustment equation) पर आधारित रिफारिशें संगत(consistent) नही हैं। इसके अलावा, बहु समाश्रीयण विधि(multiple regression) सो निकाले गए पोषक तत्वो (nutrients) के इष्टतम मान(optimall dose) हर समय सफल नही होते हैं । इसलिए यह जरूरी था कि अपनाई गई डिज़ाइब के हर पहलू की ओर इष्टतम माबों के निर्धारण के साथ-साथ सांरिव्यकीय विश्लेषण्य(statistical analysis) करने की जरूरी परिरिथतियों की समीक्षा की जाए ।

मृदा परीक्षण फस्सल अनुक्रिया सह-सम्बन्ध पर अखिल भारतीय समन्वित परियोजना के परियोजना समन्वयक(Project Coordinator), भारतीय मृदा विज्ञान संरथान, भोपाल दारा भारतीय कृषि सांखिव्यकी अनुसंधान संरथान, नई दिल्ली, के परीक्षण अभिकल्पना(design of experiments) प्रभाग के वैज्ञानिकों के साथ विचार-विमर्श के दौरान इन समरयाओं पर प्रकाश डाला वाया और आपसी सहमति हुई कि भारतीय कृषि सांख्यिकी अनुसंधान संरशान में एक परियोजना शुरूू की जाए वाकि इन समस्याओं के समाधान की संभावनाएं तलाशी जा सकें और बई डिँजाइइज विकरित करने के साथ-साथ आंकड़ों का विश्लेषण तो किया ही जाए साथ ही उनकी व्याखख्या की की जाए तथा मृदा परीक्षण अंशांक्तन (soil test calibration) गं सुधार लाया जाए । इसके फलस्वरूप "मृदा परीक्षण फसल अनृक्रिया सह-सम्बन्ध पंर अखिल भारतीय समन्वित अनुरांधाज परियोजना सो सम्बंधित परीक्षणों का नियोजन, डिजाइनिंग और विश्लोषण" (Planning, designing and analysis of experiments relating to AICRP on Soil Test Crop Response Correllations) बामक एक परियोजना 1 मार्च, 2000 से भारतीय कृषि सांरिव्यकी अनसंधान संसभान मे शुरू की गई ।

इस रिपोर्ट में एस.टी.सी.आर. परियोजना की जरूरतों के आधार पर भिन्न-भिन्न डिजाइन बिन्दुओंDesign points) सहित ( $5 \times 4 \times 3$ ), $(4 \times 4 \times 3),(4 \times 4 \times 4)$ इत्यादि डिजाइनों की किरम से अनेक् डिजाइनों का प्रसताव रखा गया है । अनुक्रिया अन्तरापृष्ठ (response surface) पद्धति कर अधारित एक विश्लोषणात्मक विधि विकरित की गई है । इस विधि में यदि मृदा परीक्षण मान उपलब्ध हों तो किसीदी एक खास सथान के लिए नाईद्रोजन, फासफोरस और पोटैशियम उर्वरक्ह पोषकों के इष्टतम मान जिकाले जा सकते है । विभिन्न सहयोगी केन्दों के आंकड़ों का विश्लोषण करते समय यह देखा गया कि सभी मामलों में जहां अनुक्रिया अन्तरापृष्ठ पद्धति से पल्याण बिन्दु (saddle point) के रूप में एक स्तब्ध बिन्दु (stationary point) बना याजि यह ब वो अधिकृतम था और न ही न्यूनतम था । इन मामलों में स्तब्ध बिन्दु के परिवेश(vicinity) में अनुक्रिया अन्वरापृष्ठ की संभावना का पता लगाया गया है । लक्षित उपज विधि के माध्यम से उर्वरक पोषकों नाईट्रोजन, फ्फ़ोरस और पोटैशियम के इष्टतम मानों को अनुक्रिया अन्वरापृष्ठ पद्धति के परिप्रेक्ष्य में सत्यापित किया गया ।

हम, डा. एस.डी. शर्मा, निदेशक, भारतीय कृषि सांख्यिकी अनुसंधान संरथाब, नई दिल्ली के अत्यंत आभारही हैं कि उन्होंजे इस परियोजना में गहरी दिलचसपी लेते हुए लगातार हमारा उत्याहवर्थन तो किम्या ही साथ ही सुझाव देने के साथ-साथ हमें सभी सूपिधाएं भी उपलब्ध की हैं । हम, डा. वी. के. गुप्ता, संयुक्त निदेशक, भा.क्.सां.अ.सं. एवं पूर्व प्रधान, परीक्षण अभिकल्पजा पभभाग का भी हार्दिक धन्यवाद अदा करते हैं कि उन्होंने इस रिपोर्ट में प्रस्तावित बतए डिजाइनों के विकास में अपना बहुमल्य योगदान दिया है और पूरी परियोजना के दौरान वे लगावार हमारे प्रेरणा सोत बने रहे और बहुमूल्य सुझाव दिए ।

हग, डा. रवीज्द्र श्रीवास्तव, प्रधान वैज्ञानिक, परीक्षण अभिकल्पना के बड़े ऋणी है जिन्होंने रिपोर्ट की गुणवत्ता में सुधार लाने के लिए सृजनात्मक सुझाव दिए और बहुमूल्य टिप्पणियां करी । हम, बाह्य रेफरी के बहुमूल्य सुझावों की भी सराहनाँ करते हैं।

हम, शी उदयवीर रिंह, तकनीकी अधिकारी, टी-5 का भी हार्दिक आभार व्यक्त करते हैं जिन्होने इस रिपोर्ट को वैयार करने के दौरान पुरे लगब और निष्ठा से कार्य किया और अपन्त अमूल्य दोगदान दिया । आंकड़ों के संक्कलन में डा. एस.एम.जी. सरन, वैज्ञानिक के बहहुमूल्य सहायता की इसके लिए हम उनका हार्दिक आभार व्यक्त करते हैं ।

अन्व में हम श्री ए.पी. सिंह, प्रभारी हिन्दी अनुभाग के अत्यन्त ही आभारी है कि उन्होने आरम्भ के कहछ पृष्ठों का अनुवाद अत्यन्त ही सरल एवं सुबोध भाषा में किया ।

## PREFACE

All India Coordinated research project on Soil Test Crop Response Correlation was launched by ICAR during 1967-68 to develop soil test calibration for condition of intensive agriculture with high yielding varieties of crops. Presently there are 16 centres in different agro climatic zones of the country. Over the last 35 years a large volume of data have been generated under the project. It was observed that the recommendations based on the Fertilizer Adjustment Equations are not consistent over the years for a crop at a particular centre. Moreover, the optimal values of the nutrients as derived by the method of multiple regression is not successful every time. Therefore, it was necessary to review the overall aspects of the design adopted, determination of the optimal values, and the conditions necessary for carrying out the statistical analysis.

The Project Coordinator AICRP on Soil Test crop Response Correlations, Indian Institute of Soil Science, Bhopal highlighted these problems in a discussion with the Scientists of Division of Design of Experiments, IASRI, New Delhi and it was mutually agreed that a project would be taken up at IASRI, to explore the possibility of solving these problems and to develop new designs and the analysis of data, their interpretation and improvement in soil test calibration. Consequently, a project entitled "Planning, Designing and analysis of experiments relating to AICRP on Soil test Crop Response Correlations" was initiated at IASRI w.e.f. $1^{\text {st }}$ March 2000.

In this report, a number of designs have been proposed from designs of type ( $5 \times 4 \times 3$ ), $(4 \times 4 \times 3),(4 \times 4 \times 4)$ etc. with different designs points, based on the requirements of STCR project. An analytical technique has been developed based on Response surface methodology. In this method, the optimal values of Nitrogen, Phosphorus and Potassium fertilizer nutrients could be derived for a particular site if its soil test values are available. While analyzing the data of different cooperating centres, it was observed that in almost all the cases the response surface methodology produced the stationary point as saddle point i.e. neither maxima nor minima. In such cases exploration of the response surface in the vicinity of the stationary point has been attempted. The optimal values of the fertilizer nutrients Nitrogen, Phosphorus and Potassium derived through Targeted Yield Approach were verified in the light of Response Surface Methodology.

We express our deep sense of gratitude to Dr. S.D. Sharma, Director, IASRI, New Delhi for his keen interest in the project, constant encouragement, suggestions and for the facilities provided. We are also thankful to Dr. V.K.Gupta, Joint director, IASRI and Ex-Head, Division of Design of Experiments, for his contributions in the development of new designs that are proposed in this report, his constant motivation and valuable suggestions during the entire period of the project.

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## Chapter -I

## INTRODUCTION

The balanced application of fertilizer particularly the major nutrients, N P and K in optimum quantity, based on soil test and crop requirement is one of the most vital aspects for sustaining higher agricultural production. This requires the application of optimal and balanced quantity of fertilizers in right proportion through appropriate method and time of application for a specific soil-crop-climate situation. It ensures increased quantity of produce, maintenance of soil productivity and the most efficient and judicious use of applied fertilizers. Thus in this context the soil fertility evolution and refined fertilizer prescription for sustained agricultural production is of great importance to farming community. Hence, the soils have to be tested precisely for their available nutrient status for making fertilizer recommendations based on crop response and economic circumstances.

The determination of the amount of fertilizer that should be applied to a crop would be simple if a chemist could analyze the soil to measure the amount of available plant nutrients present in the soil and to calculate the amount of that nutrient which should be applied to correct the deficiencies. It is unfortunate that the determination of fertilizer requirements is not as simple. As every soil chemist knows, there are basic problems in interpreting soil test values in terms of nutrient availability to crops due to the interacting effects of other soil constituents, surface reactions, the changes that may occur in test values both laterally across farmers' fields and vertically down the soil profile and to all these factors may be added the uncertainties of weather, effects of crop variety, disease, pests etc. Any suggestion, therefore, that fertilizer requirement can be determined solely on the basis of a simple laboratory analysis of a few grams of soil, represents a vast oversimplification of a highly complex system. Nevertheless soil analysis can provide useful information on the effect that fertilizers are likely to have on yields, and it is important to use this information for the estimation of fertilizer requirements. Soil tests can provide a valuable piece of information and as such should be used in conjunction with such other information that is available for the estimation of fertilizer requirements.

### 1.1 All India Coordinated Research Project on Soil Test Crop Response Correlations

Soil test crop-response studies has been going on for a quite a long period of time both in India and abroad. With the introduction of high yielding varieties and intensification of multiple cropping under expanded irrigation facilities, the importance of balanced fertilizer use for increased crop production was well recognized by the Indian farmers.
Since the fertilizer recommendations for crops based on simple field trials did not give the expected yield response; a need arose for the refinement of fertilizer prescription for varying soil test values for economic crop production. Against this background, the All India Coordinated Research Project on Soil Test Crop Response Correlation was initiated during the year 1967-68.

### 1.2 Objectives of AICRP-STCR

The project has the following objectives.
(i) To develop relationships between soil test values and crop response to fertilizers in order to provide calibration for fertilizer recommendations based on soil testing.
(ii) To obtain a basis for making fertilizer recommendations for targeted yields.
(iii) To evaluate various soil test methods for their suitability under field conditions.
(iv) To evaluate the joint use of chemical fertilizers and organic manures for enhanced nutrient use efficiency.
(v) To derive a basis for making fertilizer recommendations for a whole cropping system on initial soil test values.
1.3 Cooperating Centres, location, soil type and agro-eco region

There were eight centers under the project to begin with. During 1970-71, five more centres were added. One centre (Raipur) was added during the year 1981-82. Currently, STCR project is having Sixteen cooperating centres. The location, year of start, their agro-eco region etc. are shown in Table 1.1

### 1.4 Statistical design and conduct of experiments under STCR

The main objective of STCR consists of developing a relationship between soil test and crop response to fertilizer in order to provide a calibration for balanced fertilizer recommendations based on soil testing. Since different levels of uncontrollable variables e.g. Soil fertility, cannot be expected to occur at one place, different sites have to be selected to represent different levels of soil fertility. In order to tide over the management problem conducting a field experiment at different sites differing from each other in the extent of uncontrolled variables, artificial fertility gradients in 4 adjoining plots are created by applying different amounts of fertilizers to a preceding non-experimental crop. Under the four large plots (strips) first strip receives no fertilizer, while second, third and fourth strips receives half, one and two times the standard dose (X) of $\mathrm{N}, \mathrm{P}$, and K respectively.

The standard dose ( X ) being: $\mathrm{N}_{1}=150 \mathrm{Kg} / \mathrm{ha}^{-1}, \mathrm{P}_{1}=$ Phosphorus equivalent to the critical point in the $P$ fixation studies of that field and $K_{1}=$ enough to give $150 \mathrm{Kg} / \mathrm{ha}^{-1}$ of exchangeable K . Then a preparatory crop (or exhaust crop) has to be grown so that the fertilizers undergo reaction with the soil, plant and microbiological agencies. After the harvest of the preliminary crop, each of the strips is subdivided into 27 subplots, of which 6 are control plots and 21 receives various combinations of the levels of Nitrogen, Phosphorus, and Potassium, in a fractional factorial design.

During the experimentation, package of practices recommended for the test crop is followed for the experimental crop. The soil samples from all these plots are collected and analyzed for various soil characters. The yield and plant nutrient uptake are recorded on the harvest of crop.

### 1.5 Analytical approaches used by STCR

It is known that the yield of a crop is a function of several factors, which may be expressed as

$$
\text { Yield }=f \text { (crop, soil, climate, management })
$$

The authenticity and soundness of fertilizer recommendations will depend upon the thoroughness and quality of the background research. There are several approaches, which are followed worldwide over to derive the basis of judicious soil and fertilizer nutrient management. Some of them are: Soil analysis and correlation, soil fertility and survey, critical soil test levels, Mitscherlich's method (1909) and its modification by Mombiella et al.(1981), Bray's method (1948),foliar diagnosis, Colwell's method using simultaneous regression and orthogonal polynomials (1978), Ramamurthy's(1967) inductive approach (targeted yield) and integrated soil test crop response approach. Some other methods include, Linear response plateau models(LRP), Quadratic response plateau models(QRP) and QUEFTS( Quantitative Evaluation of Fertility of Tropical Soils).

Under the STCR project two approaches are used: multiple regression approach and Targeted yield approach(discussed in section 2,4)
Multiple regression is being used to calculate the dose of nutrient (s) required to obtain the maximum yield of crops under given set of experimental conditions. It can further be used to calculate the economic dose of fertilizer nutrients by incorporating a constant factor i.e. per unit cost of input (fertilizer) in the original equation. In this approach yield is regressed with soil nutrients, fertilizer nutrients, their quadratic terms and the interaction term of soil and fertilizer nutrients.

## Conditions for application of the technique of multiple regression:

As per the manual on statistical computation (STCR publication, 1985), the following conditions are required to be fulfilled for deriving the optimum values of the nutrients.
(a) Soil test crop response calibration for economic yield of a crop is possible only when the response to added nutrients follow the law of diminishing returns. i.e. the signs of partial regression coefficients of linear, quadratic terms of nutrients and their interaction with available soil nutrients should in general be positive, negative and negative (,,+-- ) respectively.
(b) The coefficient of determination $\left(\mathrm{R}^{2}\right)$ should be high.
(c) The partial regression coefficients should be statistically significant.
(d) The experiment should have sufficient design points i.e. the number of treatments should be at least two or more than the number of variables in the model.

### 1.6 Collaboration of AICRP. STCR with IASRI

The criterion mentioned in the previous section is seldom fulfilled under the STCR project data. In such cases the optimum values of the nutrients cannot be derived or even if they could be derived, are either too high or too low.
Keeping in view of the above problems and for better analysis of data, their interpretation and improvement in soil test calibration, the project coordinator AICRP on STCR, Indian Institute of Soil Science, Bhopal, formally approached IASRI, New Delhi for collaboration. As large amount of data have also been gathered under the project, the creation of a database under the project was also solicited. Consequently a project entitled "Planning, designing and analysis of experiments relating to AICRP on soil test crop response correlation" was under taken at IASRI with effect from $1^{\text {st }}$ march 2000 with the following objectives:

1. To improve the existing methodology for analysis of data of ongoing STCR experiments.

2 To carry out planning and designing for the conduct of new set of experiments and subsequently to carry out the analysis of data.
3. To develop database for STCR experiments.

While analyzing the data of past STCR experiments at IASRI, it has been observed that the specific conditions, mentioned earlier, are seldom fulfilled. This is basically the problem of Regression and Response Surface Methodology and has to be tackled in the light of the same. Moreover in the model adopted by the STCR project, terms like Interaction (Fertilizer N x Fertilizer P) or $\mathrm{SN}^{2}, \mathrm{SP}^{2}, \mathrm{SK}^{2}$ etc. have not been included. A proper response surface could only be fitted by carefully choosing the variables in the model and the set of meaningful treatment with sufficient design points. Besides this, certain other areas, which have to be looked into, are:

1. Whether the fertility gradient has been created in each experiment? Which is the basic necessity of the STCR project. This can be seen by assuming the four strips ( $0 \mathrm{X}, 1 / 2 \mathrm{X}, \mathrm{X}$
and 2 X ) as four replications and then performing the analysis of variance. If the replication (Strip) effect is not significant, then it can be said that there is no difference between the fertility gradients and therefore fertility gradient has not been created. In such cases the whole experimental field shall behave as a homogeneous field and the very purpose of creating artificial fertilizer gradients stands vitiated.

Another way is to include the replication as an independent variable in the model to see whether there is any significant difference between the strips.
2. It has been observed that there is considerable variation among the magnitude, sign and significance of the partial regression coefficients for a particular crop or a variety of a crop at the same site over the years. This means that the recommendation of fertilizer nutrients to the farmer will vary from year to year for the same crop. Efforts are to be made to understand the problem and for its possible solution, in the light of response surface methodology.

3 The treatment structure has to be reviewed. It is generally observed that at different centers the experiments are being conducted with different set of treatments without verifying the statistical prerequisites, which in turn makes the analysis difficult and the results unachievable. In order to streamline the treatment structures, it is necessary to consult a statistician before conducting any experiment. Haphazard way of choosing treatments makes the analysis difficult and does not serve the purpose. Attempts will be made to develop a suitable fractional factorial design, which can meet the objectives of the experiment. Of course this will require the combined effort of soil scientists and statisticians.
4. At present, when the optimal fertilizer doses are not derivable using the existing multiple regression model of the STCR project, then a fertilizer adjustment equation, as said earlier, for each nutrient is developed, which is based on the basic data of Nutrient requirement $\mathrm{kg} / \mathrm{q}$, Percent contribution of fertilizer from available soil nutrients and contribution from added fertilizer nutrients and then the optimum values are calculated for each nutrient. Since this method does not seem to have a sound statistical background, attempts will be made to arrive at a statistical solution based on response surface methodology.

Attempts will also be made to see whether it is possible to pool the fertilizer adjustment equations over the years. This aspect will be possible once the statistical solution to the Fertilizer Adjustment Equation is arrived at.

For the benefit of research workers and the scientists of the STCR project, a database in MSACCESS would be developed at IASRI. The experimental data received from different cooperating centers, would be fed into the database. This will put all the experiments conducted under the STCR project at a central place. Later we propose to place this at a central on-line sever so that all the scientists working in the project at different cooperating centres can access it through the WEB. This needs some time, proper infrastructure and mainly the cooperation of AICRP on STCR. This aspect would be taken up in a subsequent study.
Table 1.1 Experimental Sites, Agro -Eco region and Soil types of different cooperating centres of the STCR project

| S.No. | Cooperating Centre | Date of Start | Experimental Site | No. | Agro- Eco Region | No. | Agro- Eco <br> Subregion | Soil Type |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | UAS, Bangalore | 1.10 .1970 | Bangalore | 8 | Hot semi- arid | 8.2 | Hot Moist semiarid | Medium to deep red loam |
| 2. | OUAT, Bhubaneswar | 1.9.1996 | Bhubaneswar | 12 | Hot sub humid | 12.2 | Hot Moist sub humid | Medium to deep loamy red \& red lateritic soil |
| 3. | RAU, Bikaner | 1.9 .1996 | Bikaner | 2 | Hot arid | 2.1 | Hot hyperarid | Shallow \& deep sandy desert soils |
| 4. <br> 5. | TNAU, Coimbatore | 1.4.1967 | Coimbatore | 8 | Hot semiarid | 8.1 | Hot dry semiarid | Medium deep to deep, loamy to clayey mixed red \& black |
| 5. | HAU, Hisar | 1.4 .1967 | Hisar | 2 | Hot arid | 2.3 | Hot typic arid | Deep loamy desert soils |
| 6. | APAU, Hyderabad | 1.4 .1967 | Hyderabad | 7 | Hot semiarid | 7.2 | Hot Moist semiarid | Deep loamy and clayey mixed red \&black |
| 7. | JNKVV, Jabalpur | 1.4.1967 | Jabalpur | 10 | Hot sub humid | 10.1 | Hot dry sub humid | Medium black |
| 8. 8 | BCKV, Kalyani | 21.11.1997 | Kalyani | 15 | Hot semiarid | 15.1 | Hot Moist sub humid | Deep loamy to clayey alluvial derived |
| 9. | PAU, Lühiana | 1.4 .1967 | Ludhana | 4 | Hot semi- <br> arid | 4.1 | Hot Moist semianid | Deep loamy alluvial |
| 10. | IARI, New Demi | 1.5.1967 | New Delhi | 4 | Hot semiand | 4.1 | Hot semianid | Deep loamy alluvial derived |

Table 1.1 (contd.) Experimental Sites, Agro -Eco region and Soil types of different Cooperating centres of the project

| S.No. | Cooperating <br> Centre | Date of <br> Start | Experimental <br> Site | No. | Agro- Eco <br> Region | No. | Agro- Eco <br> Subregion | Soil Type |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 11. | HPKV, Palampur | 1.7 .1970 | Palampur | 14 | Warm sub-humid <br> to humid with <br> inclusion of <br> perhumid | 14.3 | Warm humid to <br> perhumid <br> transitional | Podzolic |
| 12. | GBPUA\&T, Pantnagar | 1.4 .1970 | Pantnagar | 14 | Warm sub-humid <br> to humid with <br> inclusion of <br> perhumid | 14.5 | Warm <br> humid/per <br> humid | Medium to deep <br> loamy tarai |
| 13. | RAU, Pusa | 1.12 .1967 | Pusa | 13 | Hot sub <br> humid | 13.1 | Hot dry to moist <br> Sub humid | Deep loamy <br> alluvial derived |
| 14. | MPKVV, Rahuri | 28.10 .1970 | Rahuri | 6 | Hot semi- <br> arid | 6.1 | Hot dry semi- <br> arid |  <br> medium loamy <br> black |
| 15. | IGKVV, Raipur | 1.4 .1981 | Raipur | 11 | Hot/Moist/dry <br> sub humid <br> transitional | - | Deep loamy to <br>  <br> yellow |  |
| 16 | KAU, Vellanikkara | 1.11 .1996 | Vellanikkara | 19 | Moist humid-per <br> humid | 19.2 | Hot moist sub <br> humid to humid <br> transitional | Deep loamy to <br>  <br> lateritic soils |

## Chapter -II

## REVIEW OF LITERATURE

### 2.1 Early work done on Soil-Test Crop Response

The yield response to application of most nutrients follows the law of diminishing returns. Each added fertilizer increment produces a progressively smaller yield increase, finally reaching an asymptote. The economic benefit of fertilization is a function of yield response in relation to fertilizer cost. The law of diminishing returns can be approximated by a curvilinear equation i.e. Mitscherlich equation (1909)

$$
\begin{align*}
& \log \mathrm{A}-\log (\mathrm{A}-\mathrm{Y})=\mathrm{CX} \\
& \text { or, in the form } \mathrm{Y}=\mathrm{A}\left(1-\mathrm{e}^{-\mathrm{CX}}\right) \tag{2.1}
\end{align*}
$$

where Y is yield expressed on a relative basis as obtained in proportion to a limiting factor, X ., " A " is the maximum yield, and " C " is a constant describing the shape of the curve (generally between 0.1 and 1 , the higher the value the sooner the curve reaches maximum). Thus as the value of X increases, Y increases but at ever diminishing amounts.
The first approach towards the establishment of a soil test calibration was attempted by Bray (1948) which is a modification of Mitscherlich equation and known as Mitscherlich-Bray model as follows:

$$
\begin{equation*}
(\mathrm{A}-\mathrm{Y}) / \mathrm{A}=\exp \left(\mathrm{b}_{1} \mathrm{x}+\mathrm{b}_{2} \mathrm{t}\right) \tag{2.2}
\end{equation*}
$$

In this method, the yield is converted to relative yield, which is then correlated with soil test and fertilizer rate by the equation.
Where, A is the maximum yield, Y is the relative yield, x the fertilizer rate and t the soil test value. This method suffers from the drawback that in order to have a reasonable estimate of fertilizer requirements, the maximum yield has to be some desirable proportion of the yield (e.g. $95 \%$ ) and the maximum is approached only as fertilizer rate approaches infinity.
The Mitscherlich-Bray equation was modified by Mombiela et al (1981)

$$
\begin{equation*}
\mathrm{Y}=\mathrm{A}\left\{1-\mathrm{e}^{-\mathrm{C}[\mathrm{X}+\mathrm{f}(\mathrm{~T})]}\right\} \tag{2.3}
\end{equation*}
$$

Where, Y is a predicted yield obtained by application of X units of Nutrient (fertilizer), say P, to a soil with a P soil test value T . The parameter A is defined as maximum yield and C is proportionality constant related to the efficiency of soil and fertilizer $P$. The function $f(T)$ relates to an amount of plant available $P$ in the soil. Colwell(1974) suggested a method of calculating optimal fertilizer P by the following equation:

$$
\begin{equation*}
P_{R}=(1 / C) \log (C A / p(1+R))-b T \tag{2.4}
\end{equation*}
$$

Where, p = price of fertilizer/price of crop, $\mathrm{R}=$ marginal rate of return(or interest rate), and other terms are as previously defined under the modified Mitscherlich equation.

A number of different yield functions have been proposed and used in the past, representing the relationship between crop yield and fertilizer application. Heady, Pesek and Brown (1955), Heady (1961), Abraham and Rao (1966) etc. have studied the suitability of a number of such relationships.

Heady et al. (1955) favoured the model.

$$
\begin{equation*}
\mathrm{Y}_{\mathrm{ij}}=\mathrm{A}_{\mathrm{i}}+\mathrm{B}_{\mathrm{i}} \mathrm{X}_{\mathrm{ij}}^{1 / 2}+\mathrm{C}_{\mathrm{i}} \mathrm{X}_{\mathrm{ij}}+\mathrm{D}_{\mathrm{i}} \mathrm{X}_{\mathrm{ij}}^{3 / 2}+\ldots+\varepsilon \tag{2.5}
\end{equation*}
$$

where $A_{i}, B_{i}, C_{i}$ etc. are the parameters to be estimated, $\varepsilon$ is the random error distributed as $\mathrm{N} \sim\left(0, \sigma^{2}\right)$.

While Abraham and Rao preferred the model,

$$
\begin{equation*}
\mathrm{Y}_{\mathrm{ij}}=\mathrm{A}_{\mathrm{i}}+\mathrm{B}_{\mathrm{i}} \mathrm{X}_{\mathrm{ij}}+\mathrm{C}_{\mathrm{i}} \mathrm{X}_{\mathrm{ij}}^{2}+\ldots+\varepsilon \tag{2.6}
\end{equation*}
$$

because of their simplicity in comparison to the traditional exponential growth function.

$$
\begin{equation*}
\mathrm{Y}_{\mathrm{ij}}=\alpha_{\mathrm{i}}+\beta_{\mathrm{i}} \exp \left(\gamma_{\mathrm{i}} \mathrm{X}_{\mathrm{ij}}\right) \tag{2.7}
\end{equation*}
$$

where $\alpha_{i}, \beta_{i}$ and $\gamma_{i}$ are site parameters. These authors showed that the polynomials (2.5) \& (2.6) give on an average a better regression fit of yield data. Also the polynomials have an additional advantage that they can accommodate a maximum yield, which the exponential models cannot.

Colwell (1967) developed a method wherein he used orthogonal polynomials to fit the data of n sites of a region at each of which a Randomized fertilizer experiment has been carried out with same $r$ treatments (rates of fertilizer applications). He described the calibration equation as below:

$$
\begin{equation*}
\mathrm{Y}=\mathrm{P}_{0} \xi_{0}+\mathrm{P}_{1} \xi_{1}+\mathrm{P}_{2} \xi_{2}+\mathrm{P}_{3} \xi_{3}+\ldots+\varepsilon \tag{2.8}
\end{equation*}
$$

where Y is the yield, $\xi_{0}, \xi_{1}, \xi_{2}$ and so on are orthogonal polynomials of fertilizer application rates and $\mathrm{P}_{0}, \mathrm{P}_{1}, \mathrm{P}_{2}$ and so on. are site parameters and $\varepsilon$ as defined earlier. The regression of the form given above were fitted to the data of each site and coefficients for each site were then used as dependent variables to solve simultaneous regression of the form

$$
\begin{equation*}
p_{k i}=q_{k i}+r_{k i}+T_{i}^{1 / 2}+s_{k i} T_{i}+\ldots+\varepsilon^{\prime} . ; k=0,1,2, \ldots,(r-1) ; i=1,2, \ldots ., n . \tag{2.9}
\end{equation*}
$$

where, $\mathrm{T}_{\mathrm{i}}$ is the soil test measurements of the $\mathrm{i}^{\text {th }}$ site and k corresponds to the order of the polynomial in (2.8). The coefficients $\mathrm{q}_{\mathrm{ki}}, \mathrm{r}_{\mathrm{ki}}$ and $\mathrm{s}_{\mathrm{ki}}$ may be regarded as the regional parameters that provide a generalization of (2.8) by a function relating yield to fertilizer rate and soil test values. With appropriate substitution from (2.9) for the coefficients of $\mathrm{p}_{\mathrm{ki}}$ in (2.8) and the expansion of the orthogonal polynomials, a generalized function may be obtained in the form of polynomials of soil test $\mathrm{T}_{\mathrm{i}}$ and fertilizer rate $\mathrm{X}_{\mathrm{i}}$, in the square root scale, namely,

$$
\begin{align*}
\mathrm{Y}_{\mathrm{ij}}= & \left(\alpha_{0}+\alpha_{1} \mathrm{~T}_{\mathrm{i}}^{1 / 2}+\alpha_{2} \mathrm{~T}_{\mathrm{i}}\right)+\left(\beta_{0}+\beta_{1} \mathrm{~T}_{\mathrm{i}}^{1 / 2}+\beta_{2} \mathrm{~T}_{\mathrm{i}}\right) \mathrm{X}_{\mathrm{ij}}^{1 / 2}+\left(\gamma_{0}+\gamma_{1} \mathrm{~T}_{\mathrm{i}}^{1 / 2}+\gamma_{2} \mathrm{~T}_{\mathrm{i}}\right) \mathrm{X}_{\mathrm{ij}}+ \\
& +\left(\delta_{0}+\delta_{1} \mathrm{~T}_{\mathrm{i}}^{1 / 2}+\delta_{2} \mathrm{~T}_{\mathrm{i}}\right) \mathrm{X}_{\mathrm{ij}}^{3 / 2}+\ldots+\varepsilon \tag{2.10}
\end{align*}
$$

Alternatively, an average regional yield function

$$
\begin{equation*}
\mathrm{Y}_{\mathrm{i}}=\mathrm{a}+\mathrm{b} \mathrm{X}_{\mathrm{i}}^{1 / 2}+\mathrm{c} \mathrm{X}_{\mathrm{i}}+\mathrm{dX} \mathrm{X}_{\mathrm{i}}^{3 / 2}+\ldots+\varepsilon \tag{2.11}
\end{equation*}
$$

may be obtained without soil test regression, by averaging the coefficients of (2.8) over sites and again by expanding and collecting terms. In both cases the coefficients may be regarded as regional parameters of generalized yield function.

Alternative to the derivation of (2.10)or (2.11) from(2.8) and (2.9), these equations may be estimated directly by a least square fit of regression to the yield, fertilizer and soil test data. It can be shown that the coefficients obtained by this direct method are identical with those derived from equations (2.8) and (2.9) for the same data. Colwell found square root scale to be somewhat better fit to the data as compared to the corresponding quadratic expression in natural scale. Yield response, profit and fertilizer requirements can be calculated by appropriate substitution in equation (2.10) and (2.11). Mead and Pike (1975) have given an exhaustive review of various response surface models.

Colwell (1978) brought out a comprehensive report based on his studies on soil test - crop response, titled "Computation for studies of soil fertility and fertilizer requirement". The work on soil test - crop response studies had been taken up elsewhere also, to name a few, the government soil testing agencies of Netherlands and U.S.A. in the last forty years conducted thousands of field experiments with different crops and on different types of soils under various climatic conditions.
With regard to choosing a model, Colwell (1978) noted that the model can be chosen for their:
(a) Computational convenience
(b) Statistical estimation of functions from data and
(c) The calculation of optimal rates.

Keeping this in view, the polynomial models are popular because:

1. They are easily fitted to data using standard multiple regression procedure
2. They can be made flexible enough to describe most smooth trends and rigid enough to smooth out aberrations or "errors" in data by appropriate choice of scale and degree
3. They are implicit in many standard methods of statistical analysis of variance in the form of orthogonal polynomial trends and
4. They can easily accommodate interaction effects.

### 2.2 The Indian scenario

Consequent upon the introduction of high yielding varieties, the importance of fertilizer application for higher crop production was very well recognized by the farmers. With the fast expanding soil testing advisory service in India, the Indian Council of Agricultural Research felt the need to generate information on soil test crop response calibration and fertilizer recommendation based on soil test values. In the first phase, work on soil test crop response correlation in the country was carried out at the Indian Agricultural Research Institute, New Delhi under field and pot culture conditions using limited number of soils collected from less than 20 locations in the country using the then existing tall varieties of wheat and paddy in the early sixties.

In order to provide a refinement in the scientific basis in fertilizer use suited for the modern agricultural technology, consequent upon Green Revolution, the second phase of soil test-crop response work in the country was initiated under All India Co-ordinated Research Project on Soil Test-Crop Response Correlation by the Indian Council of Agricultural Research from 1967 onwards initially at eight centres. In 1970-71 five more centres were sanctioned. At present there are seventeen centres across the country.

### 2.3 Methodology as adopted by STCR project

Main objective of STCR project is to develop a relationship between soil test and crop response to fertilizer, in order to provide a calibration for fertilizer recommendation based on soil testing. Since different levels of uncontrollable variables (e.g. soil fertility) cannot be expected to occur at one place, different sites have to be selected to represent different levels of soil fertility. In this
present approach all the needed variation in soil fertility level is obtained not by selecting soils at different locations but deliberately creating it in one and the same field experiment in order to ensure homogeneity in the soil population studied, management practices adopted and climatic conditions prevailing. This is achieved by selecting a large area for the experiment in which there will be some variation in soil fertility level.
The chosen field is divided into four-strips lengthwise. While the first strip receives no fertilizer, second, third and fourth strips half, one and two times the standard dose ( X ) of $\mathrm{N}, \mathrm{P}$ and K respectively. The standard dose ( X ) is: $\mathrm{N}_{1}=150 \mathrm{Kg} . / \mathrm{ha}, \mathrm{P}_{1}=$ Phosphorus equivalent to the critical point in the P fixation studies of that field and $\mathrm{K}_{1}=$ enough to give $150 \mathrm{Kg} / \mathrm{ha}$. of exchangeable K .
Then a preparatory crop (or exhaust crop) has to be grown so that the fertilizers undergo reactions with the soil, plant and microbiological agencies. After the harvest of the preliminary crop, the field is ready for laying out the experiment with test crop for soil test- crop response correlation studies. Next the main experiment is conducted by selecting 21 treatments(a sub-set of treatment combinations from a $5 \times 4 \times 3$ factorial experiment design). For this each one of the strips is subdivided into subplots of which 6 are control plots and 21 receives various combinations of the levels of Nitrogen( N ), Phosphorus( P ) and Potassium(K), in a fractional factorial design. The soil samples from all these plots under the experiment are to be collected from different soil layers. The package of cultural practices recommended for the test crop is followed for the experimental crop. The yield and uptake of the nutrients on harvest are recorded. After the harvest of the crop, soil values are measured. The resulting data is then subjected to multiple regression, taking the yield as dependent variable and the linear and quadratic terms of $\mathrm{N}, \mathrm{P}$ and K and the interaction of $\mathrm{N}, \mathrm{P}$ and K with the available soil Nitrogen, Phosphorus and Potash respectively, as independent variables.

The general soil test- crop response model for yield can be given in terms of soil and fertilizer variables as:

$$
\begin{align*}
\mathrm{Y}=\mathrm{a} & +\mathrm{b}_{1} \mathrm{SN}+\mathrm{b}_{2} \mathrm{SP}+\mathrm{b}_{3} \mathrm{SK}+\mathrm{b}_{4} \mathrm{FN}+\mathrm{b}_{5} \mathrm{FN}^{2}+\mathrm{b}_{6} \mathrm{FP}+\mathrm{b}_{7} \mathrm{FP}^{2}+\mathrm{b}_{8} \mathrm{FK}+\mathrm{b}_{9} \mathrm{FK}^{2}+ \\
& +\mathrm{b}_{10}(\mathrm{FN} \times \mathrm{SN})+\mathrm{b}_{11}(\mathrm{FP} \times \mathrm{SP})+\mathrm{b}_{12}(\mathrm{FK} \times \mathrm{SK})+\varepsilon \tag{2.12}
\end{align*}
$$

where, SN, SP and SK are soil available nutrients and FN, FP and FK are added fertilizer nutrients and $\varepsilon$ is the error term which is assumed to be independently and identically distributed normally with zero mean and constant variance $\sigma^{2}$.
For soil test calibration, the multiple regression equation that has a high predictability $\left(\mathrm{R}^{2}>0.67\right)$ is used for making both yield prediction and optimization of chemical fertilizer requirements (Annual report, AICRP on STCR, 1993-98,pp-9). This equation is differentiated with respect to the nutrient, which behaved with the law of diminishing returns. The derivative will give the desired optimum fertilizer dose for varying soil test values of a nutrient for maximum yield. Inclusion of economic parameters will enable calculation of soil test based fertilizer dose for maximum profit and any desired rate of return on the investment made on fertilizers. The method of multiple regression for obtaining the optimal values of the nutrients is not always successful as the coefficients of linear, quadratic and interaction effects should have positive, negative and negative signs respectively for each of $N, P$ and $K$ which is not so in general. More over the $R^{2}$ value is also not so high. So to derive the fertilizer prescriptions, the method given by Truog (1960) was adopted, which although not statistically sound but is a mathematical derivation of certain indices. The basic data of the indices were generated by calculating the Nutrient requirement, Soil use efficiency and Fertilizer use efficiencies obtained from the nutrient uptake values of N, P and K. Then these values were fed into separate formula for obtaining separate equations for $\mathrm{N}, \mathrm{P}$ and K respectively. Based on soil test values of a particular a site, the corresponding doses of $\mathrm{N}, \mathrm{P}$ and K are calculated from these equations. Then follow up trials is
conducted with these doses. Although the results of the follow up trials show good results but the coefficients of the parameters of the equations for generating the fertilizer doses vary widely from year to year. Different centres conduct experiments by choosing the number of treatments from the set defined earlier and could take any of the treatment combinations of their choice. Over the years, numbers of experiments were conducted at various centers of the AICRP on Soil Test Crop Response Project by the application of various designs with different treatment combinations. We now discuss the Targeted yield approach in the following section.

### 2.4 Targeted Yield Equations or Fertilizer Adjustment Equations

## Targeted yield concept

Among the various methods of fertilizer recommendation, the one based on yield targeting is unique in the sense that this method not only indicates soil test based fertilizer dose but also the level of yield the farmer can hope to achieve if recommended agronomic practices are followed in raising the crop. The essential basic data required for formulating fertilizer recommendation for targeted yield are :
(i) nutrient requirement in $\mathrm{kg} / \mathrm{q}$ of produce, grain or other economic produce
(ii) the percent contribution from the soil available nutrients and
(iii) the percent contribution from the applied fertilizer nutrients( Ramamoorthy et al. 1967).

The above mentioned three parameters are calculated as follows:
(i) Nutrient Requirement of Nitrogen, Phosphorus and Potassium for grain Production (NR)

> total uptake of nutrient (kg)

Kg of nutrient/ q of grain $=\frac{\text { grain yield (q) }}{}$

## Percent contribution of nutrient from soil

$$
\text { Percent contribution from soil }(\mathrm{CS})=\frac{\text { total uptake in control plots }\left(\mathrm{kg} \mathrm{ha}^{-1}\right) \times 100}{\text { Soil test values of nutrient in control plots }\left(\mathrm{kg} \mathrm{ha}^{-1}\right)}
$$

## Percent contribution of nutrient from fertilizer

Contribution from fertilizer (CF) = (total uptake of nutrients - (soil test values of fertilizer in treated plots) nutrients in fertilizer treated plots $\times$ CS)
Percent contribution from $=\frac{\mathrm{CF}}{\text { fertilizer dose }\left(\mathrm{kg} \mathrm{ha}^{-1}\right)} \times 100$
Fertilizer

## Calculation of fertilizer dose

The above basic data are transformed into workable adjustment equation as follows:

$$
\begin{aligned}
\text { Fertilizer dose } & =\frac{\begin{array}{l}
\text { Nutrient requirement } \\
\text { in } \mathrm{kg} / \mathrm{q} \text { of grain }
\end{array}}{\% \mathrm{CF}} \times 100 \times \mathrm{T}-\frac{\% \mathrm{CS}}{\% \mathrm{CF}} \times \text { Soil test value } \\
& =\mathrm{a} \text { constant } \times \operatorname{yield} \operatorname{target}\left(\mathrm{q} \mathrm{ha}^{-1}\right)-\mathrm{b} \text { constant } \times \text { soil test value }\left(\mathrm{kg} / \mathrm{ha}^{-1}\right)
\end{aligned}
$$

where T is the targeted yield

Targeted yield concept strikes a balance between 'fertilizing the crop' and 'fertilizing the soil'. The procedure provides a scientific basis for balanced fertilization and balance between applied nutrients and soil available nutrients. In the targeted yield approach, it is assumed that there is a linear relationship between grain yield and nutrient uptake by the crop, as for obtaining a particular yield, a definite amount of nutrients are taken up by the plants. Once this requirement is known for a given yield level, the fertilizer needs can be estimated taking into consideration the contribution from soil available nutrients.
The basic data comprising of NR (Nutrient Requirement), CF(Contribution of fertilizer) and CS(Contribution of soil) etc. have been derived for Maruteru(1994), Rabi Rice and is given in the appendix-I The subsequent fertilizer adjustment equations are also given separately for each gradient and over all the gradients.

### 2.5 Modified Colwell approach

Lahiri et al (1998) applied a modification to the Colwell's approach (discussed under section 2.1) in a study conducted at IASRI, New Delhi. In this approach, step wise multiple regression (backward elimination) method was applied in two stages. Let a district be divided into ' $v$ ' zones, ' $b$ ' blocks in each zone and ' $m$ ' villages in each block. Thus we have ( $\mathrm{v} \times \mathrm{b} \times \mathrm{m}$ ) sites or say ' $n$ ' sites for each district. At each site an experiment has been conducted using randomised block design, with the same set of treatments. Also, at each of these sites, s soil test measurements have been carried out. Then our problem is to relate these s soil tests to the yield data obtained by conducting the experiment at each site and testing the statistical significance of their relationship. The yield data from each of the site may be represented by a polynomial function of the fertilizer rate.

$$
\begin{align*}
Y_{i j}= & b_{0 j} \\
& +b_{1 j} X_{i 1}+b_{2 j} X_{i 2}+b_{3 j} X_{i 3}+b_{4 j} X_{i 1}{ }^{2}+b_{5 j} X_{i 2}{ }^{2}+b_{6 j} X_{i 3}{ }^{2}+  \tag{2.13}\\
& +b_{7 j} X_{i 1} X_{i 2}+b_{8 j} X_{i 1} X_{i 3}+b_{9 j} X_{i 2} X_{i 3}+\varepsilon_{i j}
\end{align*}
$$

Where ' i ' denotes the fertilizer treatment ( $\mathrm{i}=1,2, \ldots, \mathrm{p}$ ) and ' j ' denotes the site ( $\mathrm{j}=1,2, \ldots, \mathrm{n}$ ), b's are regression co-efficients of linear, quadratic and interaction effects of fertilizer nutrients $\mathrm{X}_{\mathrm{i} 1}, \mathrm{X}_{\mathrm{i} 2}$ and $\mathrm{X}_{\mathrm{i} 3}$ respectively and $\varepsilon_{\mathrm{ij}}$ 's are randomly distributed with zero mean and variance $\sigma^{2}$. The whole set up of ' $n$ ' experiments can be written as simultaneous set of regression

$$
\begin{equation*}
\mathrm{Y}=\mathrm{X} \beta+\varepsilon \tag{2.14}
\end{equation*}
$$

where Y is a matrix of order ( $\mathrm{p} \times \mathrm{n}$ ) (row corresponds to fertilizer treatments and columns to sites), X is a ( $\mathrm{p} \times \mathrm{r}$ ) matrix of polynomial terms of the fertilizer treatments and $\beta$ is a matrix of regression co-efficients which may be regarded as site parameters, representing linear and quadratic trends of yield response to fertilizers. $\beta$ is estimated by the usual least square procedure.

$$
\begin{equation*}
\hat{\beta}=\left(X^{\prime} X\right)^{-1} \mathrm{X}^{\prime} \mathrm{Y} \tag{2.15}
\end{equation*}
$$

The site parameters of matrix $\hat{\beta}$ can as such be treated as function of the ' $s$ ' site measurements (soil test values), the relationship being represented also by the simultaneous regression

$$
\begin{equation*}
\beta^{\prime}=T^{\prime} D \tag{2.16}
\end{equation*}
$$

where $\mathbf{T}^{\prime}$ is the $\mathrm{nx}(\mathrm{s}+1)$ matrix of the soil test variables for the n sites.

D is the matrix of regression co-efficients estimated by

$$
\begin{equation*}
\mathrm{D}=\left(\mathrm{T}^{\prime} \mathrm{T}\right)^{-1} \mathrm{~TB}^{\prime} \tag{2.18}
\end{equation*}
$$

From the relationships of (2.14) and (2.16), yield may be expressed as a function of fertilizer treatments and soil tests as

$$
\begin{equation*}
\mathrm{Y}=\mathrm{X}^{\prime} \mathrm{D}^{\prime} \mathrm{T} \tag{2.19}
\end{equation*}
$$

The equation (2.19) may be expanded, rearranged and written in the form as follows:$Y_{j}=\sum_{m=0}^{s} a_{m} t_{m}+\sum_{m=0}^{s} b_{m} t_{m} X_{j 1}+\sum_{m=0}^{s} c_{m} t_{m} X_{j 2}+.-----++\sum_{m=0}^{s} \mathrm{k}_{\mathrm{m}} \mathrm{t}_{\mathrm{m}} \mathrm{X}_{\mathrm{j} 2} \mathrm{X}_{\mathrm{j} 3}$
where $Y_{j}$ is yield estimated for a particular site with the soil test values $t_{1}, t_{2},--t_{s}$ and $\mathrm{X}_{\mathrm{j}}$ 's are the fertilizer polynomial terms.

The above equation (2.20) was worked out taking the linear and quadratic terms of applied fertilizer and that of soil test values. The regression analysis was carried out by the method of stepwise multiple regression (backward elimination method). This method is only possible if the number of sites is more, so as to give greater error degrees of freedom for the analysis.

## Chapter -III

## ANALYTICAL TECHNIQUES DEVELOPED

### 3.0 Introduction

We have discussed earlier that in the AICRP on STCR, the main objective is to establish a relationship between Soil Test Values, the added fertilizer doses and the yield of the crop. This relationship is then used for obtaining balanced fertilizer doses for given soil test values. To achieve this, one has to take the help of Response Surface methodology. In order to understand the mechanism of the system, we need to do certain preliminary analysis. Therefore, in this chapter, we take an experiment, which was conducted earlier in STCR project and subject it to various analyses using established statistical tools. Also we use here various regression diagnostics to study the presence of outliers

A method, which was developed under this project, to get site-specific optimal values of fertilizer nutrients, if the soil test values of that site are known, has also been discussed.

As we know, that in order to avoid multi-location trials, which involves cost factor, four strips are laid out in STCR experiments. It is believed that by conducting a test experiment by growing an exhaust crop, the fertility gradient is established in the 4 strips named as $\mathrm{OX}, 0.5 \mathrm{X}, \mathrm{X}$ and 2 X .

### 3.1 An example

We take an example by analyzing the data of experiment, conducted at Maruteru, Hyderabad centre for Rice crop in the year 1994 in Rabi season. The fertilizer doses are 0, 50, 100, 150 $\mathrm{kg} / \mathrm{ha}$ of Nitrogen; 0, 40, $80 \mathrm{~kg} / \mathrm{ha}$ of Phosphorus and $0,40,80 \mathrm{~kg} / \mathrm{ha}$ of Potassium. There were in all 30 treatments in each strip consisting of 27 fertilizer treatment combination and 3 controls. In order to see the changes in soil fertility over the gradients, analysis of variance was performed separately by taking the Soil Nitrogen (SN), Soil Phosphorus (SP) and Soil Potash (SK) as dependent variable over the treatment and Gradients (Replication). The results are as follows:

Table 3.1: Analysis of variance of data for the Maruteru centre

> Year: 1994 Season: Rabi Crop: Rice
> Total Number of treatments: 30 in each strip ( 27 fertilizer combinations + 3

Controls)
Dependent Variable: SN (Soil Nitrogen)

| Source | DF | Sum of <br> Squares | Mean <br> Squares | F Value | $\operatorname{Pr}>$ F |
| :--- | :---: | :---: | :---: | :--- | :--- |
| Model | 30 | 106298.86 | 3543.29 | 7.71 | $<0.0001$ |
| Error | 89 | 40879.10 | 459.32 |  |  |
| Corrected <br> Total | 119 | 147177.97 |  |  |  |


| R-Square | Coeff Var | Root MSE | SN MEAN |
| :--- | :--- | :--- | :--- |
| 0.7222 | 6.40 | 21.43 | 334.82 |


| Source | DF | Sum of <br> Squares | Mean <br> Squares | F Value | $\operatorname{Pr}>$ F |
| :--- | :---: | ---: | ---: | :--- | :---: |
| Gradient | 3 | 1189.90 | 396.63 | 0.86 | 0.4632 |
| Treatment | 27 | 105108.97 | 3892.92 | 8.48 | $<0.0001$ |
| Error | 89 | 40879.10 | 459.32 |  |  |
| Corrected <br> Total | 119 | 147177.97 |  |  |  |

Dependent Variable: SP (Soil Phosphorus)

| Source | DF | Sum of <br> Squares | Mean <br> Squares | F Value | $\operatorname{Pr}>$ F |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Model | 30 | 44138.71 | 1471.29 | 17.86 | $<0.0001$ |
| Error | 89 | 7333.23 | 82.40 |  |  |
| Corrected <br> Total | 119 | 51471.94 |  |  |  |


| R-Square | Coeff. Var | Root MSE | SP MEAN |
| :--- | :--- | :--- | :--- |
| 0.8575 | 16.72 | 9.08 | 54.30 |


| Source | DF | Sum of <br> Squares | Mean <br> Squares | F Value | $\operatorname{Pr}>$ F |
| :--- | ---: | :--- | ---: | ---: | :--- |
| Gradient | 3 | 32810.89 | 10936.96 | 132.74 | $<0.0001$ |
| Treatment | 27 | 11327.81 | 419.55 | 5.09 | $<0.0001$ |
| Error | 89 | 7333.23 | 82.40 |  |  |
| Corrected <br> Total | 119 | 147177.97 |  |  |  |

## Dependent Variable: SK (Soil Potassium)

| Source | DF | Sum of <br> Squares | Mean <br> Squares | F Value | $\operatorname{Pr}>$ F |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Model | 30 | 189337.20 | 6311.24 | 5.94 | $<0.0001$ |
| Error | 89 | 94490.67 | 1061.69 |  |  |
| Corrected <br> Total | 119 | 283827.87 |  |  |  |


| R-Square | Coeff Var | Root MSE | SP MEAN |
| :--- | :--- | :--- | :--- |
| 0.6671 | 9.41 | 32.58 | 346.37 |


| Source | DF | Sum of <br> Squares | Mean <br> Squares | F Value | $\operatorname{Pr}>$ F |
| :--- | :---: | ---: | :---: | :---: | :--- |
| Gradient | 3 | 27988.33 | 9329.44 | 8.79 | $<0.0001$ |
| Treatment | 27 | 161348.87 | 5975.88 | 5.63 | $<0.0001$ |
| Error | 89 | 94490.67 | 1061.69 |  |  |
| Corrected <br> Total | 119 | 147177.97 |  |  |  |

The above analysis shows that the fertility gradient was indeed created by the experiment in respect of Soil Phosphorus (SP) and Soil Potassium (SK) but not in respect of Soil Nitrogen (SN).
Now to get the optimal doses of fertilizer, it is necessary that we form a relationship between Yield as dependent variable and Soil Nutrients of Nitrogen (SN), Phosphorus (SP) and Potassium (SK) along with added fertilizer nutrients of Nitrogen (FN), Phosphorus (FP) and Potassium (FK) as independent variables. To achieve this we need to perform Multiple Regression analysis. For this we take a second degree model with Yield as dependent variable and linear, quadratic effects of Fertilizer Nitrogen (FN), Fertilizer Phosphorus (FP) and Fertilizer Potassium (FK), linear effects of soil Nitrogen (SN), Soil Phosphorus (SP), Soil Potassium (SK) and their interactions with fertilizer nutrients(FN,FP and FK) as independent variables. At present in the project of AICRP on STCR, the second degree model used for this purpose is as follows:

## Model-I (12 variable model (STCR model))

$\mathrm{Y}=\mathrm{B}_{0}+\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+\mathrm{B}_{7} \mathrm{SN}+\mathrm{B}_{8} \mathrm{SP}+\mathrm{B}_{9} \mathrm{SK}++\mathrm{B}_{10}$ $\mathrm{FN} \times \mathrm{SN}+\mathrm{B}_{11} \mathrm{FP} \times \mathrm{SP}+\mathrm{B}_{12} \mathrm{FK} \times \mathrm{SK}+\varepsilon$
where, FN, FP etc have been defined earlier and $\varepsilon$ is the random error which is assumed to be distributed as $\sim \mathrm{N}\left(0, \sigma^{2}\right)$

Another model tried earlier by AICRP on STCR is as follows:
Model-IV (18 variable model)
$\mathrm{Y}=\mathrm{B}_{0}+\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+\mathrm{B}_{7} \mathrm{SN}+\mathrm{B}_{8} \mathrm{SP}+\mathrm{B}_{9} \mathrm{SK}++\mathrm{B}_{10}$ $\mathrm{SN}^{2}+\mathrm{B}_{11} \mathrm{SP}^{2}+\mathrm{B}_{12} \mathrm{SK}^{2}+\mathrm{B}_{13} \mathrm{FN} \times \mathrm{SN}+\mathrm{B}_{14} \mathrm{FP} \times \mathrm{SP}+\mathrm{B}_{15} \mathrm{FK} \times \mathrm{SK}+\mathrm{B}_{16} \mathrm{FN} \times \mathrm{FP}+\mathrm{B}_{17}$ $\mathrm{FN} \times \mathrm{FK}++\mathrm{B}_{18} \mathrm{FP} \times \mathrm{FK}+\varepsilon$
where, FN, FP etc have been defined earlier and $\varepsilon$ is the random error which is assumed to be distributed as $\sim N\left(0, \sigma^{2}\right)$

The interactions like ( $\mathrm{FN} \times \mathrm{SN}$ ) are reasonable but within soil interactions like ( $\mathrm{SN} \times \mathrm{SP} \mathrm{)} \mathrm{and}$ quadratic effects like $\mathrm{SN}^{2}, \mathrm{SP}^{2}$ etc. are of less significance. Of course we have to take interactions of the type ( $\mathrm{FN} \times \mathrm{FP}$ ). These give 15 parameters to be estimated which are as follows:

## Model-III(b) (15 variable model)

$$
\begin{aligned}
\mathrm{Y}= & \mathrm{B}_{0}+\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+\mathrm{B}_{7} \mathrm{SN}+\mathrm{B}_{8} \mathrm{SP}+\mathrm{B}_{9} \mathrm{SK}++\mathrm{B}_{10} \\
& \mathrm{FN} \times \mathrm{SN}+\mathrm{B}_{11} \mathrm{FP} \times \mathrm{SP}+\mathrm{B}_{12} \mathrm{FK} \times \mathrm{SK}+\mathrm{B}_{13} \mathrm{FN} \times \mathrm{FP}+\mathrm{B}_{14} \mathrm{FN} \times F K+\mathrm{B}_{15} \mathrm{FP} \times \mathrm{FK}+\varepsilon
\end{aligned}
$$

In these models we can also take strips (replication) as a parameter. Inclusion of replication increases the R-Square value. Moreover the significance of the effect of the strip (replication) component would show whether the fertility gradient has been created or not. Since we have 30 treatment combinations, number of degrees of freedom for error would be sufficient.
For all the models stated above, we perform the Step-down (backward elimination) multiple regression for the $15 / 16$ variable models. We first enter all the variables and then those variables whose effects are not found significant at a desired level of significance are automatically dropped from the model. This analysis was carried out with the help of SAS package PROC REG.

Table 3.2: Multiple regression method of analysis
Centre: Maruteru, Year: 1994, Crop: Rice, Season: Rabi Model-III (includes FN $\times$ FP, $\mathbf{F N} \times$ FK and $\mathbf{F P} \times \mathbf{F K}$ interactions)

All Variables entered R-Square $=0.9089 \quad$ Analysis of Variance

| Source | DF | Sum of Squares | Meah Square | F Va | lue | Pr | F |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | 15 | 147463475 | 9830898 | 69.1 | 19 | <.000 |  |
| Error | 104 | 14777851 | 142095 |  |  |  |  |
| Corrected <br> Total | 119 | 162241326 |  |  |  |  |  |

Table 3.3 Multiple Regression (All variables entered)

|  | Parameter <br> Vstimate | Standard <br> Error | Type II SS | F Value | Pr $>F$ |
| :--- | :---: | :---: | ---: | ---: | ---: |
|  |  |  |  |  |  |
| Intercept | $4190.10335^{*}$ | 1159.30610 | 1856227 | 13.06 | 0.0005 |
| fn | 13.59956 | 8.36951 | 375169 | 2.64 | 0.1072 |
| fp | 1.82340 | 5.65208 | 14788 | 0.10 | 0.7476 |
| fk | $16.23264^{*}$ | 9.74218 | 394497 | 2.78 | 0.0987 |
| fn2 | -0.15418 | 0.02452 | 5617495 | 39.53 | $<.0001$ |
| fp2 | 0.08056 | 0.04959 | 375094 | 2.64 | 0.1072 |
| fk2 | $-0.10242^{*}$ | 0.04939 | 610964 | 4.30 | 0.0406 |
| sn | -5.58622 | 3.49895 | 362191 | 2.55 | 0.1134 |
| sp | 1.75705 | 3.22322 | 42225 | 0.30 | 0.5868 |
| sk | -1.81762 | 1.56006 | 192887 | 1.36 | 0.2466 |
| fnsn | $0.09570^{*}$ | 0.03000 | 1446279 | 10.18 | 0.0019 |
| fpsp | -0.06507 | 0.06029 | 165511 | 1.16 | 0.2830 |
| fksk | -0.00257 | 0.03186 | 927.14434 | 0.01 | 0.9358 |
| fnfp | -0.03635 | 0.02716 | 254497 | 1.79 | 0.1837 |
| fnfk | 0.00314 | 0.02906 | 1655.12781 | 0.01 | 0.9143 |
| fpfk | 0.00084992 | 0.03990 | 64.46703 | 0.00 | 0.9830 |

Table 3.4: Remaining Variables after backward elimination process (Model-III)
Analysis of Variance

| Source | DF | Sum of <br> Squares | Mean <br> Square | F Value | Pr > F |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Model | 8 | 146915470 | 18364434 | 133.01 | $<.0001$ |
| Error | 111 | 15325856 | 138071 |  |  |
| Corrected <br> Total | 119 | 162241326 |  |  |  |

[^0]Table 3.5 : Multiple Regression (Remaining Variables) after backward elimination(Model-III)

| Variable | Parameter <br> Estimate | Standard <br> Error | Type II SS | F Value | Pr >F |
| :--- | ---: | :--- | ---: | ---: | ---: |
| Intercept | 2755.60889 | 289.16690 | 12538331 | 90.81 | $<.0001$ |
| fn | 24.39779 | 4.51747 | 4027289 | 29.17 | $<.0001$ |
| fk | 16.08044 | 3.91996 | 2323452 | 16.83 | $<.0001$ |
| fn2 | -0.13557 | 0.01820 | 7658020 | 55.46 | $<.0001$ |
| fp2 | 0.06341 | 0.02793 | 711536 | 5.15 | 0.0251 |
| fk2 | -0.10505 | 0.04755 | 673842 | 4.88 | 0.0292 |
| Sk | -2.31739 | 0.94738 | 826131 | 5.98 | 0.0160 |
| fnsn | 0.05236 | 0.01200 | 2629468 | 19.04 | $<.0001$ |
| fnfp | -0.04118 | 0.02198 | 484565 | 3.51 | 0.0636 |

Table 3.6: ANOVA when replication is added as a variable in Model-III (16 variables)
All Variables Entered

> Analysis of Variance

| Source | DF | Sum of <br> Squares | Mean <br> Square | F Value | Pr >F |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Model | 16 | 148037298 | 9252331 <br> 137903 | 67.09 | $<.0001$ |
| Error | 103 | 14204028 |  |  |  |
| Corrected <br> Total | 119 | 162241326 |  |  |  |

R -Square $=0.9125$

Table 3.7: Multiple Regression Model-III + replication
(All variables entered)

|  | Parameter <br> Estimate | Standard <br> Error | Type II SS | F Value | Pr $>$ F |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Variable |  |  |  |  |  |
| Intercept | 4229.20123 | 1142.24019 | 1890498 | 13.71 | 0.0003 |
| rep | -120.09994 | 58.87632 | 573824 | 4.16 | 0.0439 |
| fn | 12.53000 | 8.26180 | 317195 | 2.30 | 0.1324 |
| fp | 0.73375 | 5.59366 | 2372.89137 | 0.02 | 0.8959 |
| fk | 14.83111 | 9.62198 | 327637 | 2.38 | 0.1263 |
| fn2 | -0.14426 | 0.02464 | 4725520 | 34.27 | $<.0001$ |
| fp2 | 0.08409 | 0.04888 | 408157 | 2.96 | 0.0884 |
| fk2 | -0.10681 | 0.04871 | 663243 | 4.81 | 0.0306 |
| sn | -5.43516 | 3.44776 | 342709 | 2.49 | 0.1180 |
| sp | 7.84537 | 4.35786 | 446946 | 3.24 | 0.0747 |
| sk | -1.72956 | 1.53748 | 174512 | 1.27 | 0.2632 |
| fnsn | 0.09186 | 0.02961 | 1327078 | 9.62 | 0.0025 |
| fpsp | -0.07059 | 0.05946 | 194368 | 1.41 | 0.2379 |
| fksk | 0.00082862 | 0.03143 | 95.84092 | 0.00 | 0.9790 |
| fnfp | -0.03434 | 0.02677 | 226826 | 1.64 | 0.2025 |
| fnfk | 0.00570 | 0.02866 | 5460.15717 | 0.04 | 0.8427 |
| fpfk | 0.00427 | 0.03935 | 1623.82712 | 0.01 | 0.9138 |

Table 3.8: ANOVA of remaining variables after backward elimination process (Model-III + replication)

Analysis of Variance

| Source | DF | Sum of <br> Squares | Mean <br> Square | F Value | Pr >F |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Model <br> Error | 8 | 146970007 | 18371251 | 133.53 | $<.0001$ |
| Corrected <br> Total | 119 | 162241326 |  |  |  |

R-Square $=0.9059$

Table: 3.9 Multiple Regression(remaining variables) after backward elimination process (Model-III)

|  | Parameter <br> Estimate | Standard <br> Error | Type II SS | F Value | Pr $>$ F |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Variable |  |  |  |  |  |
|  |  | 125.78246 | 45382311 | 329.86 | $<.0001$ |
| Intercept | 2284.47601 | 12.008 |  |  |  |
| rep | -77.25825 | 30.53624 | 880668 | 6.40 | 0.0128 |
| fn | 23.94818 | 4.48568 | 3921403 | 28.50 | $<.0001$ |
| fk | 16.24373 | 3.91230 | 2371708 | 17.24 | $<.0001$ |
| fn2 | -0.13080 | 0.01816 | 7137216 | 51.88 | $<.0001$ |
| fp2 | 0.05829 | 0.02780 | 604904 | 4.40 | 0.0383 |
| fk2 | -0.11494 | 0.04726 | 813790 | 5.92 | 0.0166 |
| fnsn | 0.04970 | 0.01207 | 2334635 | 16.97 | $<.0001$ |
| fnfp | -0.05078 | 0.02163 | 758435 | 5.51 | 0.0206 |

It is observed that although the backward elimination process in both the cases (15 and 16 Variables) returns almost similar variables, one can note that by including replication as a variable in the 16 variable model, R -square value is increased. Moreover it is observed that in the later case, since replication effect is significant, it shows that the fertility gradient has been established.

The optimal values of Nitrogen, Phosphorus and Potassium could be derived from these multiple regression equations by differentiating separately with respect to each nutrient and then solving the resulting equations (obtained by substituting the respective soil test values of SN, SP and SK in the equation of the site). The process is cumbersome.

Going through all these pros and cons one would like to switch to Response Surface Methodology.

In the sequel we compare the derived optimal values of Nitrogen, Phosphorus and Potassium by the method of the Targeted yield equations (as followed by STCR project at present) and by the method of Response Surface for this experiment at Maruteru.

Targeted Yield Equation (over all the gradients(120 observations))

| Parameter | $\mathbf{N}$ | $\mathbf{P}_{\mathbf{2}} \mathbf{O}_{\mathbf{5}}$ | $\mathbf{K}_{\mathbf{2}} \mathbf{O}$ | Fertilizer Adjustment <br> Equations | Target | Soil-test <br> Values | Optimum <br> Fertilizer <br> doses |  |
| :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | $\mathbf{( q / h a )}$ | $\mathbf{( k g / h a )}$ | $\mathbf{( k g / h a )}$ |
| $\mathrm{NR}(\mathrm{kg} / \mathrm{q})$ | $: 2.0696$ | 1.1273 | 2.7009 | $\mathrm{FN}=3.79 * \mathrm{~T}-0.29 \mathrm{SN}$ | 57.23 | 350.0 | 119 |  |
| CS | $: 0.1728$ | 0.4100 | 0.1607 | $\mathrm{FP}=2.68 * \mathrm{~T}-2.13 \mathrm{SP}$ |  | 23.4 | 73 |  |
| CF | $: 0.4777$ | 0.4409 | 1.2073 | $\mathrm{FK}=2.02 * \mathrm{~T}-0.16 \mathrm{SK}$ |  | 336.0 | 72 |  |

The response surface methodology gives the following result:

Estimated Ridge of Maximum Response for Variable yield

| Coded <br> Radius | Estimated <br> Response | Standard <br> Error | Optimum <br> FN | Values for estimated response (kg/ha) <br> FP | FK |
| :--- | :---: | ---: | ---: | ---: | ---: | ---: |

The two results of optimum values of fertilizer doses derived by Targeted yield equations and Response Surface methodology are given above. From above it is observed that the two methods seem to be matching though differing somewhere. Further study is needed to understand the mechanism of the difference between the two methods.

Here in brief we discuss Response Surface Methodology and then present a method, which has been developed at IASRI, New Delhi. In this the optimal values of nutrients could be derived with respect to soil test values of the site in question.

### 3.2 Response surface methodology

## Fitting a Second Order Response Surface

Let us consider the fitting of a second order model in k variables of the form

$$
\begin{equation*}
\mathrm{Y}=\beta_{0}+\sum_{\mathrm{i}=1}^{\mathrm{k}} \beta_{\mathrm{i}} \mathrm{x}_{\mathrm{i}}+\sum_{\mathrm{i}=1}^{\mathrm{k}} \beta_{\mathrm{ii}} \mathrm{x}_{\mathrm{i}}+\sum_{\mathrm{i} k \mathrm{j}} \sum^{\mathrm{k}} \beta_{\mathrm{ij}} \mathrm{x}_{\mathrm{i}} \mathrm{x}_{\mathrm{j}}+\varepsilon \tag{3.1}
\end{equation*}
$$

The number of terms in the model (3.1) is $p^{\prime}=(k+1)(k+2) / 2$, in our case we have taken $k=3$ i.e the three fertilizer nutrients FN, FP and FK and so the number of terms is 10 and the model becomes

$$
\begin{aligned}
\mathrm{Y}= & \mathrm{B}_{0}+\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+\mathrm{B}_{7} \mathrm{FN} \times \mathrm{FP}+\mathrm{B}_{8} \mathrm{FN} \times \mathrm{FK}+ \\
& +\mathrm{B}_{9} \mathrm{FP} \times \mathrm{FK}+\varepsilon
\end{aligned}
$$

The fitted model takes the form

$$
\begin{align*}
\hat{\mathrm{Y}}= & \mathrm{b}_{0}+\mathrm{b}_{1} \mathrm{FN}+\mathrm{b}_{2} \mathrm{FP}+\mathrm{b}_{3} \mathrm{FK}+\mathrm{b}_{4} \mathrm{FN}^{2}+\mathrm{b}_{5} \mathrm{FP}^{2}+\mathrm{b}_{6} \mathrm{FK}^{2}+\mathrm{b}_{7} \mathrm{FN} \times \mathrm{FP}+\mathrm{b}_{8} \mathrm{FN} \times \mathrm{FK}+ \\
& +\mathrm{b}_{9} \mathrm{FP} \times \mathrm{FK} \tag{3.2}
\end{align*}
$$

After the fitted model is checked for adequacy of fit in the region defined by the coordinates of the design and is found to be adequate, the model is then used to locate the coordinates of the stationary point and to perform a canonical analysis of the response surface. If the stationary point is found to be inside the experimental region, then we describe the nature of the stationary point i.e. whether it is a maximum, a minimum, or a saddle point (minimax point, i.e. neither maximum nor minimum). If the stationary point is not inside the experimental region, then the search for maximum response is undertaken by Ridge analysis. In general, this method is used for finding the absolute maximum (minimum) of estimated response $\hat{Y}$ on concentric spheres of varying radii. For a detailed study the reader is referred to Khuri and Cornell (1987).

For the analysis by Response Surface methodology described above, the SAS package PROC RSREG has been used. Further in the above analysis, the soil variables SN, SP and SK has been taken as covariates to include them into the system.

### 3.3 Analytical technique developed

At present when the multiple regression equation does not provide the required optimal values of the fertilizer nutrients, the same are worked out through Fertilizer adjustment equations developed by STCR. The equations thus generated although provide good results at the follow up trials but are not statistically sound. Therefore, there is variation in the coefficients from year to year and so these cannot be pooled. In order to give a statistical backing to the whole process, a method has been worked out at IASRI to get the desired results by combining the method of fertilizer adjustment equations with that of response surface methodology.
The basic assumption in the targeted yield approach is that the plant nutrient uptake from the control plots and treated plots is same. Therefore it was felt that the doses of FN, FP and FK be worked out through Response Surface Methodology by exploring the response surface in the vicinity of stationery point. The stationery point is a point of a maximum, minimum or a saddle point (which neither maximum nor minimum). This method is applicable when the stationery point lies within the experimental region. If it is not within the experimental region, then also it is possible to find out the different combination of doses of FN, FP and FK with the help of canonical analysis of the response surface and ridge analysis.

## EXAMPLE 3.3

For the illustration of the method and the corresponding results, we have chosen the same example of the data of one of the centers of the STCR project, namely, Maruteru (Rabi-Rice), 1994.

Multiple regression was fitted to the data, which is as follows (15 variables as taken earlier):

$$
\begin{array}{rlrl}
\mathrm{y}= & 4190.1034-5.5862 \mathrm{SN}+1.7570511 \mathrm{SP}-1.817621 \mathrm{SK}+13.599559 F \mathrm{~N}^{*} & \\
& +1.8233963 \mathrm{FP}+16.232643 F \mathrm{FK} *-0.154184 \mathrm{FN}{ }^{2} * *+0.0805624 \mathrm{FP}^{2} * & \mathrm{R}^{2}=0.9089 \\
-0.102418 \mathrm{FK}^{2} *-0.036346 \mathrm{FNFP}+0.00314 F N F K+0.0008499 F P F K & \\
& +0.0957009 F N S N *-0.065072 \text { FPSP }-0.002574 F K S K &
\end{array}
$$

Where SN, SP, SK are soil available nutrients, FN, FP, FK are added fertilizers
By substituting the values of SN, SP, SK of a particular plot, corresponding to a particular treatment, we get a fitted response surface in FN, FP and FK with following results:

For given $\mathrm{SN}=\mathbf{3 5 0}$; $\mathbf{S P}=\mathbf{2 3 . 4}$; $\mathrm{SK}=336$

|  | Eigen <br> Value | Eigenvectors |  |  |
| :--- | :--- | :--- | :--- | :---: |
|  |  | FN | FP | FK |
| FN | 0.0819615 | -0.07672 | 0.0300211 | 0.9966006 |
| FP | -0.10237 | 0.9970513 | 0.0006604 | 0.0767347 |
| FK | -0.155631 | 0.0016455 | 0.999549 | -0.029983 |

The co-ordinates of the stationary point:

| FN | FP | FK |
| :--- | :--- | :--- |
| 145.26043 | 30.493334 | 77.376379 |

The predicted yield at the stationary point: $5664.5034 \mathrm{~kg} / \mathrm{ha}$
As one Eigen Value is positive and two Eigen Values are negative, therefore, the stationary point is a saddle point indicating that there is neither Maxima nor Minimum. Also a situation can arise for a saddle point when two Eigen Values are positive and one is negative. If all are positive then it is called a minima and if all are negative then it is a maxima.

### 3.4 Exploration of the Response Surface in the vicinity of Stationery Point

The estimated response increases upon moving away from the stationary point along the $W_{i}$ if corresponding $\lambda_{i}$ is positive and decreases upon moving away from stationary point along the $W_{i}$ if corresponding $\lambda_{i}$ is negative. If the stationary point is minimax (saddle point) point, then it is desirable to explore the response surface in the vicinity of stationary point and determine the combinations of inputs for a given response. To achieve this, the $W_{i}$ 's corresponding to negative $\lambda_{i}$ ' $s$ are set to zero. Now, the values of the $W_{i}$ 's corresponding positive $\lambda_{i}$ ' $s$ are generated. To be clearer, in this case one of the $\lambda_{i}$ ' $s$ denoted by $\lambda_{1}$ is positive. Then, a restricted canonical equation can be written as

$$
\begin{equation*}
Y_{\text {des }}=\hat{y}_{0}+\lambda_{1} W_{1}^{2} \tag{3.3}
\end{equation*}
$$

where $Y_{\text {des }}$ denotes the desired response. If $Y_{d e s}-\hat{y}_{0}$ is denoted by difference of the desired and predicted response, then

Difference $=\lambda_{1} W_{1}{ }^{2}$

$$
\Rightarrow \quad \frac{\mathrm{W}_{1}^{2}}{\mathrm{a}^{2}}=1
$$

where $a^{2}=$ Difference $/ \lambda_{1}$
This equation represents a straight line. $W_{1}$ should be so generated that it falls inside the interval $(-a, a)$. Once the $W_{1}$ is generated, $W_{i}$ ' $s$ are known, we would like to express $W_{i}$ in terms of $x_{i}$ ' $s$. This can be achieved by $\mathrm{x}=\mathrm{MW}+\mathrm{x}_{0}$, where $\mathrm{x}_{0}$ is the stationary point.
Let us assume that we get $\lambda_{1}, \lambda_{2}$ and $\lambda_{3}$ as $0.0819615,-0.10237$ and
-0.155631 . As $\lambda_{2}, \lambda_{3}$ are negative, therefore, take $\mathrm{w}_{2}=\mathrm{W}_{3}=0$. Let

$$
\left.\mathbf{M}=\left\{\begin{array}{ccc}
\{-0.07672 & 0.0300211 & 0.9966006, \\
& 0.9970513 & 0.0006604 \\
& 0.0767347, \\
& 0.0016455 & 0.999549
\end{array}\right)-0.029983\right\} ;
$$

denotes the matrix of eigenvectors. Let the estimated response at the stationary points be $5664.5034 \mathrm{~kg} / \mathrm{ha}$. Let the desired response be $\mathrm{Y}_{\text {des }}=6000 \mathrm{~kg} / \mathrm{ha}$. Therefore, let $\mathrm{w}_{1}$, obtained from the equation is sqrt (difference/0.0819615)=AX1, say. To obtain various different sets of many values of $w_{1}$, generate a random variable, $u$, which follows uniform distribution and multiply this value with $2 \mathrm{u}-1$ such that $\mathrm{w}_{1}$ lies within the interval, (-AX1, AX1). Now to get a combination of $\mathrm{x}_{\mathrm{i}}$ 's that produces the desired response, obtain $\mathrm{x}=\mathrm{M} * \mathrm{~W}+\mathrm{x}_{0}$ with the help of the following SAS code:
PROC IML;
$\mathrm{W}=\mathrm{J}(3,1,0)$;
Ydes=6000;
W2=0;
W3=0;
Dif=Ydes-5664.5034;
Ax1=Sqrt(dif/0.0819615);
$\mathrm{u}=$ uniform(0);
$\mathrm{W} 1=\mathrm{ax} 1^{*}\left(2^{*} \mathrm{u}-1\right)$; print w 1 ;
$\mathrm{w}[1]=,\mathrm{w} 1$;
$\mathrm{w}[2]=$,0 ;
$\mathrm{w}[3]=$,0 ;

| $\mathrm{m}=\{$ | $\{-0.07672$ | 0.03970513 |
| ---: | :--- | ---: |
|  | 0.0006604 | 0.9966006, |
|  | 0.0016455 | 0.999549 |

xest $=\{145.26043,30.493334,77.376379\} ;$
$\mathrm{x}=\mathrm{m} * \mathrm{w}+\mathrm{xest}$;
print x ;
run;
Results:

| Desired Yield | FN | FP | FK |
| :--- | :--- | :--- | :--- |
| $6000 \mathrm{~kg} / \mathrm{ha}$ | 144.79605 | 36.528386 | 77.386339 |
|  | 146.84785 | 39.8632775 | 77.342332 |
|  | 144.75153 | 37.106991 | 77.387294 |
|  | 141.9171 | 38.94317 | 77.448087 |
| $6100 \mathrm{~kg} / \mathrm{ha}$ | 144.91531 | 34.978478 | 77.383781 |
|  | 143.36787 | 55.089018 | 77.416971 |
|  | 146.3448 | 46.400841 | 77.353121 |

This computer programme has been created for working in SAS package for checking the methodology. The technique is quite computer intensive. The development of a step-by-step procedure and the corresponding preparation of user-friendly software package are very necessary and will be taken up in a subsequent project.

### 3.5 Regression analysis

Various Multiple Regression models were tried including the one used by the AICRP on STCR.
Model-I (9 variable model)

$$
\begin{align*}
\mathrm{Y}=\mathrm{B}_{0} & +\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+ \\
& +\mathrm{B}_{7} \mathrm{FN} \times \mathrm{FP}+\mathrm{B}_{8} \mathrm{FN} \times \mathrm{FK}+\mathrm{B}_{9} \mathrm{FP} \times F K+\varepsilon \tag{3.5}
\end{align*}
$$

## Model-II ( 12 variable model(STCR model))

$$
\begin{align*}
& \mathrm{Y}=\mathrm{B}_{0}+\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+\mathrm{B}_{7} \mathrm{SN}+\mathrm{B}_{8} \mathrm{SP}+\mathrm{B}_{9} \mathrm{SK}+ \\
& \quad+\mathrm{B}_{10} \mathrm{FN} \times \mathrm{SN}+\mathrm{B}_{11} \mathrm{FP} \times \mathrm{SP}+\mathrm{B}_{12} \mathrm{FK} \times \mathrm{SK}+\varepsilon \tag{3.6}
\end{align*}
$$

## Model-III(a) (15 variable model)

$$
\begin{align*}
\mathrm{Y}=\mathrm{B}_{0} & +\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+\mathrm{B}_{7} \mathrm{SN}+\mathrm{B}_{8} \mathrm{SP}+\mathrm{B}_{9} \mathrm{SK}+ \\
& +\mathrm{B}_{10} \mathrm{SN}^{2}+\mathrm{B}_{11} \mathrm{SP}^{2}+\mathrm{B}_{12} \mathrm{SK} K^{2}+\mathrm{B}_{13} \mathrm{FN} \times \mathrm{SN}+\mathrm{B}_{14} \mathrm{FP} \times \mathrm{SP}+\mathrm{B}_{15} \mathrm{FK} \times \mathrm{SK}+\varepsilon \tag{3.7a}
\end{align*}
$$

## Model-III(b) ( 15 variable model)

$$
\begin{align*}
\mathrm{Y} & =\mathrm{B}_{0}+\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+\mathrm{B}_{7} \mathrm{SN}+\mathrm{B}_{8} \mathrm{SP}+\mathrm{B}_{9} \mathrm{SK}+ \\
& +\mathrm{B}_{10} \mathrm{FN} \times \mathrm{SN}+\mathrm{B}_{11} \mathrm{FP} \times \mathrm{SP}+\mathrm{B}_{12} \mathrm{FK} \times \mathrm{SK}+\mathrm{B}_{13} \mathrm{FN} \times \mathrm{FP}+\mathrm{B}_{14} \mathrm{FN} \times \mathrm{FK}+\mathrm{B}_{15} \mathrm{FP} \times \mathrm{FK}+\varepsilon \tag{3.7b}
\end{align*}
$$

## Model-IV (18 variable model)

$$
\begin{align*}
& \mathrm{Y}=\mathrm{B}_{0}+\mathrm{B}_{1} \mathrm{FN}+\mathrm{B}_{2} \mathrm{FP}+\mathrm{B}_{3} \mathrm{FK}+\mathrm{B}_{4} \mathrm{FN}^{2}+\mathrm{B}_{5} \mathrm{FP}^{2}+\mathrm{B}_{6} \mathrm{FK}^{2}+\mathrm{B}_{7} \mathrm{SN}+\mathrm{B}_{8} \mathrm{SP}+\mathrm{B}_{9} \mathrm{SK}+ \\
& \quad+\mathrm{B}_{10} \mathrm{SN}+\mathrm{B}_{11} \mathrm{SP}^{2}+\mathrm{B}_{12} \mathrm{SK} \mathrm{~K}^{2}+\mathrm{B}_{13} \mathrm{FN} \times \mathrm{SN}+\mathrm{B}_{14} \mathrm{FP} \times \mathrm{SP}+\mathrm{B}_{15} \mathrm{FK} \times \mathrm{SK}+\mathrm{B}_{16} \mathrm{FN} \times \mathrm{FP}+ \\
& \quad+\mathrm{B}_{17} \mathrm{FN} \times \mathrm{FK}+\mathrm{B}_{18} \mathrm{FP} \times \mathrm{FK}+\varepsilon \tag{3.8}
\end{align*}
$$

Where, FN, FP, FK are added fertilizer nutrients of Nitrogen, Phosphorus and Potassium respectively. SN, SP, SK are soil available nutrients of Nitrogen, Phosphorus and Potassium respectively, collected before the conduct of the main experiment and $\varepsilon$ is the random error term which is distributed normally as $\mathrm{N} \sim\left(0, \sigma^{2}\right)$.

Besides these models, another set of $10,13,16$ and 19 models were tested by adding replication as one of the parameters to each of the above models.

The data of each experiment was subjected to multiple regression using backward elimination procedure with the help of PROC REG of the SAS package. The SAS code used is given in the appendix.

### 3.6 Regression diagnostics

Regression Diagnostics refers to the various methods that can be used effectively to flag observations that are dominating the regression. This also helps in detecting problems with either the model or data set. At present this is a very active field of research. Here we discuss few of them. For further study one can refer to Belsley, Kuh and Welsch(1980) and Cook and Weisberg(1982) which gives a fairly thorough coverage of the theory and methods of diagnostic techniques.

Regression model is fitted using least square technique for estimating parameters. The optimality properties of these estimates are described in an ideal setting, which is not often realized in practice. It has been observed that regressions based on different subsets of data produce very different results, raising questions of model stability. Frequently we do not have 'good' data in the sense that errors are non-normal or the variance is non-homogeneous. The data may contain outliers or extremes, which are not easily detectable but highly influential, as the least square estimation procedure tends to pull the estimated regression response towards outlying observations. The variable pool may not contain the right variables in the proper functional forms and we may have included variables with a high degree of multi-collinearity. Presence of multi-collinearity in data causes serious problems in estimation, prediction and interpretation. Moreover the estimated regression may be unrealistic in magnitude and sign. In the sequel we discuss here some of the techniques of regression diagnostics.

### 3.6.1 Residual analysis

Analysis of regression residuals, or some transformation of the residuals, is very useful for detecting inadequacies in the model or problems in the data. The true error in the regression model are assumed to be normally and independently distributed random variables with zero mean and common variance $\epsilon \sim \mathrm{N}\left(\mathbf{0}, \mathbf{I} \sigma^{2}\right)$. The observed residuals, however are not independent and do not have common variance, even when the $\boldsymbol{I} \sigma^{2}$ assumption is valid. Under the usual least squares assumptions,
$\mathrm{e}=\mathrm{Y}-\hat{\mathrm{Y}}=\mathrm{Y}-\mathrm{X} \hat{\beta}=\mathrm{Y}-\left(\mathrm{X}\left(\mathrm{X}^{\prime} \mathrm{X}\right)^{-1} \mathrm{X}^{\prime}\right) \mathrm{Y}=\mathrm{Y}-\mathrm{PY}=(\mathrm{I}-\mathrm{P}) \mathrm{Y}$ has a multivariate normal distribution with $\mathrm{E}(\mathrm{e})=0$ and $\operatorname{Var}(\mathrm{e})=(\mathrm{I}-\mathrm{P}) \sigma^{2}$. Where $\mathrm{P}=\left(\mathrm{X}\left(\mathrm{X}^{\prime} \mathrm{X}\right)^{-1} \mathrm{X}^{\prime}\right)$ is an n x n matrix determined entirely by the $\mathrm{X}^{\prime}$ s. This matrix plays a particularly important role in regression analysis. It is a symmetric matrix $\left(\mathrm{P}^{\prime}=\mathrm{P}\right)$ and also idempotent $(\mathrm{PP}=\mathrm{P})$ and is therefore a projection matrix. The diagonal elements of $\operatorname{Var}(\mathrm{e})$ are not equal, so the observed residuals do not have common variance; the off-diagonal elements are not zero, so they are not independent.

The heterogeneous variances in the observed residuals are easily corrected by standardizing each residual. The variances of the residuals are estimated by diagonal elements of (I-P)s ${ }^{2}$. Dividing each residual by its standard deviation gives a standardized residual, denoted with $r_{i}$,

$$
\begin{equation*}
r_{i}=\frac{e_{i}}{s \sqrt{\left(1-v_{i j}\right)}} \tag{3.9}
\end{equation*}
$$

Where $\mathrm{V}_{\mathrm{ii}}$ is the $\mathrm{i}^{\text {th }}$ diagonal element of P . All the standardized residuals (with $\sigma$ in place of S in the denominator) have unit variance.
Another form suggested by Belsley, Kuh and Welsch (1980) is to standardize each residual with an estimate of its standard deviation that is independent of the residual. The variance labeled $\mathrm{s}^{2}{ }_{(\mathrm{i})}$, where the subscript in parentheses indicates that the $\mathrm{i}^{\text {th }}$ observation has been omitted for the estimate of $\sigma^{2}$. This is Studentized residual, denoted by $\mathbf{r}_{\mathbf{i}}{ }^{*}$.

$$
\begin{equation*}
\mathrm{r}_{\mathrm{i}}^{*}=\frac{\mathrm{e}_{\mathrm{i}}}{\mathrm{~s}_{(\mathrm{i})} \sqrt{\left(1-\mathrm{v}_{\mathrm{ii}}\right)}} . \tag{3.10}
\end{equation*}
$$

Each Studentized residual is distributed as Student's t with ( $\mathrm{n}-\mathrm{p}^{\prime}-1$ ) degrees of freedom when normality of $\in$ holds. These Studentized residuals are easily obtained by using the option RSTUDENT in PROG REG for regression provided by SAS Institute.

Although these residuals have been used extensively to study the validity of the regression models, the heterogeneous variances of the observed residuals and the lack of independence among all types of residuals complicate interpretation of their behavior. For example an outlier
may go undetected by inflating the residuals of all other observations and may itself have a relatively small residual.

In spite of the problems associated with their use, the observed, standardized Studentized residuals have proven useful for detecting model inadequacies and outliers. For most of the cases the three types behave similarly and lead to similar conclusions. The primary advantage of Studentized residuals over the standardized residuals is their closer connection to the tdistribution. This allows the use of Student's $t$ as a convenient criterion for judging whether the residuals are inordinately large.

### 3.6.2 Plot of e versus $\hat{\mathbf{Y}}$

The plot of residuals against the fitted values of the dependent variable is particularly useful. A random scattering of points above and below the line $\mathbf{e}=\mathbf{0}$ with nearly all the data points being within the band defined by e $= \pm 2 \mathrm{~s}$

### 3.7 Influence Statistics

The reference values for the influence statistics are as follows:

- $\mathbf{v}_{\mathrm{ii}}$, elements of $\boldsymbol{P}$ (called HAT DIAG in PROC REG): Average value is $\mathrm{p}^{\prime} / \mathrm{n}$. A point is potentially influential if $\mathrm{v}_{\mathrm{ii}} \geq 2 \mathrm{p}^{\prime} / \mathrm{n}$. Where $\mathrm{p}^{\prime}$ is the number of variables in the model and n is the number of observations.
- Cook's $D$ : Cutoff value for Cook's $D$ is $4 / \mathrm{n}$ if the relationship to DFFITS is used.
- DFFITS: Absolute values greater than $2 \sqrt{ } \mathrm{p}^{\prime} / \mathrm{n}$ indicate influence on $\hat{\mathbf{Y}}$.
- DFBETAS $_{j}$ : Absolute values greater than $2 / V_{n}$ indicate influence on $\hat{\beta}_{j}$.
- COVRATIO : Values outside the interval $1 \pm 3 \mathrm{p}^{\prime} / \mathrm{n}$ indicate a major effect on the generalized variance.
The data of Maruteru, as detailed earlier, was subjected to the above regression diagnostics and the results have been discussed in Chapter VI.


### 3.8 Extent of data

When the project was started, data in hand was only a few experiments of Hyderabad centre. After the commencement of the project, a tentative schedule(proforma) for recording the ancillary information of the conducted experiment along with yield data and other particulars of interest, was prepared and sent to the respective in-charge of various centres including the Project Co-ordinator. Initially data from eight centres viz. Kalyani (W.B.), Vellanikkara (Kerala). Jabalpur (M.P.), Barrackpore (W.B.), Palampur (H.P.), Ludhiana (Punjab), Raipur (Chhattisgarh) and Coimbatore (T.N.) has been received. The data received pertain to years from 1996 to 1998 only. We required data for at least past five years. After the annual workshop of the AICRP on STCR held at at BCKVV, Kalyani, from $30^{\text {th }}$ January 2002 to $2^{\text {nd }}$ February, 2002, further data could be gathered from the annual reports of some of the centres. At other centres the data in the annual report were of use for calculating the basic data for fertilizer adjustment equations and not sufficient for performing regression analysis or response surface methodology. However the data gradually trickled in due to the intervention of the Project Coordinator of AICRP on STCR till late December 2002. The position of data is given in the appendix.
In this project we have chosen experiments from some of the centres, where the analysis could be carried out for Multiple regression, Response surface and for developing the Targeted yield equations. At other centres the sets of data were not complete and there was very short time left for the clarification and correction of the discrepancies. The details of the chosen experiments are as follows:

| S.No. | Centre | Crop/variety | Year | Season |
| :--- | :--- | :--- | :--- | :--- |
| 1. | Bhubaneswar(Orissa) | Rice(Konark) | 1998 | kharif |
| 2. | Bhubaneswar(Orissa) | Rice(Lalat) | 1999 | kharif |
| 3. | Bhubaneswar(Orissa) | Rice(Konark) | 2000 | kharif |
| 4. | Hisar(Haryana) | Wheat (542) | 1993 | Rabi |
| 5. | Hisar(Haryana) | Wheat (896) | 1995 | Rabi |
| 6. | Hisar(Haryana) | Wheat(cvsonak) | 1997 | Rabi |
| 7. | Kalyani(West Bengal) | Wheat | 1999 | Rabi |
| 8. | Kalyani(West Bengal) | BoroRice | 2000 | Kharif |
| 9. | Kalyani(West Bengal) | Rape | 1998 | Rabi |
| 10. | Hyderabad(Andhra Pradesh) | Sunflower | 1993 | Rabi |
| 11. | Hyderabad(Andhra Pradesh) | Rice | 1994 | Rabi |
| 12. | Hyderabad(Andhra Pradesh) | groundnut | 1997 | Rabi |

Besides these experiments, we have taken up some experiments for studies specific to the experiments. They are:

| S.No. | Centre | Crop/variety | Year | Season |
| :--- | :--- | :--- | :--- | :--- |
| 1. | Maruteru(Andhra Pradesh) | Rice | $!993$ | Rabi |
| 2. | Maruteru(Andhra Pradesh) | Rice | 1994 | Rabi |
| 3. | Ludhiana(Punjab) | Wheat | 1997 | Rabi |
| 4. | Coimbatore(Tamil Nadu) | Onion | 1998 | Rabi |

## Chapter -IV

## DESIGNING OF STCR EXPERIMENTS

### 4.1 Introduction

The experiments under AICRP on Soil Test Crop Response Correlation (STCR) are to be conducted on a soil with a wide range of soil fertility in terms of available nitrogen (N), phosphorus ( P ) and potassium (K). For getting the wide ranges of soil fertility, normally the fertility gradients are created in the previous season. For the fertility gradient experiment, the area is divided into four equal strips. On each strip the four different fertilizer treatments viz. 0 $\mathrm{X}, 0.5 \mathrm{X}, \mathrm{X}$ and 2 X are applied. Here X is the recommended dose of $\mathrm{N}, \mathrm{P}$ and K . It is followed by sowing of an exhaust crop, preferably a crop that is not going to be taken as a test crop in the next season. The demarcation of the strips are maintained after the harvest of the exhaust crop so as to facilitate the laying out of the soil test crop response correlation experiment in the next season.

To meet the objectives, the selection of the levels of the chemical fertilizers and the fraction of the total factorial treatment combinations is to be made in an objective fashion. The different treatment structures as explained by Ramamoorthy et. al (1967) in various co-operating centres are given in Table 5.1. Throughout this chapter we shall denote the levels of a factor at $s_{i}$ levels with $0,1, \ldots, \mathrm{~s}_{\mathrm{r}}-1$. Zero ' 0 ' generally denotes the no application of that particular factor.
Table 4.1: Treatment structures experimented in the STCR

| S.No. | Nutrient Levels |  |  | No. of treatments | Treatment Combinations |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | N | P |  |  |  |
| 1 | 5 | 4 | 3 | 22 | 000, 201, 220, 221, 222, 332, 000, 300, 322, |
|  |  |  |  |  | $\begin{aligned} & 331,422,431,100,210,211,330,421,110 \text {, } \\ & 111,200,311,432 \end{aligned}$ |
| 2 | 5 | 3 | 4 | 31 | 000, 423, 322, 101, 311, 201, 221, 303, 211, |
|  |  |  |  |  | 323, 112, 210, 203, 300, 110, 223, 302, 301, |
|  |  |  |  |  | $\begin{aligned} & 000,422,313,220,212,111,200,421,411 \text {, } \\ & 410,100,213,222 \end{aligned}$ |
| 3 | 4 | 4 | 2 | 16 | 000, 030, 011, 021, 101, 131, 110, 120, 201, |
|  |  |  |  |  | 231, 210, 220, 300, 330, 311, 321 |
| 4 | 5 | 4 | 3 | 22 | 000, 011, 100, 110, 111, 200, 201, 210, 211, |
|  |  |  |  |  | 220, 221, 222, 300, 330, 311, 331, 322, 332, |
|  |  |  |  | 24 |  |
| 5 | 4 | 3 | 2 |  | 000, 001, 010, 011, 020, 021, 100, 101, 110, $111,120,121,200,201,210,211,220,221,$ |
|  |  |  |  |  | 300, 301, 310, 311, 320, 321 |
| 6 | 5 | 4 | 4 | 14 | 000, 111, 211, 221, 222, 311, 322, 331, 332, |
|  |  |  |  |  | 333, 422, 431, 432, 433 |
| 7 | 5 | 5 | 5 | 15 | 000, 001, 010, 011, 100, 101, 110, 111, 222, |
|  |  |  |  |  | 223, 224, 232, 242, 322, 422 |
| 8 | 5 | 5 | 5 | 14 | 000, 032, 132, 232, 302, 312, 322, 330, 331, |
|  |  |  |  |  | 332, 333, 334, 342, 432 |
| 9 | 5 | 5 | 5 | 14 | 000, 033, 133, 233, 303, 313, 323, 330, 331, |
|  |  |  |  |  | 332, 333, 334, 343, 433 |
| 10 | 4 | 4 | 4 | 11 | 000, 022, 122, 202, 212, 222, 232, 220, 221, |
|  |  |  |  |  | 223, 322 |

There are many more variations of the treatment structures that are being used for field experimentation for the project. It is well known that in an experiment where it is desired to build a relationship between the response and levels of the input factors, it is desired that the number of treatment combinations tried should be more than the number of parameters estimated in the model. It is generally believed that quadratic response surface is a good fit in fertilizer trials. Thus, if we want to fit a complete quadratic response surface, we need more than 28 design points as we have 6 input factors namely, soil nitrogen (SN), soil phosphorus (SP), Soil potassium (K), added nitrogen (FN), phosphorus ( P ) and potassium (K) respectively. In this situation, the quadratic terms of SN, SP, SK and cross product terms like $\mathrm{FN} \times \mathrm{SP}, \mathrm{FN} \times \mathrm{SK}$, $F P \times S N, F P \times S K, F K \times S N F K \times S P, S N \times S P, S N \times S K$ and $S P \times$ SK may not play very important role. Therefore, we require at least 17 distinct points for fitting the response surface and some points are to be replicated to estimate the pure error. The most common treatment structure is 21 design points in case of $5 \times 4 \times 3$ factorial and 7 absolute treatment combinations i.e. per strip there are 28 design points. The design points are given at serial number 1 in Table 4.1. We have to use these design points in our further discussions; therefore, we number these points and present in Table 4.2.

Table 4.2: Design being used at present by STCR (Design points given below + 7 controls; Total 28 design points)

| Design Point | $\mathbf{N}$ | $\mathbf{P}$ | $\mathbf{K}$ |
| :---: | :---: | :---: | :---: |
| 1. | 0 | 1 | 1 |
| 2. | 1 | 0 | 0 |
| 3. | 1 | 1 | 0 |
| 4. | 2 | 1 | 1 |
| 5. | 2 | 0 | 0 |
| 6. | 2 | 1 | 0 |
| 7. | 2 | 2 | 0 |
| 8. | 2 | 0 | 1 |
| 9. | 2 | 1 | 1 |
| 10. | 2 | 2 | 1 |
| 11. | 3 | 2 | 2 |
| 12. | 3 | 0 | 0 |
| 13. | 3 | 3 | 0 |
| 14. | 3 | 1 | 1 |
| 15. | 4 | 2 | 1 |
| 16. | 4 | 3 | 2 |
| 17. | 4 | 2 | 2 |
| 18. | 4 | 3 | 1 |
| 19. |  | 2 | 1 |
| 20. |  | 3 | 2 |
| 21. |  |  | 2 |

Some of the centers also use a $5 \times 4 \times 3$ design in 32 plots per strip. These design points are given in Table 4.3.

Table 4.3: Design points given below (DESIGN 1 - Design points 13, 15, 17) + * points + 8 control; Total 32 points

| 1. | 0 | 1 | 1 |
| :---: | :---: | :---: | :---: |
| 2. | 1 | 0 | 0 |
| 3. | 1 | 1 | 0 |
| 4. | 1 | 1 | 1 |
| 5. | 2 | 0 | 0 |
| 6. | 2 | 1 | 0 |
| 7. | 2 | 2 | 0 |
| 8. | 2 | 0 | 1 |
| 9. | 2 | 1 | 1 |
| 10. | 2 | 2 | 1 |
| 11. | 3 | 2 | 2 |
| 12. | 3 | 0 | 0 |
| $13 .^{*}$ | 3 | 0 | 1 |
| $14 .^{*}$ | 3 | 1 | 0 |
| 15. | 3 | 2 | 1 |
| $16 .^{*}$ | 3 | 2 | 0 |
| $1 .^{*}$ | 4 | 2 | 1 |
| 18. | 4 | 1 | 2 |
| $19 .^{*}$ | 4 | 1 | 1 |
| $20 .^{*}$ | 4 | 2 | 2 |
| 21. | 4 | 2 | 1 |
| 22. | 4 | 3 | 2 |
| 23. | 2 | 1 |  |
| $2 .^{2}$ | 2 | 2 |  |

A discussion with the subject matter specialists, revealed that besides fitting of a restricted quadratic response surface, the following points should be kept in mind in the choice of a treatment structure. The design or the treatment structure should enable to study the (i) response due to $\mathrm{N}, \mathrm{P}$, and K , (ii) accumulation behaviour of $\mathrm{N}, \mathrm{P}$, and K (iii) dilution behaviour of $\mathrm{N}, \mathrm{P}$, and K and should include (iv) treatment combination corresponding to balanced fertilizer dose of $\mathrm{N}, \mathrm{P}$, and K and (v) a treatment combination corresponding to highest level of $\mathrm{N}, \mathrm{P}$, and K . The designs discussed in Tables 4.2 and 4.3, do not answer some of these questions. Therefore, in the present investigation an attempt has been made to develop the designs/ treatment structure taking into account the above points. These designs are discussed in the section 2.

### 4.2 Proposed Designs

In this section, we shall describe, the designs obtained for $(5 \times 4 \times 3),(4 \times 4 \times 4)$, $(4 \times 4 \times 3)$ and $(4 \times 3 \times 3)$ factorials. These designs were developed under the active support and guidance of Dr. V.K.Gupta, Head, Division of Design of Experiments and presented during the meeting with subject matter specialists, DDG(NRM) and Project Co-ordinator held at IASRI, New Delhi on April 16, 2002. The presentation was made by Dr. V.K.Gupta. although all the designs discussed above shall be given, but the design for $5 \times 4 \times 3$ factorial will be discussed in detail.

Table 4.4: DESIGN PROPOSED $(5 \times 4 \times 3)$ :
The design points given below +4 control; Total 28 design points

| Design Points | N | P | K |
| :---: | :---: | :---: | :---: |
| 1. | 0 | 2 | 1 |
| 2. | 1 | 2 | 1 |
| 3. | 2 | 2 | 1 |
| 4. | 3 | 2 | 1 |
| 5. | 4 | 2 | 1 |
| 6. | 3 | 0 | 1 |
| 7. | 3 | 1 | 1 |
| 8. | 3 | 3 | 1 |
| 9. | 3 | 2 | 0 |
| 10. | 3 | 2 | 2 |
| 11. | 0 | 3 | 2 |
| 12. | 1 | 3 | 2 |
| 13. | 2 | 3 | 2 |
| 14. | 3 | 3 | 2 |
| 15. | 4 | 3 | 2 |
| 16. | 4 | 0 | 2 |
| 17. | 4 | 1 | 2 |
| 18. | 4 | 2 | 2 |
| 19. | 4 | 3 | 0 |
| 20. | 4 | 3 | 1 |
| 21. | 2 | 1 | 1 |
| 22. | 4 | 0 | 0 |
| 23. | 0 | 3 | 0 |
| 24. | 0 | 0 | 2 |
| In place of 22, 23, and 24 one may also try the following |  |  |  |
| 22. | 4 | 1 | 1 |
| 23. | 1 | 3 | 1 |
| 24. | 1 | 1 | 2 |

In the sequel we give the comparison of the proposed design with the design given in Table 4.3.

Table 4.5: COMPARISON

| STCR DESIGN |  |  |  | DESIGN PROPOSED |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S.No. | N | P | K | S.No. | N | P | K |
| 1. | 0 | 1 | 1 | 1. | 0 | 0 | 2 |
| 2. | 1 | 0 | 0 | 2. | 0 | 2 | 1 |
| 3. | 1 | 1 | 0 | 3. | 0 | 3 | 0 |
| 4. | 1 | 1 | 1 | 4. | 0 | 3 | 2 |
| 5. | 2 | 0 | 0 | 5. | 1 | 2 | 1 |
| 6. | 2 | 1 | 0 | 6. | 1 | 3 | 2 |
| 7. | 2 | 1 | 1 | 7. | 2 | 1 | 1 |
| 8. | 2 | 2 | 1 | 8. | 2 | 2 | 1 |
| 9. | 2 | 2 | 0 | 9. | 2 | 3 | 2 |


| 10. | 2 | 0 | 1 | 10. | 3 | 3 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 11. | 2 | 2 | 2 | 11. | 3 | 3 | 1 |
| 12. | 3 | 2 | 2 | 12. | 3 | 2 | 2 |
| 13. | 3 | 0 | 1 | 13. | 3 | 0 | 1 |
| 14. | 3 | 2 | 1 | 14. | 3 | 2 | 1 |
| 15. | 3 | 1 | 1 | 15. | 3 | 1 | 1 |
| 16. | 3 | 2 | 0 | 16. | 3 | 2 | 0 |
| 17. | 3 | 1 | 0 | 17. | 4 | 3 | 0 |
| 18. | 3 | 0 | 0 | 18. | 4 | 0 | 0 |
| 19. | 4 | 1 | 1 | 19. | 4 | 0 | 2 |
| 20. | 4 | 1 | 2 | 20. | 4 | 1 | 2 |
| 21. | 4 | 2 | 1 | 21. | 4 | 2 | 1 |
| 22. | 4 | 2 | 2 | 22. | 4 | 2 | 2 |
| 23. | 4 | 3 | 1 | 23. | 4 | 3 | 1 |
| 24. | 4 | 3 | 2 | 24. | 4 | 3 | 2 |

## > For the design in Table 4.2

It is not possible to get response to N and P . However, response to K can be obtained at levels 2 of N and P and levels 3 of N and P . This design does not include the balanced fertilizer dose. However, the highest levels on $\mathrm{N}, \mathrm{P}$, and K are included as a design point.

## > For the design in Table 4.3

It is possible to get the response to N at levels 1 of P and K (and not at optimum levels of P and K that are 2 and 1 respectively).
Similarly, the response to K can be obtained at levels 2 of both N and P and at optimum levels 3 of N and 2 of P .
However, it is not possible to obtain the response of P at any levels of N and K .
> In the proposed design given in Table 4.4, however, the scenario is different.

## $>$ For studying response to N

| Design points 1-5 |  |  |  | Design points 11-15 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| Point | $\mathbf{N}$ | P | K | Point | $\mathbf{N}$ | P | K |  |
| 1. | $\mathbf{0}$ | 2 | 1 | 11. | $\mathbf{0}$ | 3 | 2 |  |
| 2. | $\mathbf{1}$ | 2 | 1 | 12. | $\mathbf{1}$ | 3 | 2 |  |
| 3. | $\mathbf{2}$ | 2 | 1 | 13. | $\mathbf{2}$ | 3 | 2 |  |
| 4. | $\mathbf{3}$ | 2 | 1 | 14. | $\mathbf{3}$ | 3 | 2 |  |
| 5. | $\mathbf{4}$ | 2 | 1 | 15. | $\mathbf{4}$ | 3 | 2 |  |

## $>$ For studying response to $P$

| Design points 4, 6, 7, 8 |  |  |  | Design points 15, 16, 17, 18 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Point | N | $\mathbf{P}$ | K | Point | N | $\mathbf{P}$ | K |
| 4. | 3 | $\mathbf{2}$ | 1 | 15. | 4 | $\mathbf{3}$ | 2 |
| 6. | 3 | $\mathbf{0}$ | 1 | 16. | 4 | $\mathbf{0}$ | 2 |
| 7. | 3 | $\mathbf{1}$ | 1 | 17. | 4 | $\mathbf{1}$ | 2 |
| 8. | 3 | $\mathbf{3}$ | 1 | 18. | 4 | $\mathbf{2}$ | 2 |

## For studying response to $K$

| Design point 4, 9, 10 |  |  |  | Design points 15, 19, 20 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Point | N | P | K | Point | N | P | K |
| 4. | 3 | 2 | $\mathbf{1}$ | 15. | 4 | 3 | $\mathbf{2}$ |
| 9. | 3 | 2 | $\mathbf{0}$ | 19. | 4 | 3 | $\mathbf{0}$ |
| 10. | 3 | 2 | $\mathbf{2}$ | 20. | 4 | 3 | $\mathbf{1}$ |

For studying accumulation behaviour of N, P, K

| Points | $\mathbf{N}$ | $\mathbf{P}$ | $\mathbf{K}$ |  | $\mathbf{N}$ | $\mathbf{N}$ | $\mathbf{P}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{K}$ | $\mathbf{K}$ |  |  |  |  |  |
| 22. | 4 | 0 | 0 | 4 | 1 | 1 |  |
| 23. | 0 | 3 | 0 | or | 1 | 3 | 1 |
| 24. | 0 | 0 | 2 |  | 1 | 1 | 2 |

For studying dilution behaviour of N, P, K

| Points | $\mathbf{N}$ | $\mathbf{P}$ | $\mathbf{K}$ |
| :---: | :---: | :---: | :---: |
| 11. | 0 | 3 | 2 |
| 16. | 4 | 0 | 2 |
| 19. | 4 | 3 | 0 |

## Balanced fertilizer doses/Highest Doses

| Points | $\mathbf{N}$ | $\mathbf{P}$ | $\mathbf{K}$ |
| :---: | :---: | :---: | :---: |
| 4. | 3 | 2 | 1 |
| 15. | 4 | 3 | 2 |

## Comparison

| Characteristic | Design (Table 4.2) | Design (Table 4.3) | Proposed <br> Design |
| :---: | :---: | :---: | :---: |
| Response to N at optimum <br> levels of P and K (2 and 1) | No | No <br> (Possible only at <br> levels 1 0f P and K) | Yes |
| Response to P at optimum <br> levels of N and K (3 and 1) | No | No | Yes |
| Response to K at optimum <br> levels of N and P (3 and 2) | No <br> (Possible at levels 2 <br> of N and P and levels <br> 3 of N and P) | Yes | Yes |
| Accumulation behaviour | No |  |  |
| Dilution behaviour | No | No | Yes |
| Balanced dose | No | Yos | Yes |
| Highest dose | Yes | Yes | Yes |

Note 4.1: It can be observed that the proposed design involves some of the design points that involve application of phosphorus and potassium at zero level of nitrogen. Some agronomists may have an objection to the inclusion of such points in the design. These points are, however, necessary to study the accumulation behaviour of P and K . If required, these points may be replaced by the points where the nitrogen is at lowest level other than zero. This, however, may not provide the accumulation behaviour of a particular input. If the accumulation behaviour of $P$ and K are not of interest (as was felt by some of the subject matter specialists in meeting held at IASRI, New Delhi on April 16, 2002), then one may think of replacing these points by some
other combinations. The points 021 (point number 1 in Table 4.4) and 032 (point number 11 in Table 4.4) are required for obtaining the response of nitrogen. One may think of experimenting with non-zero levels of $\mathrm{N}, \mathrm{P}$ and K . Of course absolute control 000 may be included in the experiment to study the relationship between the soil test values in the unfertilized plots and the corresponding crop yields.

In the sequel we give the designs for $(4 \times 4 \times 4)$, $(4 \times 4 \times 3)$ and $(4 \times 3 \times 3)$ experiments. The discussion in note 4.1 is also applicable to these designs.

Table 4.6: DESIGN PROPOSED ( $4 \times 4 \times 4$ ): The design points given below +4 control; Total 28 design points

| Design Points | N | P | K |
| :---: | :---: | :---: | :---: |
| 1. | 0 | 2 | 2 |
| 2. | 1 | 2 | 2 |
| 3. | 2 | 2 | 2 |
| 4. | 3 | 2 | 2 |
| 5. | 2 | 0 | 2 |
| 6. | 2 | 1 | 2 |
| 7. | 2 | 3 | 2 |
| 8. | 2 | 2 | 0 |
| 9. | 2 | 2 | 1 |
| 10. | 2 | 2 | 3 |
| 11. | 0 | 3 | 3 |
| 12. | 1 | 3 | 3 |
| 13. | 2 | 3 | 3 |
| 14. | 3 | 3 | 3 |
| 15. | 3 | 0 | 3 |
| 16. | 3 | 1 | 3 |
| 17. | 3 | 2 | 3 |
| 18. | 3 | 3 | 0 |
| 19. | 3 | 3 | 1 |
| 20. | 3 | 3 | 2 |
| 21. | 2 | 1 | 1 |
| 22. | 3 | 0 | 0 |
| 23. | 0 | 3 | 0 |
| 24. | 0 | 0 | 3 |
| In place of 22,23 , and 24 one may also try the following |  |  |  |
| 22. | 3 | 1 | 1 |
| 23. | 1 | 3 | 1 |
| 24. | 1 | 1 | 3 |

Table 4.7: DESIGN PROPOSED ( $4 \times 4 \times 3$ ):
The design points given below +7 control; Total 28 design points

| Design <br> Points | $\mathbf{N}$ | $\mathbf{P}$ | $\mathbf{K}$ |
| ---: | :---: | :---: | :---: |
| 1. | 0 | 2 | 1 |
| 2. | 1 | 2 | 1 |
| 3. | 2 | 2 | 1 |
| 4. | 3 | 2 | 1 |
| 5. | 2 | 0 | 1 |
| 6. | 2 | 1 | 1 |
| 7. | 2 | 3 | 1 |
| 8. | 2 | 2 | 0 |
| 9. | 2 | 2 | 2 |
| 10. | 0 | 3 | 2 |
| 11. | 1 | 3 | 2 |
| 12. | 2 | 3 | 2 |
| 13. | 3 | 3 | 2 |
| 14. | 3 | 0 | 2 |
| 15. | 3 | 1 | 2 |
| 16. | 3 | 2 | 2 |
| 17. | 3 | 3 | 0 |
| 18. | 3 | 3 | 1 |
| 19. | 3 | 0 | 0 |
| 20. | 0 | 3 | 0 |
| 21. | 0 | 0 | 2 |

In place of 19, 20, and 21 one may also try the
following

| 19. | 3 | 1 | 1 |
| ---: | :---: | :---: | :---: |
| 20. | 1 | 3 | 1 |
| 21. | 1 | 1 | 2 |

Table 4.8: DESIGN PROPOSED (4x3x3): The design points given below + 4 control; Total 24 design points

| Design <br> Points | N | P | K |
| :---: | :---: | :---: | :---: |
| 1. | 0 | 1 | 1 |
| 2. | 1 | 1 | 1 |
| 3. | 2 | 1 | 1 |
| 4. | 3 | 1 | 1 |
| 5. | 2 | 0 | 1 |
| 6. | 2 | 2 | 1 |
| 7. | 2 | 1 | 0 |
| 8. | 2 | 1 | 2 |
| 9. | 0 | 2 | 2 |
| 10. | 1 | 2 | 2 |
| 11. | 2 | 2 | 2 |
| 12. | 3 | 2 | 2 |
| 13. | 3 | 2 | 0 |
| 14. | 3 | 2 | 1 |
| 15. | 3 | 0 | 2 |
| 16. | 3 | 1 | 2 |
| 17. | 1 | 1 | 2 |
| 18. | 3 | 0 | 0 |
| 19. | 0 | 2 | 0 |
| 20. | 0 | 0 | 2 |
| In place of 18,19 , and 20 , one may also try the following |  |  |  |
| 18. | 3 | 0 | 1 |
| 19. | 3 | 1 | 0 |
| 20. | 1 | 2 | 1 |

## 4.3: Designing with Organic Manure (OM) and Bio-fertilizers (BF)

In addition to the objectives mentioned in section 4.1, the experiment is also aimed at evolving basis for conjoint use of organic manures and fertilizers efficiently in providing integrated nutrient supply system. The inclusion of organic manure(s) (OM) and biofertilizers (BF) in the experiment shall be discussed in the sequel. We shall illustrate the designing with OM and BF for one case, i.e., $5 \times 4 \times 3$ experiment. For other cases, it can be done similarly.

Suppose that OM with 4 levels as OM0, OM1, OM2, OM3 required to be introduced in the design. To get the treatment structure of the $5 \times 4 \times 3(\mathrm{~N} \times \mathrm{P} \times \mathrm{K})$ design with four levels of OM :

- Divide 24 treatment combinations into 4 groups named as A, B, C and D and control treatment is added once to each group.
- Each group thus has 7 treatment combinations.

The groups formed are shown below:


The OM levels denoted as OM0, OM1, OM2, OM3 are superimposed on the 4 strips as follows:

|  | I | II | III | IV |
| :---: | :---: | :---: | :---: | :---: |
| OM3 | A | B | C | D |
| OM2 | B | C | D | A |
| OM1 | C | D | A | B |
| OM0 | D | A | B | C |

The main features of the above design are:

- This arrangement is a Latin Square type arrangement.
- All treatment combinations are tried on each level of OM. All treatment combinations are tried on all the strips.
- All the four groups viz. A, B, C, D, are appearing with every level of OM and also in all the strips precisely once.
- This design may be viewed alternatively as a reinforced resolvable block design with four replications (or resolvable groups). Each group is a complete replicate.
- The 4 levels of OM are the 4 replications or the 4 resolvable groups.
- There are four blocks within each replication. The four strips on each level of OM are the 4 blocks. In all there are 16 blocks.
- There are 6 treatment combinations in each block.
- Each block is reinforced with a control treatment.
- Thus the resolvable design has the following parameters:

Number of treatments, $\mathrm{v}=24+1$ (control), Number of replications $=4$, Number of blocks per replication $=4$, Total number of blocks $=16$, Number of treatment combinations per block or the block size $=7$, Replication of treatment combinations $=4$, Replication of the control treatment $=$ 16.

## > How to Analyze the Data?

The analysis of the data generated can be presented in the following ANOVA:

| Source | D.F. |
| :--- | :--- |
| Replications (OM) | 3 |
| Blocks within replication [Strips within levels of OM] | 12 |
| Treatments | 24 |
| Error | 72 |
| Total | $\mathbf{1 1 1}$ |

Through this analysis one can identify the best level of OM. Analysis of covariance may also be carried out using SN, SP and SK as covariates.

The ANCOVA will be as follows:

| Source | D.F. |
| :--- | :--- |
| Replication (OM) | 3 |
| Blocks within replication [Strips within levels of OM] | 12 |
| Treatments | 24 |
| SN | 1 |
| SP | 1 |
| SK | 1 |
| Error | 69 |
| Total | $\mathbf{1 1 1}$ |

One may be interested in comparing the performance of treatment combinations at different levels of OM. For example, one may be interested to study whether or not the effect of balanced fertilizer dose is same at OM0 and OM3 levels of OM? For making such comparisons, contrast analysis would be useful. However, to make such comparisons possible, one needs to analyze the data differently. Instead of 25 treatment combinations ( $24+$ one control), now one has to think of $25 \times 4=100$ treatment combinations obtained by taking the combinations of 25 treatments and 4 levels of OM. The data is then analyzed as per procedure of completely randomized designs and taking SN, SP and SK as covariates. This procedure ignores the effect of strips that seems appropriate, as SN, SP and SK have been included as covariates.

One may be interested in studying the effect of OM on the relationship of soil test values (SN, SP and SK) and added fertilizers FN, FP and FK. To study this, one may

- Fit the second order response surface to the 28 design points at each level of OM ignoring the effect of strips.
- The effect of strips may be ignored since we are taking soil parameters into consideration.

$$
\begin{aligned}
\mathrm{y}= & \beta_{0}+\beta_{1} \mathrm{SN}+\beta_{2} \mathrm{SP}+\beta_{3} \mathrm{SK}+\beta_{4} \mathrm{FN}+\beta_{5} \mathrm{FP}+\beta_{6} \mathrm{FK}+\beta_{7} \mathrm{FN}^{2} \\
& +\beta_{8} \mathrm{FP}^{2}+\beta_{9} \mathrm{FK}+\beta_{10} \mathrm{FN} \times \mathrm{FP}+\beta_{11} \mathrm{FN} \times \mathrm{FK}+\beta_{12} \mathrm{FP} \times \mathrm{FK} \\
& +\beta_{13} \mathrm{FN} \times \mathrm{SN}+\beta_{14} \mathrm{FP} \times \mathrm{SP}+\beta_{15} \mathrm{FK} \times \mathrm{SK}+\mathrm{e}
\end{aligned}
$$

- Test the homogeneity of the four regression equations.
- If the regression equations are not homogeneous, then separate recommendations may be made for each level of organic manure otherwise we can pool the data and fit only one response surface.
- If we are interested in giving recommendations on the given level of OM, then the effect of OM can also be incorporated into the model as:

$$
\begin{aligned}
\mathrm{y}= & \beta_{0}+\beta_{1} \mathrm{SN}+\beta_{2} \mathrm{SP}+\beta_{3} \mathrm{SK}+\beta_{4} \mathrm{FN}+\beta_{5} \mathrm{FP}+\beta_{6} \mathrm{FK}+\beta_{7} \mathrm{FN}^{2} \\
& +\beta_{8} \mathrm{FP}^{2}+\beta_{9} \mathrm{FK}^{2}+\beta_{10} \mathrm{FN} \times \mathrm{FP}+\beta_{11} \mathrm{FN} \times \mathrm{FK}+\beta_{12} \mathrm{FP} \times \mathrm{FK} \\
& +\beta_{13} \mathrm{FN} \times \mathrm{SN}+\beta_{14} \mathrm{FP} \times \mathrm{SP}+\beta_{15} \mathrm{FK} \times \mathrm{SK}+\beta_{16} \mathrm{OM}+\mathrm{e}
\end{aligned}
$$

Here OM is taken as covariate. If the organic manure levels are quantitative in nature, then we may include the interaction terms of OM with and FK in the model. Since all the 25 distinct design points have been tried at each level FN, FP of OM, therefore, separate response curves may also be fitted for $\mathrm{N}, \mathrm{P}$ and K at each level of OM. The homogeneity of the response curves for $\mathrm{N}, \mathrm{P}$, and K may also be tested over all levels of OM.

### 4.4 Discussion

In the meeting held at IASRI, New Delhi on April 16, 2002, it was felt that these experiments have been continuing since long. Therefore, now we should conduct experiments with N ( 3 levels), P (3 levels) and K (3 levels). The levels of N, P and K are to be decided based on the results of previous experiments. Three levels of organic manure are to be incorporated while deciding the treatment structure. The three levels should not include the zero application of the particular input. Absolute control treatments, however, can be incorporated in the design. An effort to finalize the design in discussion with the Project Co-ordinator and subject matter specialists is in progress.

Table 4.8 : Treatments Structures (as reported) experimented in the STCR at various centres

| Sl.No. | Centre/crop/ variety/year | Nutrient Levels |  |  |  | No.of treatments | Treatments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | FYM | N | P | K |  |  |
| 1. | Kalyani/ <br> Rice/IET- 4094/1996 | 0 | 5 | 4 | 3 | 27 | Same combination in all strips 011,100,110,111,200,201,210, 211,220,221,222,300,311,322, 330,331,332,421,422,431,432, 000 ( 7 times ) |
| 2. | Jabalpur/Sunfl ower/Modern/ 1997 | 4 | 5 | 4 | 3 | 30 | Strip-I $0100,0200,0201,0210,0220,0221$ $0222,0311,0332,0422,1000,1300$ $1322,1331,1422,1431,2000,2100$ $2210,2211,2330,2421,3000,3110$ $3111,3200,3311,3432,0000,0000$ Strip-II $0110,0111,0211,0300,0330,0322$ $0331,0421,0431,0432,1000,1100$ $1200,1220,1222,1330,2000,2111$ $2201,2221,2311,2332,3000,3210$ $3322,3331,3422,3431$ Strip -III $0100,0200,0201,0210,0220,0221$ $0222,0311,0332,0422,1000,1110$ $1111,1221,1332,1432,2000,2220$ $2222,2322,2331,2431,3000,3201$ $3211,3300,3330,3421$ Strip -IV $0110,0111,0211,0300,0322,0330$ $0331,0421,0431,0432,1000,1201$ $1210,1211,1311,1421,2000,2110$ $2200,2300,2422,2432,3000,3100$ $3220,3221,3222,3332$ |


| 3. | Hyderabad | 0 | 4 | 3 | 3 | 30 | Same combinations in all strips $100,101,102,110,111,112,120$ $121,122,200,201,202,210,211$ $212,220,221,222,300,301,302$ $310,311,312,320,321,322,000$ 000,000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4. | Coimbatore (Ragi) | 3 | 5 | 3 | 4 | 24 | Strip -I $0000,0000,0000,0000,1000,1010$ $1110,2000,2011,2020,2100,2110$ $2120,2221,3001,3031,3111,3131$ $3221,3231,4120,4131,4220,4231$ Strip -II $0000,0000,0000,0000,1001,1011$ $1111,2001,2011,2021,2101,2111$ $2120,2220,3000,3030,3100,3130$ $3221,3230,4120,4130,4220,4231$ Strip -III 0000,0000,0000,0000,1001,1010 $1111,2000,2010,2021,2100,2110$ $2121,2221,3000,3031,3111,3131$ $3220,3230,4121,4130,4221,4230$ Strip -IV $0000,0000,0000,0000,1000,1011$ $1110,2001,2010,2020,2101,2111$ $2121,2220,3001,3030,3110,3130$ $3220,3231,4121,4131,4221,4230$ |
| 5. | Coimbatore ( Sorghum ) | 3 | 5 | 4 | 3 | 24 | Strip -I $0000,0000,0001,0002,1002,1102$ $1112,2002,2012,2100,2110,2200$ $2210,2220,3001,3111,3220,3300$ $3311,3320,4210,4220,4311,4321$ Strip -II $0000,0000,0001,0002,1000,1100$ $1111,2000,2011,2101,2111,2200$ $2212,2222,3000,3110,3221,3302$ $3310,3320,4212,4222,4310,4320$ Strip -III $0000,0000,0001,0002,1001,1100$ $1110,2000,2010,2102,2112,2201$ $2210,2221,3002,3110,3220,3301$ $3310,3322,4210,4221,4312,4320$ Strip -IV $0000,0000,0001,0002,1000,1101$ $1110,2001,2010,2100,21102202$ $2211,2220,3000,3112,3222,3300$ $3312,3321,4211,4220,4310,4322$ |
| 6. | Ludhiana ( Maize ) | 0 | 5 | 4 | 3 | 27 | $011,100,110,111,200,201,210$ $211,220,221,222,300,311,322$ $330,331,332,421,422,431,432$ 000 ( 6 times as control ) |


| 7. | Ludhiana ( Wheat ) | 0 | 4 | 3 | 3 | 40 | $\begin{aligned} & \hline 021,121,201,211,220,221,222 \\ & 231,321,331 \\ & \text { ( This set of treatments is } \\ & \text { repeated } 4 \text { times in each strip ) } \\ & \hline \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8. | Palampur ( Wheat) | 4 | 5 | 4 | 3 | 30 | Strip -I <br> 0000,0000,0100,0200,0201,0210 <br> 0220,02210222,0311,0332,0422, <br> 1000,13001322,1331,1422,1431, <br> 2000,21002210,2211,2330,2422, <br> 3000,3110,3111,3200,3311,3423 <br> Strip -II <br> 0000,0000,0110,0111,0211,0300 <br> 0322,03300331,0421,0431,0432, <br> 1000,11001200,1220,1222,1300, <br> 2000,21112201,2221,2311,2332, <br> 3000,3210,3322,3331,3422,3431 <br> Strip -III <br> 0000,0000,0100,0200,0201,0210 <br> 0220,0221,0222,0311,0332,0422 <br> 1000,1110,1111,1221,1332,1432 <br> 2000,2220,2222,2322,2331,2431 <br> 3000,3201,3211,3300,3330,3421 <br> Strip -IV <br> 0000,0000,0110,0111,0211,0300 <br> 0322,0330,0331,0421,0431,0432 <br> 1000,1200,1210,1211,1311,1421 <br> 2000,2110,2200,2300,2422,2432 <br> 3000,3100,3220,3221,3222,3332 |
| 9. | Vellanikkara <br> Kerala <br> (Banana) | 0 | 5 | 4 | 3 | 27 | $\begin{aligned} & \hline 011,100,110,111,200,201,210 \\ & 211,220,221,222,300,311,322 \\ & 330,331,332,421,422,431,432 \\ & 000 \text { ( 6 times ) } \\ & \hline \end{aligned}$ |
| 10. | Hisar <br> Wheat-912 | 0 | 5 | 4 | 3 | 28 | $\begin{aligned} & 422,431,300,331,332,011,311 \\ & 200,432,111,110,221,222,322 \\ & 220,201,210,330,211,421,100 \\ & 000(7 \text { times }) \end{aligned}$ |

## Chapter-V

## RESULTS AND DISCUSSION

It is well known that fertilizer is an important input in agricultural crop production. Besides being soil hazard in the long run, it is also cost intensive. Therefore its judicious use is very essential for any country. With a view to reduce the use of fertilizer nutrients, the AICRP on Soil Test Crop Response correlation was launched.
Having discussed the various problems associated with the analysis of these experiments in earlier chapters, the remedial measures were investigated.

We now give in the sequel, the results of the experiments conducted under STCR project, centre wise.

## BHUBANESHWAR

At this centre, an experiment on paddy with variety as 'Konark' conducted over the years 1998, 1999 and 2000 in the Kharif season has been selected. The fertilizer doses are same in all the years. They are $0,25,50,75 \mathrm{~kg} / \mathrm{ha}$ of Nitrogen, $0,20,40,60,80$ $\mathrm{kg} /$ ha of Phosphorus and $0,20,40 \mathrm{~kg} / \mathrm{ha}$ of Potassium.

The data of the experiment conducted in the year 1998 was subjected to multiple regression analysis as explained earlier. A look at the table 5.1 .1 shows that over $90 \%$ of the variability is explained by the models with $9,12,15$ and 18 variables and looking at the table 5.1.2, in the backward elimination process, it is observed that models with 9 and 12 variables shows linear trend for fertilizer Phosphorus (FP) and Potash (FK) as significant variables and linear and quadratic trend for fertilizer Nitrogen (FN). In case of 15 and 18, the resulting significant variables although explains $97 \%$ of variability but only FK shows linear effect whereas there is quadratic effect of FP and FK. Other effects found significantly contributing are soil Nitrogen (SN), Quadratic effects of soil Phosphorus (SP) and soil Potash (SK) and the interactions between FN and SN, between FP and SP and between FN and FP.

From these it is observed that the linear, quadratic and interaction effects of FN, FP and FK are all not significant and the criteria of signs are not of the form ",,+-- ," and therefore the optimum values cannot be derived from these equations. Similar is the case for the years 1999 and 2000.

Therefore, the data for the three years were subjected to analysis by Response surface methodology. In this case the stationary point is a saddle point (as discussed earlier). Therefore exploration of the response surface in the vicinity of the stationary point was attempted. In this case the variables SN, SP and SK have been taken as covariates. Optimum values have been calculated by taking into consideration the mean values of SN, SP and SK. In table 5.7, optimum fertilizer doses obtained by Targeted yield approach and Response surface approach have been compared. Maximum response achievable by Response surface methodology has been taken as Targeted yield for the crops at all the centres. This has been done to check the reliability of the Optimum doses calculated by the Targeted yield approach. From this table it is observed that for the year 1998, a maximum response of $40.98 \mathrm{q} \mathrm{ha}^{-1}$ is achievable by taking FN as $70 \mathrm{~kg} \mathrm{ha}^{-1}$, FP as $58 \mathrm{~kg} \mathrm{ha}^{-1}$ and FK as $23 \mathrm{~kg} \mathrm{ha}{ }^{-1}$
respectively. The corresponding optimum values by Targeted yield approach are FN= $63, \mathrm{FP}=58$ and $\mathrm{FK}=35 \mathrm{~kg} \mathrm{ha}^{-1}$. These optimal values obtained by both the methods i.e. response surface and Targeted yield equation are moderately similar. The optimal values for the other two years i.e. 1999 and 2000 also are also fairly similar. This gives credibility to the Targeted yield approach as has been verified by the Response surface methodology in the above case.

## HYDERABAD

(1) At this centre, an experiment on Sunflower conducted in the year 1993-94 Rabi season has been selected. The fertilizer doses are $0,40,80,120 \mathrm{~kg} / \mathrm{ha}$ of Nitrogen; 0, 40, $80 \mathrm{~kg} / \mathrm{ha}$ of Phosphorus and $0,40,80 \mathrm{~kg} / \mathrm{ha}$ of Potassium.

The experiment was subjected to multiple regression analysis as explained earlier. A look at the table 5.2 .1 shows that over 76 to $80 \%$ of the variability is explained by the models with $9,12,15$ and 18 variables and looking at the table 5.2.2, in the backward elimination process, it is observed that the model with 12 variables (STCR model) shows linear trend for fertilizer Nitrogen (FN) , quadratic trend for FN and FP and interaction (FP X SP) as significant variables. In case of 15 and 18, the resulting significant variables are similar. Other effects found significantly contributing are soil Phosphorus (SP), Soil Potash (FK) and quadratic effect of soil Phosphorus (SP) and the interactions between FN and FK. The Optimum value calculated from the model with 12 variables gives $\mathrm{FN}=111 \mathrm{~kg} /$ ha and $\mathrm{FP}=41 \mathrm{~kg} / \mathrm{ha}$. The optimum value for FK is not derivable.

An interesting aspect is that by adding replication as a variable in the model with 15 variables, the $\mathrm{R}^{2}$ value has increased to $83 \%$. The replication effect is significant. Moreover the soil variables SN, SP and SK are also significant, thereby showing (table 5.2.3) the creation of fertility gradient (one of the feature of STCR project).

When the data was subjected to analysis by Response surface methodology it is observed that the stationary point is a saddle point (as discussed earlier). Therefore exploration of the response surface in the vicinity of the stationary point was attempted. In this case the variables SN, SP and SK have been taken as covariates. Optimum values have been calculated by taking into consideration the mean values of SN, SP and SK. In table 5.7, optimum fertilizer doses obtained by Targeted yield approach and Response surface approach have been compared. Maximum response achievable by Response surface methodology has been taken as Targeted yield for the crops at all the centres. This has been done to check the reliability of the Optimum doses calculated by the Targeted yield approach. From this table it is observed that for this experiment, a maximum response of $15.12 \mathrm{q} \mathrm{ha}^{-1}$ is achievable by taking FN as $100 \mathrm{~kg} \mathrm{ha}^{-1}$, FP as $41 \mathrm{~kg} \mathrm{ha}^{-1}$ and FK as $14 \mathrm{~kg} \mathrm{ha}^{-1}$ respectively. The corresponding optimum values by Targeted yield approach are $\mathrm{FN}=106, \mathrm{FP}=79$ and $\mathrm{FK}=57 \mathrm{~kg} \mathrm{ha}{ }^{-1}$. These optimal values obtained by both the methods i.e. response surface and Targeted yield equation are moderately similar for FN but fairly different for FP and FK. The reason for this may be that in the reported data it is not mentioned whether the values of soil FP and FK are actual values of Phosphorus and Potash or they are in the form of $\mathrm{P}_{2} \mathrm{O}_{5}$ and $\mathrm{K}_{2} \mathrm{O}$.
(2) Another experiment which have been considered for this centre is an experiment on Groundnut conducted in the year 1997-98 in the Rabi season.
The fertilizer doses are $0,15,30,60 \mathrm{~kg} /$ ha of Nitrogen; $0,30,60 \mathrm{~kg} / \mathrm{ha}$ of Phosphorus and $0,30,60 \mathrm{~kg} / \mathrm{ha}$ of Potassium. There were in all 30 treatments in each strip consisting of 26 fertilizer treatment combination and 4 controls
The experiment was subjected to multiple regression analysis as explained earlier. A look at the table 5.2 .6 shows that over 86 to $97 \%$ of the variability is explained by the models with $9,12,15$ and 18 variables and looking at the table 5.2.7, in the backward elimination process, it is observed that in the model with 9 variables, the effects found significant were FN, FP, FK, $\mathrm{FN}^{2}$ and interaction $\mathrm{FN} \times \mathrm{FP}\left(\mathrm{R}^{2}=85 \%\right)$. For 12 variables (STCR model), the variables $\mathrm{FN}, \mathrm{FN}^{2}$, SP and interactions $\mathrm{FN} \times$ SN, FP $\times$ SP, and $\mathrm{FK} \times$ SK are significant $\left(\mathrm{R}^{2}=94.88 \%\right)$ In case of 15 and 18 , the resulting significant variables are similar $\left(\mathrm{R}^{2}=95 \%\right)$ i.e the quadratic terms of FN, FP and FK are significant, excepting the fact that with 18 variables, the interactions FN $\times$ FP, FN $\times$ FK and FP $\times$ FK are also significant. The signs of the different effects do not follow the desired ' + , - , -' form and even if some of the optimal values which could be derived, the process is very cumbersome. However a test of Normal Probability plot below shows that the data are normally distributed
Normal P-P Plot of Regression

Scatterplot
Dependent Variable: YIELD


Regression Studentized Residual

The scatter plot also shows fairy uniform pattern of spread although some outliers are observed which goes beyond the (+2,-2) interval. Here also it is observed (table 5.2.8) that by adding replication as a variable in the all the models, there is an increase in $\mathrm{R}^{2}$ values. More over the value of $\mathrm{R}^{2}$ is further increased by using the variables $\mathrm{FN} \times \mathrm{FP}$, $\mathrm{FN} \times \mathrm{FK}$ and $\mathrm{FP} \times \mathrm{FK}$ in place of $\mathrm{SN}^{2} \mathrm{SP}^{2}$ and $\mathrm{SK}^{2}$ respectively for the model (table 5.2.11)with15 and16(with replication) variables. The replication effect is significant in all the models (models with 10, 13, 16 and 19 variables). Thereby showing the creation of fertility gradient (one of the feature of STCR project). The soil variables SN, SP and the interactions $\mathrm{FN} \times$ SN and $\mathrm{FP} \times$ SP are significant. Again the optimal doses are derivable but one has to solve a number of equations

When the data was subjected to analysis by Response surface methodology it is observed that the stationary point is a saddle point (as discussed earlier). Therefore exploration of the response surface in the vicinity of the stationary point was attempted. In this case the variables SN, SP and SK have been taken as covariates. Optimum values have been calculated by taking into consideration the mean values of SN, SP and SK. In table 5.7, optimum fertilizer doses obtained by Targeted yield approach and Response surface approach have been compared. Maximum response achievable by Response surface methodology has been taken as Targeted yield for the crops at all the centres. This has been done to check the reliability of the Optimum doses calculated by the Targeted yield approach. From this table it is observed that for this experiment, a maximum response of $20.48 \mathrm{q} \mathrm{ha}^{-1}$ is achievable by taking FN as $29 \mathrm{~kg} \mathrm{ha}^{-1}$, FP as $39 \mathrm{~kg} \mathrm{ha}^{-1}$ and FK as $35 \mathrm{~kg} \mathrm{ha}^{-1}$ respectively by Response surface methodology. The corresponding optimum values by Targeted yield approach are $\mathrm{FN}=28, \mathrm{FP}=47$ and $\mathrm{FK}=83 \mathrm{~kg} \mathrm{ha}^{-1}$. These optimal values obtained by both the methods i.e. response surface and Targeted yield equation are moderately similar for FN and FP but fairly different for FK.
(3) The third experiment at this centre chosen was on Rice in the Rabi season conducted at the centre Maruteru. This experiment has been investigated for other aspects and discussed in detail in Chapter-III.

The fertilizer doses are $0,50,100,150 \mathrm{~kg} / \mathrm{ha}$ of Nitrogen; $0,40,80 \mathrm{~kg} / \mathrm{ha}$ of Phosphorus and $0,40,80 \mathrm{~kg} / \mathrm{ha}$ of Potassium. There were in all 30 treatments in each strip consisting of 27 fertilizer treatment combination and 3 controls
Out of all models tested for regression, most of them had variables like $\mathrm{FP}, \mathrm{FK}, \mathrm{FN}^{2}$, $\mathrm{FP}^{2}, \mathrm{FK}^{2}$ and interactions $\mathrm{FN} \times \mathrm{SN}, \mathrm{FP} \times$ SP etc significant(Tables 5.2.12 to 5.2.15). The variable FN was found significant only for the models with $9,10,12,15,18$ and 19 variables. $\mathrm{R}^{2}$ value for all the models was around $90 \%$. The replication effect was found significant in all the four models i.e. with variables $10,13,16$ and 19 . This shows that fertility gradient has been created. Optimal values are derivable from the models with 18,10, 13,16 and 19 variables.

## Regression Diagnostics

To apply regression diagnostics, first of all we observe the scatter plot between Yield and Standardized residuals along with the Normal probability plot which are shown below.

# Scatter plot and Normal probability plot of Maruteru Rabi Rice 1994 Experiment conducted by STCR (Total Number of Observations=120) 



Fig: 5.1(a) Scatter plot of Yield Vs Standardized Residual
No. of Observations: 120(all)
Note: observation number 19 on the far left and observation numbers, 21,24, 26 and 40 on extreme right are outside -2 to +2 range. These are outliers.

Normal P-P Plot of Regression Standardized Residual


Fig: 5.1(b) The normal P-P shown above does not have much irregularity or breaks
It is observed from the scatter plot of Standardized residuals(6.1a) above that the observations numbers $19,21,24,26$ and 40 are lying beyond the ( $+2,-2$ ) range and hence they seem to be outliers. Therefore we delete these observations one by one and see if there is any change in the pattern.

## Normal P-P Plot of Regression Standardized Residual

## Deleted observation 19

Normal P-P Plot of Regression Standardized Residual
Dependent Variable: YIELD


Deleted observation 24
Normal P-P Plot of Regression Standardized Residual


Observed Cum Prob

Observed Cum Prob

Deleted observation 40
Normal P-P Plot of Regression Standardized Residual


Deleted observation 21
Normal P-P Plot of Regression Standardized Residual Dependent Variable: YIELD


Deleted observation 26
Normal P-P Plot of Regression Standardized Residual


Observed Cum Prob

Deleted observations 19,21,24,26 \&40
Normal P-P Plot of Regression Standardized Residual


Fig: 5.2 Changes in Normal probability plots after deletion of observations

Plot of Standardized Residuals and Yield for different deleted observations

## Deleted Observation number 19



Deleted Observation number24


Deleted Observation number 40


Deleted Observation number21


## Deleted Observation number26



Deleted Observation numbers 19,21,24,26,40
Scatterplot


The above plots of standardized residual shows no change in the status of outliers. Only it is observed that Observation number 19 is influenced by other observations as in each deletion it moves further out of range. Also it is observed that observation
number 21 comes within the range of $(+2,-2)$ standardized residual, when observation 19 is deleted.

It is also observed that all these outliers, except observation number 40, lies in the Strip 0X on which no fertilizer was added in the previous season and comparatively higher yield is observed in plot numbers $21\left(72.28 \mathrm{Qh}^{-1}\right), 24\left(70.89 \mathrm{Q} \mathrm{h}^{-1}\right), 26(67.42$ $\mathrm{Qh}^{-1}$ ) and $40\left(56.30 \mathrm{Qh}^{-1}\right)$ in Strip 0X. By putting average yield values from corresponding treatments in other strips did not alter the status of the plots or of analysis. Although we cannot pin point the outlier, but it seems that there is some problem in the recording of actual data, which is generally one of the problems of outlier detection.

Our next step is to apply various regression diagnostics and calculate the parameters of influence statistics like Hat Diagonal, COVRATIO, DFFITS, DFBETAS ${ }_{j}$, and Cook's D. Critical values of these influence statistics have been calculated and presented in the table 5(a) given overleaf. A summary of influence statistics is given in table 5(b). From the table 5(b) we see that besides the outliers mentioned above, there are a few more outliers such as $10,88,93,106,108,111$ and 115 but they are not as prominent as the earlier observations $19,21,24,26$ and 40 . From table 5(a) which gives influential Statistics with critical values, it is observed that under DFFITS column, the observation number 19 has a negative sign always whenever an observation is deleted. From the sign on the DFFITS measures, we can conclude that by adding observation 19 decreases the magnitude of $\hat{y}$. From the original output statistics for all observations (not shown here because of space) it has been observed that for observation number 19, the individual DFFITS(DFBETAS) which show negative sign are Intercept, $F N, \mathrm{FP}^{2}, \mathrm{FK}^{2}, \mathrm{SN}, \mathrm{FN} \times \mathrm{SN}, \mathrm{FP} \times \mathrm{SP}$ and $\mathrm{FK} \times$ SK and thereby their magnitude of regression coefficient are decreased. This is also evident from the table, which gives final regression equations after backward elimination. It is seen that the regression coefficients for $\mathrm{FP}^{2}$, SN and $\mathrm{FN} \times$ SN have decreased. Also by deletion of observation 19 , the $\mathrm{R}^{2}$ value increases from0.9055 to 0.9145 .

Similarly by deleting observations 26 and 40 , the $\mathrm{R}^{2}$ value of the resulting equation increases in both the cases from 0.9055 to 0.9129 and 0.9125 respectively.

When these three observations are deleted, the $\mathrm{R}^{2}$ value increases to 0.9240 and the number of significant regression equations, after backward elimination, increases to 9 from 8. Therefore, it is felt that the three observations 19, 26 and 40 are superfluous and should be omitted.

The process of regression diagnostics should be attempted with great caution as an observation which looks innocent may be 'masked' by another. For simple experiments with less observation one can go ahead with Regression diagnostics but in experiments of Soil test crop response project, which has more than 100 observations for each experiment, one must be cautious in dealing with data.

## Chapter-V

## RESULTS AND DISCUSSION

It is well known that fertilizer is an important input in agricultural crop production. Besides being soil hazard in the long run, it is also cost intensive. Therefore its judicious use is very essential for any country. With a view to reduce the use of fertilizer nutrients, the AICRP on Soil Test Crop Response correlation was launched.
Having discussed the various problems associated with the analysis of these experiments in earlier chapters, the remedial measures were investigated.

We now give in the sequel, the results of the experiments conducted under STCR project, centre wise.

## BHUBANESHWAR

At this centre, an experiment on paddy with variety as 'Konark' conducted over the years 1998, 1999 and 2000 in the Kharif season has been selected. The fertilizer doses are same in all the years. They are $0,25,50,75 \mathrm{~kg} / \mathrm{ha}$ of Nitrogen, $0,20,40,60,80$ $\mathrm{kg} /$ ha of Phosphorus and $0,20,40 \mathrm{~kg} / \mathrm{ha}$ of Potassium.

The data of the experiment conducted in the year 1998 was subjected to multiple regression analysis as explained earlier. A look at the table 5.1 .1 shows that over $90 \%$ of the variability is explained by the models with $9,12,15$ and 18 variables and looking at the table 5.1.2, in the backward elimination process, it is observed that models with 9 and 12 variables shows linear trend for fertilizer Phosphorus (FP) and Potash (FK) as significant variables and linear and quadratic trend for fertilizer Nitrogen (FN). In case of 15 and 18, the resulting significant variables although explains $97 \%$ of variability but only FK shows linear effect whereas there is quadratic effect of FP and FK. Other effects found significantly contributing are soil Nitrogen (SN), Quadratic effects of soil Phosphorus (SP) and soil Potash (SK) and the interactions between FN and SN, between FP and SP and between FN and FP.

From these it is observed that the linear, quadratic and interaction effects of FN, FP and FK are all not significant and the criteria of signs are not of the form ",,+-- ," and therefore the optimum values cannot be derived from these equations. Similar is the case for the years 1999 and 2000.

Therefore, the data for the three years were subjected to analysis by Response surface methodology. In this case the stationary point is a saddle point (as discussed earlier). Therefore exploration of the response surface in the vicinity of the stationary point was attempted. In this case the variables SN, SP and SK have been taken as covariates. Optimum values have been calculated by taking into consideration the mean values of SN, SP and SK. In table 5.7, optimum fertilizer doses obtained by Targeted yield approach and Response surface approach have been compared. Maximum response achievable by Response surface methodology has been taken as Targeted yield for the crops at all the centres. This has been done to check the reliability of the Optimum doses calculated by the Targeted yield approach. From this table it is observed that for the year 1998, a maximum response of $40.98 \mathrm{q} \mathrm{ha}^{-1}$ is achievable by taking FN as $70 \mathrm{~kg} \mathrm{ha}^{-1}$, FP as $58 \mathrm{~kg} \mathrm{ha}^{-1}$ and FK as $23 \mathrm{~kg} \mathrm{ha}{ }^{-1}$
respectively. The corresponding optimum values by Targeted yield approach are FN= $63, \mathrm{FP}=58$ and $\mathrm{FK}=35 \mathrm{~kg} \mathrm{ha}^{-1}$. These optimal values obtained by both the methods i.e. response surface and Targeted yield equation are moderately similar. The optimal values for the other two years i.e. 1999 and 2000 also are also fairly similar. This gives credibility to the Targeted yield approach as has been verified by the Response surface methodology in the above case.

## HYDERABAD

(1) At this centre, an experiment on Sunflower conducted in the year 1993-94 Rabi season has been selected. The fertilizer doses are $0,40,80,120 \mathrm{~kg} / \mathrm{ha}$ of Nitrogen; 0, 40, $80 \mathrm{~kg} / \mathrm{ha}$ of Phosphorus and $0,40,80 \mathrm{~kg} / \mathrm{ha}$ of Potassium.

The experiment was subjected to multiple regression analysis as explained earlier. A look at the table 5.2 .1 shows that over 76 to $80 \%$ of the variability is explained by the models with $9,12,15$ and 18 variables and looking at the table 5.2.2, in the backward elimination process, it is observed that the model with 12 variables (STCR model) shows linear trend for fertilizer Nitrogen (FN) , quadratic trend for FN and FP and interaction (FP X SP) as significant variables. In case of 15 and 18, the resulting significant variables are similar. Other effects found significantly contributing are soil Phosphorus (SP), Soil Potash (FK) and quadratic effect of soil Phosphorus (SP) and the interactions between FN and FK. The Optimum value calculated from the model with 12 variables gives $\mathrm{FN}=111 \mathrm{~kg} /$ ha and $\mathrm{FP}=41 \mathrm{~kg} / \mathrm{ha}$. The optimum value for FK is not derivable.

An interesting aspect is that by adding replication as a variable in the model with 15 variables, the $\mathrm{R}^{2}$ value has increased to $83 \%$. The replication effect is significant. Moreover the soil variables SN, SP and SK are also significant, thereby showing (table 5.2.3) the creation of fertility gradient (one of the feature of STCR project).

When the data was subjected to analysis by Response surface methodology it is observed that the stationary point is a saddle point (as discussed earlier). Therefore exploration of the response surface in the vicinity of the stationary point was attempted. In this case the variables SN, SP and SK have been taken as covariates. Optimum values have been calculated by taking into consideration the mean values of SN, SP and SK. In table 5.7, optimum fertilizer doses obtained by Targeted yield approach and Response surface approach have been compared. Maximum response achievable by Response surface methodology has been taken as Targeted yield for the crops at all the centres. This has been done to check the reliability of the Optimum doses calculated by the Targeted yield approach. From this table it is observed that for this experiment, a maximum response of $15.12 \mathrm{q} \mathrm{ha}^{-1}$ is achievable by taking FN as $100 \mathrm{~kg} \mathrm{ha}^{-1}$, FP as $41 \mathrm{~kg} \mathrm{ha}^{-1}$ and FK as $14 \mathrm{~kg} \mathrm{ha}^{-1}$ respectively. The corresponding optimum values by Targeted yield approach are $\mathrm{FN}=106, \mathrm{FP}=79$ and $\mathrm{FK}=57 \mathrm{~kg} \mathrm{ha}{ }^{-1}$. These optimal values obtained by both the methods i.e. response surface and Targeted yield equation are moderately similar for FN but fairly different for FP and FK. The reason for this may be that in the reported data it is not mentioned whether the values of soil FP and FK are actual values of Phosphorus and Potash or they are in the form of $\mathrm{P}_{2} \mathrm{O}_{5}$ and $\mathrm{K}_{2} \mathrm{O}$.
(2) Another experiment which have been considered for this centre is an experiment on Groundnut conducted in the year 1997-98 in the Rabi season.
The fertilizer doses are $0,15,30,60 \mathrm{~kg} /$ ha of Nitrogen; $0,30,60 \mathrm{~kg} / \mathrm{ha}$ of Phosphorus and $0,30,60 \mathrm{~kg} / \mathrm{ha}$ of Potassium. There were in all 30 treatments in each strip consisting of 26 fertilizer treatment combination and 4 controls
The experiment was subjected to multiple regression analysis as explained earlier. A look at the table 5.2 .6 shows that over 86 to $97 \%$ of the variability is explained by the models with $9,12,15$ and 18 variables and looking at the table 5.2.7, in the backward elimination process, it is observed that in the model with 9 variables, the effects found significant were FN, FP, FK, $\mathrm{FN}^{2}$ and interaction $\mathrm{FN} \times \mathrm{FP}\left(\mathrm{R}^{2}=85 \%\right)$. For 12 variables (STCR model), the variables $\mathrm{FN}, \mathrm{FN}^{2}$, SP and interactions $\mathrm{FN} \times$ SN, FP $\times$ SP, and $\mathrm{FK} \times$ SK are significant $\left(\mathrm{R}^{2}=94.88 \%\right)$ In case of 15 and 18 , the resulting significant variables are similar $\left(\mathrm{R}^{2}=95 \%\right)$ i.e the quadratic terms of FN, FP and FK are significant, excepting the fact that with 18 variables, the interactions FN $\times$ FP, FN $\times$ FK and FP $\times$ FK are also significant. The signs of the different effects do not follow the desired ' + , - , -' form and even if some of the optimal values which could be derived, the process is very cumbersome. However a test of Normal Probability plot below shows that the data are normally distributed
Normal P-P Plot of Regression

Scatterplot
Dependent Variable: YIELD


Regression Studentized Residual

The scatter plot also shows fairy uniform pattern of spread although some outliers are observed which goes beyond the (+2,-2) interval. Here also it is observed (table 5.2.8) that by adding replication as a variable in the all the models, there is an increase in $\mathrm{R}^{2}$ values. More over the value of $\mathrm{R}^{2}$ is further increased by using the variables $\mathrm{FN} \times \mathrm{FP}$, $\mathrm{FN} \times \mathrm{FK}$ and $\mathrm{FP} \times \mathrm{FK}$ in place of $\mathrm{SN}^{2} \mathrm{SP}^{2}$ and $\mathrm{SK}^{2}$ respectively for the model (table 5.2.11)with15 and16(with replication) variables. The replication effect is significant in all the models (models with 10, 13, 16 and 19 variables). Thereby showing the creation of fertility gradient (one of the feature of STCR project). The soil variables SN, SP and the interactions $\mathrm{FN} \times$ SN and $\mathrm{FP} \times$ SP are significant. Again the optimal doses are derivable but one has to solve a number of equations

When the data was subjected to analysis by Response surface methodology it is observed that the stationary point is a saddle point (as discussed earlier). Therefore exploration of the response surface in the vicinity of the stationary point was attempted. In this case the variables SN, SP and SK have been taken as covariates. Optimum values have been calculated by taking into consideration the mean values of SN, SP and SK. In table 5.7, optimum fertilizer doses obtained by Targeted yield approach and Response surface approach have been compared. Maximum response achievable by Response surface methodology has been taken as Targeted yield for the crops at all the centres. This has been done to check the reliability of the Optimum doses calculated by the Targeted yield approach. From this table it is observed that for this experiment, a maximum response of $20.48 \mathrm{q} \mathrm{ha}^{-1}$ is achievable by taking FN as $29 \mathrm{~kg} \mathrm{ha}^{-1}$, FP as $39 \mathrm{~kg} \mathrm{ha}^{-1}$ and FK as $35 \mathrm{~kg} \mathrm{ha}^{-1}$ respectively by Response surface methodology. The corresponding optimum values by Targeted yield approach are $\mathrm{FN}=28, \mathrm{FP}=47$ and $\mathrm{FK}=83 \mathrm{~kg} \mathrm{ha}^{-1}$. These optimal values obtained by both the methods i.e. response surface and Targeted yield equation are moderately similar for FN and FP but fairly different for FK.
(3) The third experiment at this centre chosen was on Rice in the Rabi season conducted at the centre Maruteru. This experiment has been investigated for other aspects and discussed in detail in Chapter-III.

The fertilizer doses are $0,50,100,150 \mathrm{~kg} / \mathrm{ha}$ of Nitrogen; $0,40,80 \mathrm{~kg} / \mathrm{ha}$ of Phosphorus and $0,40,80 \mathrm{~kg} / \mathrm{ha}$ of Potassium. There were in all 30 treatments in each strip consisting of 27 fertilizer treatment combination and 3 controls
Out of all models tested for regression, most of them had variables like $\mathrm{FP}, \mathrm{FK}, \mathrm{FN}^{2}$, $\mathrm{FP}^{2}, \mathrm{FK}^{2}$ and interactions $\mathrm{FN} \times \mathrm{SN}, \mathrm{FP} \times$ SP etc significant(Tables 5.2.12 to 5.2.15). The variable FN was found significant only for the models with $9,10,12,15,18$ and 19 variables. $\mathrm{R}^{2}$ value for all the models was around $90 \%$. The replication effect was found significant in all the four models i.e. with variables $10,13,16$ and 19 . This shows that fertility gradient has been created. Optimal values are derivable from the models with 18,10, 13,16 and 19 variables.

## Regression Diagnostics

To apply regression diagnostics, first of all we observe the scatter plot between Yield and Standardized residuals along with the Normal probability plot which are shown below.

# Scatter plot and Normal probability plot of Maruteru Rabi Rice 1994 Experiment conducted by STCR (Total Number of Observations=120) 



Fig: 5.1(a) Scatter plot of Yield Vs Standardized Residual
No. of Observations: 120(all)
Note: observation number 19 on the far left and observation numbers, 21,24, 26 and 40 on extreme right are outside -2 to +2 range. These are outliers.

Normal P-P Plot of Regression Standardized Residual


Fig: 5.1(b) The normal P-P shown above does not have much irregularity or breaks
It is observed from the scatter plot of Standardized residuals(6.1a) above that the observations numbers $19,21,24,26$ and 40 are lying beyond the ( $+2,-2$ ) range and hence they seem to be outliers. Therefore we delete these observations one by one and see if there is any change in the pattern.

## Normal P-P Plot of Regression Standardized Residual

## Deleted observation 19

Normal P-P Plot of Regression Standardized Residual
Dependent Variable: YIELD


Deleted observation 24
Normal P-P Plot of Regression Standardized Residual


Observed Cum Prob

Observed Cum Prob

Deleted observation 40
Normal P-P Plot of Regression Standardized Residual


Deleted observation 21
Normal P-P Plot of Regression Standardized Residual Dependent Variable: YIELD


Deleted observation 26
Normal P-P Plot of Regression Standardized Residual


Observed Cum Prob

Deleted observations 19,21,24,26 \&40
Normal P-P Plot of Regression Standardized Residual


Fig: 5.2 Changes in Normal probability plots after deletion of observations

Plot of Standardized Residuals and Yield for different deleted observations

## Deleted Observation number 19



Deleted Observation number24


Deleted Observation number 40


Deleted Observation number21


## Deleted Observation number26



Deleted Observation numbers 19,21,24,26,40
Scatterplot


The above plots of standardized residual shows no change in the status of outliers. Only it is observed that Observation number 19 is influenced by other observations as in each deletion it moves further out of range. Also it is observed that observation
number 21 comes within the range of $(+2,-2)$ standardized residual, when observation 19 is deleted.

It is also observed that all these outliers, except observation number 40, lies in the Strip 0X on which no fertilizer was added in the previous season and comparatively higher yield is observed in plot numbers $21\left(72.28 \mathrm{Qh}^{-1}\right), 24\left(70.89 \mathrm{Q} \mathrm{h}^{-1}\right), 26(67.42$ $\mathrm{Qh}^{-1}$ ) and $40\left(56.30 \mathrm{Qh}^{-1}\right)$ in Strip 0X. By putting average yield values from corresponding treatments in other strips did not alter the status of the plots or of analysis. Although we cannot pin point the outlier, but it seems that there is some problem in the recording of actual data, which is generally one of the problems of outlier detection.

Our next step is to apply various regression diagnostics and calculate the parameters of influence statistics like Hat Diagonal, COVRATIO, DFFITS, DFBETAS ${ }_{j}$, and Cook's D. Critical values of these influence statistics have been calculated and presented in the table 5(a) given overleaf. A summary of influence statistics is given in table 5(b). From the table 5(b) we see that besides the outliers mentioned above, there are a few more outliers such as $10,88,93,106,108,111$ and 115 but they are not as prominent as the earlier observations $19,21,24,26$ and 40 . From table 5(a) which gives influential Statistics with critical values, it is observed that under DFFITS column, the observation number 19 has a negative sign always whenever an observation is deleted. From the sign on the DFFITS measures, we can conclude that by adding observation 19 decreases the magnitude of $\hat{y}$. From the original output statistics for all observations (not shown here because of space) it has been observed that for observation number 19, the individual DFFITS(DFBETAS) which show negative sign are Intercept, $F N, \mathrm{FP}^{2}, \mathrm{FK}^{2}, \mathrm{SN}, \mathrm{FN} \times \mathrm{SN}, \mathrm{FP} \times \mathrm{SP}$ and $\mathrm{FK} \times$ SK and thereby their magnitude of regression coefficient are decreased. This is also evident from the table, which gives final regression equations after backward elimination. It is seen that the regression coefficients for $\mathrm{FP}^{2}$, SN and $\mathrm{FN} \times$ SN have decreased. Also by deletion of observation 19 , the $\mathrm{R}^{2}$ value increases from0.9055 to 0.9145 .

Similarly by deleting observations 26 and 40 , the $\mathrm{R}^{2}$ value of the resulting equation increases in both the cases from 0.9055 to 0.9129 and 0.9125 respectively.

When these three observations are deleted, the $\mathrm{R}^{2}$ value increases to 0.9240 and the number of significant regression equations, after backward elimination, increases to 9 from 8. Therefore, it is felt that the three observations 19, 26 and 40 are superfluous and should be omitted.

The process of regression diagnostics should be attempted with great caution as an observation which looks innocent may be 'masked' by another. For simple experiments with less observation one can go ahead with Regression diagnostics but in experiments of Soil test crop response project, which has more than 100 observations for each experiment, one must be cautious in dealing with data.


Table: 5(b) Summary of influential statistics to detect outliers
Maruteru Rabi Rice 1994

| Observation Number <br> Critical values $\rightarrow$ | Studentized Residual$(> \pm 2)$ | HAT DIAG H$(>0.1250)$ | COVRATIO$(1.375-0.625)$ | DFFITS$(> \pm 0.7071)$ | DFBETAS ( > 0.1826) |  |  |  | Cook's D$(>0.0333)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | INTER <br> CEPT | FN | FP | FK |  |
|  |  |  |  |  |  |  |  |  |  |
| 10 | - | $\sqrt{ }$ | - | + $\sqrt{ }$ | - | $\sqrt{ }$ | $\sqrt{ }$ | - | $\checkmark$ |
| 19 | $\checkmark$ | $\checkmark$ | $\checkmark$ | - $\sqrt{ }$ | - | - | $\checkmark$ | - | $\checkmark$ |
| 21 | $\checkmark$ | $\checkmark$ | - | $+\sqrt{ }$ | - | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| 24 | $\checkmark$ | $\checkmark$ | - | $+\sqrt{ }$ | - | $\checkmark$ | $\checkmark$ | - | $\checkmark$ |
| 26 | $\checkmark$ | $\checkmark$ | $\sqrt{ }$ | $+\sqrt{ }$ | - | - | $\checkmark$ | $\sqrt{ }$ | $\checkmark$ |
| 40 | $\checkmark$ | - | $\checkmark$ | $+\sqrt{ }$ | $\sqrt{ }$ | $\checkmark$ | $\checkmark$ | $\sqrt{ }$ | $\checkmark$ |
| 88 | - | $\sqrt{ }$ | $\sqrt{ }$ | - $\sqrt{ }$ | $\sqrt{ }$ | $\sqrt{ }$ | - | - | $\checkmark$ |
| 93 | - | $\checkmark$ | - | $+\sqrt{ }$ | - | - | - | - | $\checkmark$ |
| 106 | - | $\checkmark$ | - | $+\sqrt{ }$ | $\sqrt{ }$ | - | - | $\sqrt{ }$ | $\checkmark$ |
| 108 | - | $\checkmark$ | - | + $\sqrt{ }$ | - | - | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| 111 | - | $\checkmark$ | - | - $\sqrt{ }$ | - | $\sqrt{ }$ | $\sqrt{ }$ | - | $\checkmark$ |
| 115 | - | $\checkmark$ | - | - $\sqrt{ }$ | $\sqrt{ }$ | - | - | $\sqrt{ }$ | $\sqrt{ }$ |

Note: ' $\sqrt{ }$ • Represents the values which are greater than the critical values (which are given in parentheses)

-     - • Represents the values which are less than the critical values

Table: 5(c) Final Regression equations after backward elimination

## Maruteru Rice Rabi 1994

Original regression equation ( 120 observations)
$\mathrm{Y}=2755.60889+24.39779 \mathrm{FN}+16.08044 \mathrm{FK}-0.13557 \mathrm{FN}^{2}+0.06341 \mathrm{FP}^{2}-0.10505 \mathrm{FK}^{2}-2.31739$ SK $-0.04118 \mathrm{FN} \times$ FP $+0.05236 \mathrm{FN} \times$ SN $\quad \mathrm{R}^{2}=0.9055$

Regression equation after deleting observation 19

$$
\begin{aligned}
\mathrm{Y}= & 4338.76309+13.97894 \mathrm{FN}+14.83166 \mathrm{FK}-0.14964 \mathrm{FN}^{2}+0.07655 \mathrm{FP}^{2}-0.09463 \mathrm{FK}^{2}- \\
& 5.40397 \mathrm{SN}-2.31602 \mathrm{SK}-0.05312 \mathrm{FN} \times \mathrm{FP}+0.09546 \mathrm{FN} \times \text { SN } \quad \mathrm{R}^{2}=0.9145
\end{aligned}
$$

Regression equation after deleting observation 21
$\mathrm{Y}=2626.09926+27.55086 \mathrm{FN}+16.64638 \mathrm{FK}-0.14974 \mathrm{FN}^{2}-0.11556 \mathrm{FK}^{2}-1.80080 \mathrm{SK}$
$+0.04653 \mathrm{FN} \times$ SN $\quad \mathrm{R}^{2}=0.9013$
Regression equation after deleting observation 24
$\mathrm{Y}=2742.28406+26.74566 \mathrm{FN}+16.32247 \mathrm{FK}-0.13406 \mathrm{FN}^{2}+0.06873 \mathrm{FP}^{2}-0.11096 \mathrm{FK}^{2}-$
2.29138 SK-0.04564 FN $\times$ FP $+0.04529 \mathrm{FN} \times$ SN $\quad R^{2}=0.9069$

Regression equation after deleting observation 26
$\mathrm{Y}=4130.60071+13.86550 \mathrm{FN}+14.31508 \mathrm{FK}-0.15797 \mathrm{FN}^{2}+0.06680 \mathrm{FP}^{2}-0.08650 \mathrm{FK}^{2}-$
5.33959SN-2.70065 SK-0.05014 FN $\times$ FP $+0.09723 \mathrm{FN} \times$ SN $\quad \mathrm{R}^{2}=0.9129$

## Regression equation after deleting observation 40

$\mathrm{Y}=4507.81242+13.30066 \mathrm{FN}+16.99820 \mathrm{FK}-0.14828 \mathrm{FN}^{2}+0.06844 \mathrm{FP}^{2}-0.11071 \mathrm{FK}^{2}-$
5.59125SN-2.70065 SK-0.03776FN $\times$ FP $+0.09486 \mathrm{FN} \times$ SN $\quad \mathrm{R}^{2}=0.9125$

Regression equation after deleting observation all the above 5

## Observations

$$
\begin{array}{r}
\mathrm{Y}=4475.42287+20.79627 \mathrm{FN}+16.99820 \mathrm{FK}-0.15421 \mathrm{FN}^{2}+0.07300 \mathrm{FP}^{2}-0.08936 \mathrm{FK}^{2}- \\
4.93321 \mathrm{SN}-3.20131 \mathrm{SK}-0.05610 \mathrm{FN} \times \mathrm{FP}+0.07761 \mathrm{FN} \times \mathrm{SN}+0.03962 \mathrm{FK} \times \mathrm{SK} \\
\mathrm{R}^{2}=0.9125
\end{array}
$$

## LUDHIANA

An experiment on Wheat crop(variety PBW- 343) conducted at Punjab Agricultural University, Ludhiana in 1997 under the soil test crop response correlation project was take up, as this experiment was different from others, The experiment consisted of 10 treatment combinations of N, P and K selected from a $5 \times 4 \times 3$ factorial experiment. This set of 10 treatments was replicated four times in each of the four strips (as mentioned earlier) in a randomized way. In all there were four strips. Therefore each strip contained a set of 10 treatments, which is repeated four times in the same strip, thereby giving 40 plots or observations.

We analyzed this experiment as follows: The data of individual strips (4 in all) were analyzed separately as Randomized block design with four replications. The error variances of the four experiments were tested by Bartlett's test and were found to be homogeneous. Next a pooled analysis was performed for the four sites as per the following ANOVA:

## Analysis of Variance

| Source | d.f. | sum of sq. | Mean sq. | F | pr $>$ F |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Strips | 3 | 1371.71502 | 457.23834 | 37.63** | <. 0001 |
| Treatment | 9 | 10458.37335 | 1162.04148 | 95.63** | <. 0001 |
| Rep (Strips) | 12 | 393.71485 | 32.80957 | 2.70 * | 0.0032 |
| StripsXTreat. | 27 | 788.29057 | 29.19595 | 2.40* | 0.0008 |
| Error | 108 | 1312.31980 | 12.15111 | ---- |  |
| Total | 159 | 14324.41359 |  |  |  |
| $\mathrm{R}^{2} \quad$ C.V. | Yiel | Mean (Kg./Ha.) | Max.Yield | Kg./На.) |  |
| 0.90836 .65 |  | . 39 | 57.03(treat.no | 10) |  |

In this analysis, the effects of Strips and Treatment were found to be highly significant .while the effect of Replication (Strips) and (Strips * Treatment) were only significant .
As the replications (strips) are significant, then each set of ten treatments can be taken as a different site. In that case, we would have 16 sites ( $4 \times 4$ ) instead of the regular 4 sites (strips). Since the strips are highly significant, it shows that the fertility gradient has been established, which is one of the aims of the STCR experiment.

The method applied at IASRI was adopted for further analysis. The following model is generally used by the STCR project:
$\mathrm{Y}=\mathrm{b}_{0}+\mathrm{b}_{1} \mathrm{FN}+\mathrm{b}_{2} \mathrm{FP}+\mathrm{b}_{3} \mathrm{FK}+\mathrm{b}_{4} \mathrm{FN}^{2}+\mathrm{b}_{5} \mathrm{FP}^{2}+\mathrm{b}_{6} \mathrm{FK}^{2}+\mathrm{b}_{7} \mathrm{SN}+\mathrm{b}_{8} \mathrm{SP}+\mathrm{b}_{9} \mathrm{SK}+$ $+\mathrm{b}_{10} \mathrm{FN} \times \mathrm{SN}+\mathrm{b}_{11} \mathrm{FP} \times \mathrm{SP}+\mathrm{b}_{12} \mathrm{FK} \times \mathrm{SK}+\varepsilon$

Where, $\mathrm{b}_{\mathrm{i}}$ ' s are the regression coefficients, FN, FP and FK are applied fertilizer doses of Nitrogen, Phosphorus and Potash, SN, SP and SK are available soil fertilizers for Nitrogen, Phosphorus and potash respectively. $\varepsilon$ is the random error which is assumed $\sim N\left(0, \sigma^{2}\right)$

Since the numbers of distinct design points are only 10 in this case, the Response Surface for above model could not be fitted. Thus as per our assumption, we have an experiment with a set of 10 treatment combinations of N, P and K conducted at 16 sites. Therefore, considering the number of design points available, a multiple regression equation (backward elimination) was fitted to the whole data consisting of 160 observations taking 'yield' as dependent variable as per the following model:

$$
\begin{equation*}
\mathrm{Y}=\mathrm{b}_{0}+\mathrm{b}_{1} \mathrm{FN}+\mathrm{b}_{2} \mathrm{FP}+\mathrm{b}_{3} \mathrm{FK}+\mathrm{b}_{4} \mathrm{FN}^{2}+\mathrm{b}_{5} \mathrm{FP}^{2}+\mathrm{b}_{6} \mathrm{FK}^{2}+\mathrm{b}_{7}(\mathrm{FN} \times \mathrm{FP})+\varepsilon \ldots \tag{1}
\end{equation*}
$$

Where, FN, FP, FK are the applied fertilizer doses of N, P and K, $\mathrm{b}_{\mathrm{i}}$ 's are the regression coefficients and $\varepsilon$ the random error assumed $\sim N\left(0, \sigma^{2}\right)$

The effects of ( $\mathrm{FN} \times \mathrm{FK}$ ) and ( $\mathrm{FP} \times \mathrm{FK}$ ) were omitted from the model as these were found to be combinations of the other effects. The $R^{2}$ - value was found to be $74 \%$. Although the $R^{2}$ value was high but the significant effects were, only N and $\mathrm{N}^{2}$.
A number of other models have been tried like with parameters,[ $\mathrm{N}, \mathrm{P}, \mathrm{K}, .(\mathrm{N} \times \mathrm{P})$ and $\left.\mathrm{N}^{2}\right],[$ $N, P,(N \times P)],\left[N, P, N^{2}\right]$ etc. But $R^{2}$ value is of the order of $74 \%$ only when $N^{2}$ is there in the model. Moreover the linear effect of K is also not significant Therefore it appears that the contribution of K is negligible and therefore could not be estimated. The final model selected was:

$$
\begin{equation*}
\mathrm{Y}=\mathrm{b}_{0}+\mathrm{b}_{1} \mathrm{FN}+\mathrm{b}_{2} \mathrm{FP}+\mathrm{b}_{3} \mathrm{FN}^{2}+\mathrm{b}_{4} \mathrm{FN} \times \mathrm{FP}+\varepsilon \tag{2}
\end{equation*}
$$

Next taking each $b_{i}$ as dependent variable and the set of available soil test values of Nitrogen and Phosphorus (designated as SN and SP respectively) as independent variables a multiple regression was fitted using the following models:

$$
\begin{aligned}
& b_{1}=a_{10}+a_{11} S N+a_{12} S N^{2}+e_{1} \\
& b_{2}=a_{20}+a_{21} S P+a_{22} S P^{2}+e_{2} \\
& b_{3}=a_{30}+a_{31} S N+a_{32} S N^{2}+e_{3} \\
& b_{4}=a_{40}+a_{41} S N+a_{42} S N^{2}+a_{43} S P+a_{44} S P^{2}+e_{4}
\end{aligned}
$$

These values of $b_{i}$ 's were substituted in the original regression equation (1).
The new equation takes the following form:
$\mathrm{Y}=\mathrm{b}_{0}+\left(\mathrm{a}_{10}+\mathrm{a}_{11} \mathrm{SN}+\mathrm{a}_{12} \mathrm{SN}^{2}\right) \mathrm{FN}+\left(\mathrm{a}_{20}+\mathrm{a}_{21} \mathrm{SP}+\mathrm{a}_{22} \mathrm{SP}^{2}\right) \mathrm{FP}+\left(\mathrm{a}_{30}+\mathrm{a}_{31} \mathrm{SN}+\mathrm{a}_{32} \mathrm{SN}^{2}\right) \mathrm{FN}^{2}$
$+\left(\mathrm{a}_{40}+\mathrm{a}_{41} \mathrm{SN}+\mathrm{a}_{42} \mathrm{SN}^{2}+\mathrm{a}_{43} \mathrm{SP}+\mathrm{a}_{44} \mathrm{SP}^{2}\right) \mathrm{FN} \times F P+\varepsilon^{\prime}$
By substituting the soil values of SN and SP of a particular site in the above equation and after simplification, the equation reduces to the following form:

$$
\begin{equation*}
\mathrm{Y}=\mathrm{c}_{0}+\mathrm{c}_{1} \mathrm{FN}+\mathrm{c}_{2} \mathrm{FP}+\mathrm{c}_{3} \mathrm{FN}^{2}+\mathrm{c}_{4} \mathrm{FN} \times \mathrm{FP}+\varepsilon \tag{4}
\end{equation*}
$$

Then by differentiating the above equation with respect to FN and FP respectively and equating resulting equations to zero, the optimal values of N and P can be obtained for that particular site.

Also a Response Surface was fitted to the data by taking Soil $\mathrm{N}_{2} \mathrm{P}_{2} \mathrm{O}_{5}$ and $\mathrm{K}_{2} \mathrm{O}$ and Replication as Co-variates and followed by canonical analysis, to get the optimal values of N and P .

## Results and interpretations

From table L. 1 it can be observed that the response of wheat up to $N_{120}$ over $P_{60} K_{30}$ (28.38), up to $\mathrm{P}_{60}$ over $\mathrm{N}_{120} \mathrm{~K}_{30}$ (2.90) and up to $\mathrm{K}_{30}$ over $\mathrm{N}_{120} \mathrm{P}_{60}(1.90)$ is high. Moreover the response of $N_{120}$ is highest in gradient II, that of $\mathrm{P}_{60}$ is highest in gradient I and that of $\mathrm{K}_{30}$ is highest in gradient III. The optimum dose is in the vicinity of $\mathrm{N}_{120} \mathrm{P}_{60} \mathrm{~K}_{30}$.

The optimum value of the nutrients obtained (Table L.3) by applying multiple regression for the STCR model were $N=134$ and $P=57$ with $R^{2}$ value of $79 \%$ and $N=125, P=24$ with $R^{2}$ value of $81 \%$ when replication was introduced as a variable.

The optimum values of the nutrients obtained by IASRI approach were $\mathrm{N}=121$ and $\mathrm{P}=57$ with $\mathrm{R}^{2}$ value of $62 \%$.

Since it was not possible to fit a complete response surface to the data because of lesser number of distinct design points, as an illustration, 10 more treatment combinations were chosen from the $5 \times 4 \times 3$ combinations and were superimposed in each gradient and replicated twice. So now each gradient contains 20 treatments replicated twice. The covariates taken in this model were SN, SP, SK and Replication. The optimum values of the nutrients obtained by this method (table L.2) were $\mathrm{N}=115, \mathrm{P}=33$ and $\mathrm{K}=10 \mathrm{~kg} / \mathrm{ha}$.

So it is suggested that this particular experiment should have been undertaken with at least 20 distinct treatment combinations replicated twice in each gradient instead of 10 treatments, replicating four times in each gradient, since resources were available.

From the above it can be concluded that each experiment should be conducted by choosing a proper set of treatment combinations and sufficient number of design points so that a complete response surface could be fitted.

Table L.1: Response of Wheat (Q/ha.) to N,P,K at graded levels of application under different gradients (Ludhiana 1997)

| Gradient | Response to N Over $\mathrm{P}_{60} \mathrm{~K}_{30}$ <br> $\begin{array}{lll}\mathrm{N}_{30} & \mathrm{~N}_{120} & \mathrm{~N}_{160}\end{array}$ |  |  | Response to P Over $\mathrm{N}_{120} \mathrm{~K}_{30}$ $\mathrm{P}_{30} \quad \mathrm{P}_{60} \quad \mathrm{P}_{90}$ |  |  | Response to K Over $\mathrm{N}_{120} \mathrm{P}_{60}$ $\mathrm{K}_{30} \quad \mathrm{~K}_{60}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 19.46 | 29.42 | 30.13 | 4.94 | 4.61 | 4.80 | -0.38 | 0.12 |
| II | 26.88 | 34.61 | 31.49 | -3.51 | 2.69 | 2.13 | 2.31 | -0.88 |
| III | 21.79 | 26.42 | 22.73 | -0.67 | 2.17 | -0.91 | 4.80 | 4.03 |
| IV | 21.28 | 23.07 | 27.07 | -3.30 | -0.99 | -0.49 | 0.87 | -0.25 |
| Overall | 22.35 | 28.38 | 25.36 | -0.63 | 2.90 | 1.38 | 1.90 | 0.76 |

Table L.2: Optimal values of $\mathrm{N}, \mathrm{P}$ and $\mathrm{K}(\mathrm{kg} / \mathrm{ha})$ obtained by fitting of response surface for different gradients (Covariates: Rep, SN, SP and SK)

| Nutrients | Gradients |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | I | II | III | IV | Overall |
| $\mathbf{N}$ | 90 | 128 | 126 | 107 | 115 |
| $\mathbf{P}$ | 22 | 19 | 64 | 56 | 33 |
| $\mathbf{K}$ | 31 | 10 | 55 | 39 | 10 |
| $\mathbf{R}^{\mathbf{2}}$ | 0.87 | 0.91 | 0.86 | 0.83 | 0.79 |
| $\mathbf{C . V}$. | 8.64 | 6.88 | 6.03 | 6.89 | 8.68 |


| Gradients | I | II | III | IV | Overall |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Predicted yield <br> (q ha $\mathbf{- a}^{-1}$ ) at | 47.70 | 55.22 | 61.24 | 54.64 | 54.76 |
| Stationary point <br> (Saddle point) |  |  |  |  |  |

Table L.3: Multiple regression equations and the derived optimal values
Multiple regression equation (backward elimination) for the STCR model is as follows (all effects are significant).

$$
\begin{array}{rlr}
\mathrm{Y}= & -2.9298+0.35988 \mathrm{FN}-0.00153 \mathrm{FN}^{2}+.000863 \mathrm{FNFP} & \\
& +0.40022 \mathrm{SP}-0.00267 \mathrm{SP}^{2}+0.17482 \mathrm{SK}-0.0002969 \mathrm{SK}^{2} & \mathrm{R}^{2}=0.79 \\
& -0.001571 \text { FPSP }
\end{array}
$$

For a particular site with soil test values (kg/ha): $\mathrm{SN}=88, \mathrm{SP}=73.5$ and $\mathrm{SK}=330$
The derived optimal Values of Nutrients (kg/ha): N=134, P=57
Multiple regression equation (backward elimination) for the above STCR model including replication as a variable is as follows (all effects are significant).
$\mathrm{Y}=7.0709+2.7325 \mathrm{REP}+0.3387 \mathrm{FN}-0.00154 \mathrm{FN}^{2}++0.00083 \mathrm{FNFP}+$

$$
\begin{aligned}
& +0.40022 \text { SP }-0.00267 \mathrm{SP}^{2}+0.17482 \mathrm{SK}-0.0002969 \mathrm{SK}^{2} \\
& -0.001571 \mathrm{FPSP}
\end{aligned} \mathrm{R}^{2}=0.81
$$

For a Particular site with Soil Test Values (kg/ha):SN $=75, \mathrm{SP}=66.8$ and $\mathrm{SK}=370$
The derived optimal Values of Nutrients (kg/ha): $\mathrm{N}=125, \mathrm{P}=24$
Multiple regression equation (backward elimination) for the IASRI model is as follows For a Particular site with Soil Test Values (kg/ha):
$\mathrm{SN}=75, \mathrm{SP}=66.8$ and $\mathrm{SK}=370$
$\mathrm{Y}=1.41988++0.24396$ FN +0.51806 FP -0.00428 FNFP

$$
R^{2}=0.62
$$

The derived optimal Values of Nutrients(kg/ha): $\mathrm{N}=121, \mathrm{P}=57$

Table L.4: Estimated ridge of maximum response for yield optimum values
( $\mathrm{kg} \mathrm{ha}^{-1}$ )

| Coded <br> Radius | Estimated <br> Response | Standard <br> Error | FN | FP | FK |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{0 . 0}$ | 52.1999 | 1.6286 | 80.00 | 45.00 | 30.00 |
| $\mathbf{0 . 1}$ | 53.1937 | 1.4823 | 87.81 | 44.06 | 30.18 |
| $\mathbf{0 . 2}$ | 53.9693 | 1.3000 | 95.66 | 43.29 | 30.48 |
| $\mathbf{0 . 3}$ | 54.5299 | 1.0875 | 103.56 | 43.00 | 31.09 |
| $\mathbf{0 . 4}$ | 54.8917 | 0.8670 | 111.28 | 44.74 | 32.52 |
| $\mathbf{0 . 5}$ | 55.1337 | 0.7232 | 117.02 | 50.62 | 34.27 |
| $\mathbf{0 . 6}$ | 55.3587 | 0.6551 | 120.80 | 56.95 | 35.15 |
| $\mathbf{0 . 7}$ | 55.5988 | 0.6126 | 123.83 | 62.70 | 35.63 |
| $\mathbf{0 . 8}$ | 55.8615 | 0.5843 | 126.53 | 68.06 | 35.93 |
| $\mathbf{0 . 9}$ | 56.1493 | 0.5741 | 129.04 | 73.18 | 36.15 |
| $\mathbf{1 . 0}$ | $\mathbf{5 6 . 4 6 3 6}$ | $\mathbf{0 . 5 9 2 8}$ | $\mathbf{1 3 1 . 4 4}$ | $\mathbf{7 8 . 1 4}$ | $\mathbf{3 6 . 3 2}$ |

## KALYANI

At this centre, an experiment on Rape crop, conducted in the year 1998 in the Rabi season has been selected. The fertilizer doses are $0,50,75,100$ and $125 \mathrm{~kg} / \mathrm{ha}$ of Nitrogen, $0,25,50,75$ $\mathrm{kg} / \mathrm{ha}$ of Phosphorus and $0,25,50 \mathrm{~kg} / \mathrm{ha}$ of Potassium. The design used is $5 \times 4 \times 3$ fractional factorial and number of fertilizer treatment combinations are 21 with 7 controls making a total of 28 treatments.
The data was subjected to multiple regression analysis as explained earlier. A look at the table 5.3.1 shows that, excepting the model with 9 variables (only added fertilizer treatments), over $87 \%$ of the variability is explained by the models with 12,15 and 18 variables and looking at the table 5.3.2, in the backward elimination process, it is observed that in all the models, linear and quadratic trend for fertilizer Phosphorus (FP) is prominent. Whereas in table 5.3.3 it is observed that (when replication is used as a variable) even the model with 9 variables (plus replication) the R-square value is more than $86 \%$. Also in the remaining variables, after backward elimination (Table 5.3.4), quadratic trend of Nitrogen is observed. Although, optimal values of Nitrogen and Phosphorus could be derived but the same for Potassium is not possible.
Therefore, the data for the year was subjected to analysis by Response surface methodology. In this case the stationary point is a saddle point, which is neither maximum nor minimum. Therefore exploration of the response surface in the vicinity of the stationary point was attempted. In this case the variables SN, SP and SK have been taken as covariates. Optimum values have been calculated by taking into consideration the mean values of SN, SP and SK. In table 5.7, optimum fertilizer doses obtained by Targeted yield approach and Response surface approach have been compared for all the centres. Maximum response achievable by Response surface methodology has been taken as the Targeted yield for the crops at all the centres. This has been done to check the reliability of the Optimum doses calculated by the Targeted yield approach. For this centre, a look at the table 5.7 shows that for achieving a maximum response of $12.38 \mathrm{q} \mathrm{ha}^{-1}$, the required optimal fertilizer doses of FN, FP and FK are $119 \mathrm{~kg} \mathrm{ha}^{-1}, 47 \mathrm{~kg} \mathrm{ha}^{-1}$ and $34 \mathrm{~kg} \mathrm{ha}^{-1}$ respectively as derived by the Response surface methodology. The corresponding optimum values by Targeted yield approach are $\mathrm{FN}=109, \mathrm{FP}=58$ and $\mathrm{FK}=39 \mathrm{~kg} \mathrm{ha}^{-1}$. This shows that the Targeted yield approach and the Response surface methodology give somewhat similar results.

## COIMBATORE

An experiment on Onion conducted in the year 1998 in the Rabi season has been selected. The fertilizer doses are 0, 30, 60, 90 and $120 \mathrm{~kg} /$ ha of Nitrogen, $0,30,60,90 \mathrm{~kg} / \mathrm{ha}$ of Phosphorus
and $0,30,60 \mathrm{~kg} / \mathrm{ha}$ of Potassium. A fractional factorial design $5 \times 4 \times 3$ was used and number of fertilizer treatment combinations was 20 with 4 controls making a total of 24 treatments.
A look at the table 5.4 .1 (multiple regression) shows that over $80 \%$ of the variability is explained by the models with $9,12,15$ and 18 variables and looking at the table 6.4.2, in the backward elimination process, it is observed that in all the models, linear and quadratic trends for fertilizer Nitrogen (FN) and fertilizer Phosphorus (FP) are significant. Also the interactions $\mathrm{FN} \times \mathrm{SN}$ and $\mathrm{FP} \times$ SP are found to be significant in all the models. Here it is observed in all the models Potassium (FK) has no role to play. From table 5.4.3 it is observed that the use of replication as a variable, the R-square value, as reported earlier, goes than $87 \%$ in all the models. Also after backward elimination, in the remaining variables, (Table 5.4.4), similar trend is observed. Here it is also observed that the derivation of optimal values are only possible for fertilizer Nitrogen and Phosphorus.
In this case also the RSM shows that the stationary point is a saddle point (as discussed earlier). The exploration of the response surface in the vicinity of the stationary point shows that to get a response of $181.34 \mathrm{q} \mathrm{ha}^{-1}$, the optimal values of FN, FP and FK required are 110, 68 and 36 kg ha ${ }^{-1}$ respectively. The corresponding optimum values by Targeted yield approach are FN= 111, $\mathrm{FP}=68$ and $\mathrm{FK}=56 \mathrm{~kg} \mathrm{ha}^{-1}$ for the same achievable target. This gives credibility to the Targeted yield approach as has been verified by the Response surface methodology in the above cases.

## HISAR

At this centre, we have chosen two experiments on Wheat crop. The first one was conducted in the year 1993-94 with variety WH-542 and the second was conducted with variety WH-896. The fertilizer doses for both the years were $0,50,100,150$ and $200 \mathrm{~kg} / \mathrm{ha}$ of Nitrogen, $0,30,60,90$ $\mathrm{kg} / \mathrm{ha}$ of Phosphorus and $0,30,60 \mathrm{~kg} /$ ha of Potassium. A fractional factorial design $5 \times 4 \times 3$ was used and number of fertilizer treatment combinations was 21 with 9 controls making a total of 30 treatments.
After subjecting the data to multiple regression analysis, a look at the table 5.5 .1 for the year 1993-94, shows that over $90 \%$ of the variability is explained by the models with $9,12,15$ and 18 variables and looking at the table 5.5.2, in the backward elimination process, it is observed that in all the models, linear and quadratic trends for fertilizer Nitrogen (FN) and fertilizer Phosphorus (FP), the linear trends of soil variables SN, SP, SK and also the interactions $\mathrm{FN} \times \mathrm{SN}$ and $\mathrm{FP} \times$ SP are found to be significant in all the models. Here we observe that the criteria for deriving optimal fertilizer doses when the law of diminishing returns operates i.e. the coefficients of linear, quadratic and interaction terms should be positive(+), Negative(-), Negative(-) is fulfilled. Therefore the optimal values of Fertilizer Nitrogen and Fertilizer Phosphorus are derivable. From table 5.5.3 it is observed that by inclusion of replication as a variable, R-square value becomes more than $99 \%$ in all the models. Also in the remaining variables, after backward elimination (Table 6.5.4), similar trend is observed. Although, optimal values of Nitrogen and Phosphorus could be derived but the same for Potassium is not possible.
The analysis by Response surface methodology, again, in this case shows the stationary point as a saddle point. In table 5.7, optimum fertilizer doses obtained by Targeted yield approach and Response surface approach have been compared. Maximum response achievable by Response surface methodology has been taken as Targeted yield for the crops at all the centres. From this table 5.6 .7 it is observed that for the year 1993-94, a maximum response of $60.97 \mathrm{q} \mathrm{ha}^{-1}$ is achievable by taking FN as $180 \mathrm{~kg} \mathrm{ha}^{-1}$, FP as $70 \mathrm{~kg} \mathrm{ha}^{-1}$ and FK as $24 \mathrm{~kg} \mathrm{ha}^{-1}$ respectively. The corresponding optimum values by Targeted yield approach are FN= 153, FP= 67 and $\mathrm{FK}=52 \mathrm{~kg} \mathrm{ha}{ }^{-1}$. We find some difference in the two methods here at this centre and most likely reason for this is selection of treatments for maximum response procedure of targeted yield equations. From tables 5.5.6 to 5.5.10, which are the results of the experiment conducted in the year 1995-96, we observe similar trends as mentioned in the 1993-94 experiment and therefore are not discussed separately.

## Chapter- VI

## DATABASE FOR STCR EXPERIMENTS

For the benefit of research workers and the scientists of the STCR project, a preliminary database in MS-ACCESS has been developed at IASRI. The experimental data received from a few co-operating centers, has been fed into the database to check its operation. In future, experimental data to be received from different cooperating centres would be fed into this database which will put all the experiments conducted under the STCR project at a central place. Later we propose to place this in IASRI website so that all the scientists working in the project at different cooperating centres can access it through the WEB. This needs some time, proper infrastructure and mainly the cooperation of all the cooperating centres. Therefore it is proposed that for maintaining a database for STCR experiments, an externally funded project would be launched which will provide proper infrastructure and manpower to develop the database..

For the present database, three tables has been created as ExpInfo (Table containing the information of experiment), ExpData (Containing the information on the data of experiment) and DataNPK (information about the treatment structure).

Screen showing the relation ship between three tables


Here after clicking the queries as indicated by arrow the data about the experiment can be retrieved. Various queries are already designed.


## Searches on various basis can be done. For example:

If we want to search the experiments which are conducted in the year 1995.
This can be searched through database by query "search by year" with dummy data as below


Following output will be generated.


## Search By Crop

Likewise various experiments conducted on specific crop can be searched by running the query "search by crop". Here experiments are searched by crop "Rice" and result is as below


Experimental data regarding various experiments can be searched by crop and season from ExpData table. This gives the following output:

Here we see Experiment Number, Treatment No. Nitrogen Fertilizer doses, Phosphorus Fertilizer doses, Potassium fertilizer doses, Soil available Nitrogen, Phosphorus and Potassium, Grain yield and host of other information about experiments


These data can be subjected to analysis by SAS and SPSS packages directly.
Similarly, various queries can be thought of and can be designed using MS Access as per the need of the user.

TABLES

Table 5.1.1: Parameter estimates along with standard errors for response surface models using different number of variables
Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1998

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error |
| Intercept | 2103.84595 | 50.31420 | -2197.74275 | 682.54206 | -2228.77164 | 5778.99510 | -120.80415 | 5584.17236 |
| fn | 5.35190 | 5.04078 | 9.12115 | 9.90485 | -1.31199 | 10.90774 | -4.19969 | 10.51809 |
| $f \mathrm{p}$ | 9.93661 | 4.36936 | -1.1545 | 3.12698 | -2.03116 | 3.03627 | 2.95264 | 3.20845 |
| fk | 12.71041 | 7.84978 | 8.07315 | 14.94661 | 15.84625 | 18.42116 | 16.08370 | 17.83399 |
| $f \mathrm{n}^{2}$ | 0.06506 | 0.09410 | 0.12940 | 0.02905 | 0.12418 | 0.02851 | -0.00138 | 0.04818 |
| $\mathrm{fp}^{2}$ | -0.06342 | 0.07854 | -0.00200 | 0.02311 | -0.00469 | 0.02267 | -0.11739 | 0.03857 |
| $\mathrm{fk}^{2}$ | -0. 20280 | 0.20907 | -0.16343 | 0.08189 | -0.15483 | 0.07909 | -0.19476 | 0.10092 |
| sn | -----. | ----... | 37.66482 | 6.18995 | 154.23751 | 109.29830 | 113.07796 | 106.94426 |
| sp | ------- | ------ | -45.21108 | 11.48897 | 41.94265 | 47.39644 | 47.26447 | 45.61922 |
| sk |  | ------ | ' -1.00398 | 10.46500 | -191.20187 | 150.72924 | -178.81034 | 144.48752 |
| $\mathrm{sn}^{2}$ | ------- |  | ------ |  | -0.42417 | 0.36195 | -0.28110 | 0.35404 |
| sp ${ }^{2}$ | ------- |  | --.-.-. |  | -1.49387 | 0.83601 | -1.74719 | 0.80724 |
| sk ${ }^{2}$ | ------- |  | ------- |  | 0.98900 | 0.74006 | 0.95555 | 0.70918 |
| fn*sn | ------ | ------ | -0.01090 | 0.06756 | 0.06459 | 0.07500 | 0.06408 | 0.07153 |
| fp*sp | -.-.--- | ------ | 0.39462 | 0.10754 | 0.43401 | 0.10417 | 0.42838 | 0.09918 |
| fk*sk | ------ | ------ | 0.06877 | 0.15285 | -0.02013 | 0.18489 | -0.01339 | 0.17696 |
| fn*fp | 0.15486 | 0.14572 | .-.--- | ------ | ....... | ------ | 0.22044 | 0.07262 |
| fn*fk | 0.09372 | 0.14250 | ------- | ------ | ------- | ------ | 0.10462 | 0.06894 |
| fp*fk | -0.03010 | 0.20390 | ------- | ------ | ------ | -...... | -0.10235 | 0.10011 |
| $\mathrm{R}^{2}$ | 0.9026 |  | 0.9741 |  | 0.9768 |  | 0.9796 |  |

Table: 5.1.2 Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure

## Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1998

| Model | Variable | Parameter <br> Estimates | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 2085.28878 | 45.59517 | 162340991 | 2091.68 | <. 0001 |
|  | fn | 7.46991 | 3.69509 | 317186 | 4.09 | 0.0457 |
|  | $f p$ | 8.32184 | 1.46118 | 2517473 | 32.44 | <. 0001 |
|  | fk | 8.39841 | 2.56110 | 834592 | 10.75 | 0.0014 |
|  | fn2 | 0.15691 | 0.04780 | 836301 | 10.78 | 0.0014 |
|  | $\mathrm{R}^{2}=0.8994$ |  |  |  |  |  |
| I] | Intercept | -2312.94255 | 526.65401 | 399795 | 19.29 | <. 0001 |
|  | fn | 7.53193 | 2.05720 | 277855 | 13.40 | 0.0004 |
|  | fk | 14.52385 | 3.41757 | 374359 | 18.06 | <. 0001 |
|  | fn2 | 0.12715 | 0.02687 | 464091 | 22.39 | <. 0001 |
|  | fk2 | -0.15745 | 0.07928 | 81764 | 3.94 | 0.0497 |
|  | sn | 37.55461 | 4.95891 | 1188813 | 57.35 | <.0001 |
|  | sp | -43.97069 | 8.41526 | 565914 | 27.30 | <. 0001 |
|  | fpsp | 0.35424 | 0.02742 | 3458995 | 166.87 | <. 0001 |
|  | $\mathrm{R}^{2}=0.9739$ |  |  |  |  |  |
| III | Intercept | -2269.16199 | 493.68112 | 413451 | 21.13 | <. 0001 |
|  | fk | 14.11420 | 3.27016 | 364553 | 18.63 | <. 0001 |
|  | fn2 | 0.12518 | 0.02563 | 466919 | 23.86 | <. 0001 |
|  | fk2 | -0.14945 | 0.07656 | 74567 | 3.81 | 0.0536 |
|  | sn | 32.95247 | 3.87453 | 1415549 | 72.33 | <. 0001 |
|  | sp2 | -0.71028 | 0.11962 | 690028 | 35.26 | <.0001 |
|  | fnsn | 0.05285 | 0.01338 | 305391 | 15.61 | 0.0001 |
|  | fpsp | 0.35163 | 0.02672 | 3388720 | 173.16 | <. 0001 |
|  | $\mathrm{R}^{2}=0.9753$ |  |  |  |  | . 0001 |
| IV | Intercept | -2355.90198 | 473.00562 | 445331 | 24.81 | <, 0001 |
|  | $f \mathrm{k}$ | 13.61671 | 3.13346 | 338997 | 18.88 | <. 0001 |
|  | fp2 | -0.10654 | 0.02819 | 256303 | 14.28 | 0.0003 |
|  | fk2 | -0.17727 | 0.07398 | 103086 | 5.74 | 0.0184 |
|  | sn | 29.45527 | 4.58035 | 742387 | 41.36 | <. 0001 |
|  | sp2 | -1.07425 | 0.16016 | 807595 | 44.99 | <. 0001 |
|  | sk2 | 0.09242 | 0.04445 | 77604 | 4.32 | 0.0401 |
|  | fnsn | 0.04962 | 0.01228 | 293299 | 16.34 | 0.0001 |
|  | fpsp | 0.46996 | 0.05672 | 1232296 | 68.65 | <. 0001 |
|  | fnfp | 0.20585 | 0.03538 | 607653 | 33.85 | <, 0001 |
|  | $\mathrm{R}^{2}=0.9778$ |  |  |  |  |  |

Table 5.1.3: Parameter estimates along with standard errors for response surface models using different number of variables (models include replication)

Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1998

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 1641.85488 | 49.74558 | -801.52358 | 1303.62495 | -1371.01740 | 7821.35721 | 1888.00985 | 7516.26217 |
| Replication | 184.79643 | 15.17350 | 130.90781 | 104.24835 | 24.76415 | 151.22083 | 57.96281 | 144.35031 |
| $f \mathrm{f}$ | 5.35190 | 3.22414 | 9.29396 | 9.87707 | -1.51775 | 11.03522 | -4.73317 | 10.64905 |
| $f p$ | 9.93661 | 2.79469 | -2.22480 | 3.23231 | -2.18441 | 3.19205 | 2.63189 | 3.32052 |
| $f \mathrm{k}$ | 12.71041 | 5.02081 | 5.94472 | 14.99933 | 16.58612 | 19.05850 | 17.88745 | 18.46956 |
| $f \mathrm{n}^{2}$ | 0.06506 | 0.06018 | 0.13024 | 0.02897 | 0.12374 | 0.02878 | -0.00372 | 0.04875 |
| $\mathrm{fp}^{2}$ | -0.06342 | 0.05023 | 0.00343 | 0.02345 | -0.00402 | 0.02314 | -0.11654 | 0.03881 |
| $f \mathrm{k}^{2}$ | -0.20280 | 0.13372 | -0.15326 | 0.08206 | -0.15347 | 0.07993 | -0.19076 | 0.10187 |
| sn |  | --.-----. | 31.15851 | 8.05850 | 155.11555 | 109.98731 | 115.28458 | 107.57028 |
| sp |  | -------- | -50.04361 | 12.08477 | 41.54672 | 47.69983 | 46.24783 | 45.89623 |
| sk | ---------- | --------- | -7.67322 | 11.70850 | -208.26740 | 183.87939 | -219.03171 | 176.35218 |
| sn ${ }^{2}$ | ---------- | ----- | ------.--- |  | -0.42826 | 0.36465 | -0.29107 | 0.35651 |
| sp ${ }^{2}$ |  |  | ---------- | -------- | -1.50964 | 0.84578 | -1.78393 | 0.81605 |
| sk ${ }^{2}$ |  | -------- |  |  | 1.06462 | 0.87549 | 1.13409 | 0.83976 |
| $f n^{*}$ sn |  |  |  |  |  | -------- | 0.06853 | 0.07270 |
| fp*sp |  |  |  |  |  |  | 0.43902 | 0.10309 |
| fk*sk | --------- | -------- | ---------- | --------- |  | ---.-.-. - | -0.02884 | 0.18188 |
| $f n^{* f p}$ | 0.15486 | 0.09321 | -0.00943 | 0.06738 | 0.06646 | 0.07623 | 0.22274 | 0.07318 |
| fn*fk | 0.09372 | 0.09114 | 0.42204 | 0.10943 | 0.43856 | 0.10832 | 0.10599 | 0.06933 |
| fp*fk | -0.03010 | 0.13041 | 0.09160 | 0.15349 | -0.02658 | 0.18996 | -0.10519 | 0.10081 |
| $\mathrm{R}^{2}$ | 0.9606 |  | 0.9745 |  | 0.9768 |  | 0.9796 |  |

Table: 5.1.4 Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure

Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1998

| Model. | Variable | Parameter <br> Estimates | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Intercept | 1647.97757 | 49.66344 | 35623009 | 1101.11 | <. 0001 |
|  | rep | 184.79643 | 15.20151 | 4780961 | 147.78 | <. 0001 |
|  | fn | 7.79025 | 2.39115 | 343393 | 10.61 | 0.0015 |
|  | $f p$ | 6.71565 | 1.24459 | 941945 | 29.12 | <.0001 |
|  | $f \mathrm{f}$ | 7.91442 | 1.67152 | 725297 | 22.42 | <. 0001 |
|  | fn2 | 0.10403 | 0.04083 | 210068 | 6.49 | 0.0123 |
|  | fnfp | 0.07228 | 0.03653 | 126646 | 3.91 | 0.0500 |
|  | $\mathrm{R}^{2}=0.9588$ |  |  |  |  |  |
| II | Intercept | -2152.40417 | 524.51382 | 348047 | 16.84 | <. 0001 |
|  | $f$ f | 7.81062 | 2.02012 | 308973 | 14.95 | 0.0002 |
|  | fn2 | 0.12623 | 0.02671 | 461499 | 22.33 | <. 0001 |
|  | fk2 | -0.15487 | 0.07806 | 81361 | 3.94 | 0.0499 |
|  | sn | 36.62775 | 4.94327 | 1134742 | 54.90 | <. 0001 |
|  | $s p$ | -44.84017 | 8.41424 | 586961 | 28.40 | <. 0001 |
|  | fpsp | 0.34829 | 0.02755 | 3303785 | 159.85 | <. 0001 |
|  | fksk | 0.14491 | 0.03377 | 380576 | 18.41 | <. 0001 |
|  | $\mathrm{R}^{2}=0.9740$ |  |  |  |  |  |
| HII | Intercept | -2269.16199 | 493.68112 | 413451 | 21.13 | <. 0001 |
|  | fk | 14.11420 | 3.27016 | 364553 | 18.63 | <. 0001 |
|  | fn2 | 0.12518 | 0.02563 | 466919 | 23.86 | <. 0001 |
|  | fk2 | -0.14945 | 0.07656 | 74567 | 3.81 | 0.0536 |
|  | sn | 32.95247 | 3.87453 | 1415549 | 72.33 | . $<.0001$ |
|  | sp2 | -0.71028 | 0.11962 | 690028 | 35.26 | <. 0001 |
|  | fnsn | 0.05285 | 0.01338 | 305391 | 15.61 | 0.0001 |
|  | fpsp | 0.35163 | 0.02672 | 3388720 | 173.16 | $<.000$ |
|  | $\mathrm{R}^{2}=0.9753$ |  |  |  |  |  |
| IV | Intercept | -2355.90198 | 473.00562 | 445331 | 24.81 | <. 0001 |
|  | $f \mathrm{k}$ | 13.61671 | 3.13346 | 338997 | 18.88 | <. 0001 |
|  | fp2 | -0.10654 | 0.02819 | 256303 | 14.28 | 0.0003 |
|  | fk2 | -0.17727 | 0.07398 | 103086 | 5.74 | 0.0184 |
|  | sn | 29.45527 | 4.58035 | 742387 | 41.36 | <. 0001 |
|  | sp2 | -1.07425 | 0.16016 | 807595 | 44.99 | <. 0001 |
|  | sk2 | 0.09242 | 0.04445 | 77604 | 4.32 | 0.0401 |
|  | fnsn | 0.04962 | 0.01228 | 293299 | 16.34 | 0.0001 |
|  | fpsp | 0.46996 | 0.05672 | 1232296 | 68.65 | <. 0001 |
|  | fnfp | 0.20585 | 0.03538 | 607653 | 33.85 | <.0001 |
|  | $\mathrm{R}^{2}=0.9778$ |  |  |  |  |  |

## Table 5.1.5 : Estimated ridge of maximum yield

## Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1998

Average STV* of the Site: $\mathrm{SN}=147.87 \mathrm{Kg}$; SP $=\mathbf{2 6} .72 \mathrm{Kg} ; \mathrm{SK}=\mathbf{9 7 . 8 3 K g}$

| Coded Estimated |  | Standard | Uncoded Factor Values |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Radi | us yield | Error | FN | FP | FK |
| 0.0 | 3143.606330 | 66.562771 | 37.500000 | 40.000000 | 20.000000 |
| 0.1 | 3225.819399 | 66.115593 | 40.702312 | 41.970421 | 20.335319 |
| 0.2 | 3310.949111 | 65.437225 | 43.931705 | 43.898631 | 20.658488 |
| 0.3 | 3399.007714 | 64.582448 | 47.182735 | 45.792379 | 20.971542 |
| 0.4 | 3490.004610 | 63.676834 | 50.451305 | 47.657658 | 21.276090 |
| 0.5 | 3583.947126 | 62.927154 | 53.734277 | 49.499166 | 21.573415 |
| 0.6 | 3680.841058 | 62.627026 | 57.029208 | 51.320631 | 21.864556 |
| 0.7 | 3780.691048 | 63.148020 | 60.334175 | 53.125050 | 22.150364 |
| 0.8 | 3883.500859 | 64.904319 | 63.647640 | 54.914856 | 22.431537 |
| 0.9 | 3989.273568 | 68.288497 | 66.968362 | 56.692042 | 22.708658 |
| 1.0 | 4098.011721 | 73.599067 | 70.295330 | 58.458258 | 22.982215 |

Table 5.1.6 : Parameter estimates along with standard errors for response surface models using different number of variables
Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1999

| Models |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error |
| Intercept | 2398.64608 | 51.76926 | -963.27973 | 374.87570 | -3307.97975 | 4745.99114 | -2847.45544 | 4745.13883 |
| fn | 7.29797 | 5.18656 | -19.60467 | 9.61552 | -22.41375 | 25.62646 | -26.12402 | 25.64255 |
| fp | 8.59660 | 4.49572 | 8.83645 | 2.33153 | 5.97360 | 4.06860 | 6.70185 | 4.09250 |
| fk | 11.68171 | 8.07679 | 10.08234 | 6.43459 | -5.19061 | 13.17134 | -1.10061 | 13.30775 |
| $\mathrm{fn}^{2}$ | 0.11731 | 0.09682 | 0.08843 | 0.02920 | 0.09656 | 0.03822 | 0.06852 | 0.04629 |
| $f p^{2}$ | 0.00854 | 0.08081 | 0.01643 | 0.01994 | 0.00750 | 0.02219 | -0.00111 | 0.03185 |
| $\mathrm{fk}^{2}$ | -0.07928 | 0.21511 | -0.12080 | 0.06445 | -0.17180 | 0.07242 | -0.08307 | 0.08689 |
| sn | ------- | ------- | 15.06504 | 3.32886 | 18.69820 | 71.99401 | 13.69406 | 71.97483 |
| sp | -------- | -------- | 1.70873 | 6.47478 | 22.33281 | 23.19912 | 23.13348 | 23.22677 |
| sk | --------- | -------- | 11.10649 | 2.92624 | 46.33871 | 24.90950 | 43.32657 | 24.91027 |
| $\mathrm{sn}^{2}$ | -------- | -------- | ------- | ------- | -0.02062 | 0.24898 | 0.00010599 | 0.24909 |
| sp ${ }^{2}$ | ------- | -------- | -------- | ------- | -0.52716 | 0.44566 | -0.55454 | 0.44688 |
| sk ${ }^{2}$ | -------- | -------- | --------- | -------- | -0.14055 | 0.11214 | -0.12834 | 0.11223 |
| $f n^{*}$ n | 0.02830 | 0.14994 | -------- | -------- | 0.16903 | 0.17573 | 0.18084 | 0.17556 |
| $f p^{*}$ sp | 0.03611 | 0.14662 | ------- | ------- | 0.09758 | 0.15212 | 0.09522 | 0.15258 |
| fk*sk | -0.08620 | 0.20979 | -------- | -------- | 0.08274 | 0.12577 | 0.07241 | 0.12575 |
| $f n^{*} \mathrm{fp}$ | -------- | -------- | 0.15270 | 0.06626 | -------- | -------- | 0.06622 | 0.04916 |
| $f{ }^{*}$ * f | -------- |  | -0.05684 | 0.07151 | -------- | -------- | -0.01710 | 0.04903 |
| fp*fk | ------- | ---- | -0.04878 | 0.06334 | ------ | -------- | -0.10853 | 0.06921 |
| $\mathrm{R}^{2}$ | 0.8876 |  | 0.9876 |  | 0.9887 |  | 0.9891 |  |

Table 5.1.7 Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure

Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1999

| Model | Variable | Parameter <br> Estimate | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 2404.76465 | 46.31781 | 215894182 | 2695.56 | <. 0001 |
|  | fn | 8.90327 | 3.75365 | 450592 | 5.63 | 0.0195 |
|  | fp | 8.75776 | 1.48434 | 2788125 | 34.81 | <.0001 |
|  | fk | 6.03265 | 2.60169 | 430622 | 5.38 | 0.0223 |
|  | $\mathrm{fn}^{2}$ | 0.12365 | 0.04856 | 519289 | 6.48 | 0.0123 |
|  | $\mathrm{R}^{2}=0.8868$ |  |  |  |  |  |
| II | Intercept | -1070.63946 | 250.21834 | 169815 | 18.31 | <. 0001 |
|  | $f$ | -13.86882 | 7.52388 | 31515 | 3.40 | 0.0682 |
|  | $f \mathrm{p}$ | 8.11463 | 0.50591 | 2386275 | 257.27 | <.0001 |
|  | $f \mathrm{f}$ | 5.79270 | 2.39548 | 54238 | 5.85 | 0.0174 |
|  | $f n^{2}$ | 0.10252 | 0.02639 | 140011 | 15.10 | 0.0002 |
|  | $\mathrm{fk}^{2}$ | -0.14399 | 0.05303 | 68372 | 7.37 | 0.0078 |
|  | sn | 17.10685 | 2.49832 | 434881 | 46.89 | <.0001 |
|  | sk | 9.59817 | 1.77729 | 270513 | 29.17 | <.0001 |
|  | fnxsn | 0.10947 | 0.05150 | 41916 | 4.52 | 0.0359 |
|  | $\mathrm{R}^{2}=0.9874$ |  |  |  |  |  |
| III | Intercept | -2693.94301 | 575.05815 | 193248 | 21.95 | $<.0001$ |
|  | $f$ f | -17.75041 | 8.76483 | 36115 | 4.10 | 0.0455 |
|  | $\mathrm{fn}^{2}$ | 0.09830 | 0.02660 | 120280 | 13.66 | 0.0004 |
|  | $f{ }^{2}$ | -0.08978 | 0.03369 | 62531 | 7.10 | 0.0090 |
|  | sn | 11.95563 | 2.96093 | 143566 | 16.30 | 0.0001 |
|  | sp | 49.47431 | 12.54512 | 136953 | 15.55 | 0.0001 |
|  | sk | 36.86771 | 12.07854 | 82040 | 9.32 | 0.0029 |
|  | $\mathrm{sp}^{2}$ | -1.07390 | 0.22653 | 197905 | 22.47 | <. 0001 |
|  | sk ${ }^{2}$ | -0.08422 | 0.05037 | 24614 | 2.80 | 0.0976 |
|  | fnxsn | 0.14181 | 0.06054 | 48311 | 5.49 | 0.0211 |
|  | fpxsp | 0.30112 | 0.03378 | 699559 | 79.44 | <. 0001 |
|  | $\mathrm{R}^{2}=0.9883$ |  |  |  |  |  |
| IV | Intercept | -2433.31741 | 473.60883 | 227601 | 26.40 | <. 0001 |
|  | fn | -21.41012 | 7.93224 | 62815 | 7.29 | 0.0082 |
|  | $f \mathrm{p}$ | 8.07323 | 0.67617 | 1229119 | 142.55 | <. 0001 |
|  | $f n^{2}$ | 0.05407 | 0.02758 | 33151 | 3.84 | 0.0527 |
|  | sn | 12.99325 | 2.95891 | 166260 | 19.28 | <.0001 |
|  | sk | 44.85101 | 10.85156 | 147291 | 17.08 | <.0001 |
|  | sk ${ }^{2}$ | -0.15389 | 0.04563 | 98086 | 11.38 | 0.0011 |
|  | fnxsn | 0.15673 | 0.05445 | 71433 | 8.28 | 0.0049 |
|  | fkxsk | 0.06040 | 0.02431 | 53207 | 6.17 | 0.0146 |
|  | fnxfp | 0.08175 | 0.03172 | 57259 | 6.64 | 0.0114 |
|  | fpxfk ${ }^{2}$ | -0.14648 | 0.04934 | 75979 | 8.81 | 0.0037 |
|  | $\mathrm{R}^{2}=0.9885$ |  |  |  |  |  |

Table 5.1.9 Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure
Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1999

```
    Parameter Standard
Variable Estimate Error Type II SS F Value Pr > F
```

II

| $\quad$ Intercept | 1829.54647 |
| :--- | :---: |
| rep | 228.06071 |
| fn | 7.84231 |
| fp | 8.73036 |
| fk | 10.68243 |
| $\mathrm{fn}^{2}$ | 0.13632 |
| $\mathrm{fk}^{2}$ | -0.11698 |
| $\mathrm{R}^{2}=0.9874$ |  |


| Intercept | -1070.63946 |
| :--- | ---: |
| fn | -13.86882 |
| fp | 8.11463 |
| fk | 5.79270 |
| fn $^{2}$ | 0.10252 |
| fk $^{2}$ | -0.14399 |
| sn | 17.10685 |
| sk | 9.59817 |
| fnxsn | 0.10947 |
| $\quad R^{2}=0.9874$ |  |


| 29.19511 | 46491594 | 3927.05 | $<.0001$ |
| :---: | :---: | :---: | :---: |
| 9.19581 | 7281637 | 615.07 | $<.0001$ |
| 1.54195 | 306237 | 25.87 | $<.0001$ |
| 0.57085 | 2769038 | 233.90 | $<.0001$ |
| 2.58167 | 202697 | 17.12 | $<.0001$ |
| 0.01976 | 563203 | 47.57 | $<.0001$ |
| 0.05988 | 45187 | 3.82 | 0.0534 |
|  |  |  |  |
| 250.21834 | 169815 | 18.31 | $<.0001$ |
| 7.52388 | 31515 | 3.40 | 0.0682 |
| 0.50591 | 2386275 | 257.27 | $<.0001$ |
| 2.39548 | 54238 | 5.85 | 0.0174 |
| 0.02639 | 140011 | 15.10 | 0.0002 |
| 0.05303 | 68372 | 7.37 | 0.0078 |
| 2.49832 | 434881 | 46.89 | $<.0001$ |
| 1.77729 | 270513 | 29.17 | $<.0001$ |
| 0.05150 | 41916 | 4.52 | 0.0359 |
|  |  |  |  |
| 472.29626 | 207301 | 23.54 | $<.0001$ |
| 7.66631 | 50958 | 5.79 | 0.0180 |
| 0.49241 | 2367275 | 268.82 | $<.0001$ |
| 0.02632 | 118717 | 13.48 | 0.0004 |
| 0.05936 | 50507 | 5.74 | 0.0185 |
| 2.89179 | 180367 | 20.48 | $<.0001$ |
| 10.85132 | 130287 | 14.79 | 0.0002 |
| 0.04558 | 81566 | 9.26 | 0.0030 |
| 0.05369 | 64838 | 7.36 | 0.0078 |
| 0.02303 | 35520 | 4.03 | 0.0472 |
| 735.07595 | 251291 | 30.37 | $<.0001$ |
| 52.87285 | 67866 | 8.20 | 0.0051 |
| 8.87289 | 75922 | 9.17 | 0.0031 |
| 0.03012 | 23387 | 2.83 | 0.0959 |
| 3.70389 | 192525 | 23.27 | $<.0001$ |
| 12.36796 | 157986 | 19.09 | $<.0001$ |
| 12.01400 | 114110 | 13.79 | 0.0003 |
| 0.22608 | 150794 | 18.22 | $<.0001$ |
| 0.04896 | 30913 | 3.74 | 0.0561 |
| 0.05914 | 72588 | 8.77 | 0.0038 |
| 0.04925 | 172270 | 20.82 | $<.0001$ |
| 0.03418 | 65236 | 7.88 | 0.0060 |
| 0.03341 | 130388 | 15.76 | 0.0001 |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

Table 5.1.9 Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure
Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1999

IV

I

II

III

Parameter Standard

| Parameter |  |  | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Variable | Estimate | Error |  |  |  |
| Intercept | 1829.54647 | 29.19511 | 46491594 | 3927.05 | <.0001 |
| rep | 228.06071 | 9.19581 | 7281637 | 615.07 | <.0001 |
| $f \mathrm{f}$ | 7.84231 | 1.54195 | 306237 | 25.87 | <.0001 |
| $f p$ | 8.73036 | 0.57085 | 2769038 | 233.90 | <.0001 |
| $f \mathrm{f}$ | 10.68243 | 2.58167 | 202697 | 17.12 | <.0001 |
| $\mathrm{fn}^{2}$ | 0.13632 | 0.01976 | 563203 | 47.57 | <. 0001 |
| $\mathrm{fk}^{2}$ | -0.11698 | 0.05988 | 45187 | 3.82 | 0.0534 |
| $\mathrm{R}^{2}=0.9874$ |  |  |  |  |  |
| Intercept | -1070.63946 | 250.21834 | 169815 | 18.31 | <. 0001 |
| $f \mathrm{n}$ | -13.86882 | 7.52388 | 31515 | 3.40 | 0.0682 |
| $f p$ | 8.11463 | 0.50591 | 2386275 | 257.27 | <.0001 |
| $f \mathrm{f}$ | 5.79270 | 2.39548 | 54238 | 5.85 | 0.0174 |
| $\mathrm{fn}^{2}$ | 0.10252 | 0.02639 | 140011 | 15.10 | 0.0002 |
| $\mathrm{fk}^{2}$ | -0.14399 | 0.05303 | 68372 | 7.37 | 0.0078 |
| sn | 17.10685 | 2.49832 | 434881 | 46.89 | <.0001 |
| sk | 9.59817 | 1.77729 | 270513 | 29.17 | <.0001 |
| fnxsn | 0.10947 | 0.05150 | 41916 | 4.52 | 0.0359 |
| $\mathrm{R}^{2}=0.9874$ |  |  |  |  |  |
| Intercept | -2291.50713 | 472.29626 | 207301 | 23.54 | <. 0001 |
| $f \mathrm{n}$ | -18.44154 | 7.66631 | 50958 | 5.79 | 0.0180 |
| $f p$ | 8.07334 | 0.49241 | 2367275 | 268.82 | <.0001 |
| $\mathrm{fn}^{2}$ | 0.09664 | 0.02632 | 118717 | 13.48 | 0.0004 |
| $\mathrm{fk}^{2}$ | -0.14216 | 0.05936 | 50507 | 5.74 | 0.0185 |
| sn | 13.08731 | 2.89179 | 180367 | 20.48 | <. 0001 |
| sk | 41.73878 | 10.85132 | 130287 | 14.79 | 0.0002 |
| $s k^{2}$ | -0.13872 | 0.04558 | 81566 | 9.26 | 0.0030 |
| fnxsn | 0.14568 | 0.05369 | 64838 | 7.36 | 0.0078 |
| $\mathrm{R}^{2}=0.9881$ |  |  |  |  |  |
| Intercept | -4050.77186 | 735.07595 | 251291 | 30.37 | <. 0001 |
| rep | -151.41751 | 52.87285 | 67866 | 8.20 | 0.0051 |
| $f{ }^{\text {f }}$ | -26.87616 | 8.87289 | 75922 | 9.17 | 0.0031 |
| $\mathrm{fn}^{2}$ | 0.05064 | 0.03012 | 23387 | 2.83 | 0.0959 |
| sn | 17.86565 | 3.70389 | 192525 | 23.27 | <.0001 |
| sp | 54.04114 | 12.36796 | 157986 | 19.09 | <. 0001 |
| sk | 44.61347 | 12.01400 | 114110 | 13.79 | 0.0003 |
| $\mathrm{sp}^{2}$ | -0.96510 | 0.22608 | 150794 | 18.22 | <. 0001 |
| $s \mathrm{sk}^{2}$ | -0.09463 | 0.04896 | 30913 | 3.74 | 0.0561 |
| fnxsn | 0.17517 | 0.05914 | 72588 | 8.77 | 0.0038 |
| fpxsp | 0.22470 | 0.04925 | 172270 | 20.82 | <. 0001 |
| $f n x f p$ | 0.09597 | 0.03418 | 65236 | 7.88 | 0.0060 |
| fpxfk | -0.13261 | 0.03341 | 130388 | 15.76 | 0.0001 |

Table 5.1.10 Estimated ridge of maximum yield Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 1999 Average STV* of the Site: SN= $157.42 \mathrm{Kg} ; \mathrm{SP}=33.55 \mathrm{Kg} ; \mathrm{SK}=109.54 \mathrm{Kg}$

| Coded <br> Radius | Estimated <br> yield | Standard <br> Error | Uncoded Factor Values |  |  |
| :--- | :---: | :--- | :--- | :--- | :--- |
| fn |  |  | fk |  |  |
| 0.0 | 3321.498899 | 23.637714 | 37.500000 | 40.000000 | 20.000000 |
| 0.1 | 3378.876646 | 23.681125 | 40.468165 | 42.444345 | 19.981644 |
| 0.2 | 3439.287680 | 23.910252 | 43.527816 | 44.758488 | 19.936489 |
| 0.3 | 3502.809194 | 24.331266 | 46.662130 | 46.958681 | 19.871124 |
| 0.4 | 3569.503069 | 24.966935 | 49.857654 | 49.059390 | 19.790502 |
| 0.5 | 3639.419219 | 25.858413 | 53.103649 | 51.073249 | 19.698340 |
| 0.6 | 3712.598180 | 27.063183 | 56.391527 | 53.011168 | 19.597431 |
| 0.7 | 3789.073118 | 28.649513 | 59.714392 | 54.882520 | 19.489880 |
| 0.8 | 3868.871368 | 30.688604 | 63.066685 | 56.695338 | 19.377281 |
| 0.9 | 3952.015622 | 33.246474 | 66.443890 | 58.456507 | 19.260847 |
| 1.0 | 4038.524853 | 36.377771 | 69.842322 | 60.171938 | 19.141506 |
|  |  |  |  |  |  |

Table 5.1.11 : Parameter estimates along with standard errors for response surface models using different number of variables
Centre: Bhubaneswar Crop: Paddy Year: Kharif 2000

| Models |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error |
| Intercept | 2871.21669* | 77.36596 | 1930.94112 | 1592.65048 | -2655.21570 | 7995.36833 | 1672.22195 | 7772.81469 |
| fn | 20.63827* | 7.72328 | 14.37558 | 22.51648 | -23.78817 | 75.69921 | -20.08764 | 74.56008 |
| fp | 9.97022 | 6.89032 | -3.74100 | 10.30949 | -3.16906 | 18.20276 | 2.96869 | 17.69390 |
| $f \mathrm{f}$ | 4.88214 | 12.06608 | 16.03722 | 23.83112 | 16.62854 | 48.64238 | 27.72245 | 47.85593 |
| $\mathrm{fn}^{2}$ | -0.45531* | 0.15166 | -0.23861* | 0.12099 | -0.29871* | 0.16405 | -0.56052* | 0.19361 |
| $f p^{2}$ | -0.18297 | 0.12431 | 0.11559 | 0.07345 | 0.11533 | 0.08184 | -0.19238 | 0.12660 |
| $\mathrm{fk}^{2}$ | 0.21219 | 0.32236 | 0.42286* | 0.24798 | 0.43462 | 0.27748 | 0.33549 | 0.33576 |
| sn | ------- | ------- | -8.17558 | 13.60940 | 54.26162 | 122.15873 | 45.95277 | 119.51532 |
| sp | ------- | ------- | 22.95060 | 24.35525 | 16.43070 | 102.51585 | 46.24442 | 99.62992 |
| sk | ------- | ------- | 14.92981 | 10.29697 | 13.61061 | 87.87601 | -2.03861 | 85.78530 |
| sn ${ }^{2}$ | ------- | ------- | ------- | ------- | -0.20184 | 0.39662 | -0.17126 | 0.38833 |
| sp ${ }^{2}$ | ------- | ------- | ------- | ------- | 0.06156 | 1.75083 | -0.38179 | 1.69693 |
| sk ${ }^{2}$ | ------- | ------- | ------ | ------- | 0.00442 | 0.43089 | 0.07224 | 0.42052 |
| fn*sn | ------- | ------- | 0.11208 | 0.17959 | 0.35787 | 0.50115 | 0.27872 | 0.49136 |
| fp*sp | ------ | ------ | -0.06048 | 0.32595 | -0.06908 | 0.60865 | 0.09868 | 0.59283 |
| fk*sk | ------- | ------ | -0.22280 | 0.24028 | -0.22974 | 0.49334 | -0.27908 | 0.47866 |
| fn*fp | 0.52543* | 0.22919 | ---- | ---- | -- | ---- | 0.55392* | 0.21027 |
| fn*fk | 0.12570 | 0.22298 | -- | ------- | ------- | ------- | 0.13875 | 0.20946 |
| $f \mathrm{f}^{*} \mathrm{fk}$ | -0.16611 | 0.31038 | ------- | ------- | ------- | ------ | -0.18574 | 0.28578 |
| $\mathrm{R}^{2}$ | 0.7614 |  | 0.8070 |  | 0.8077 |  | 0.8263 |  |

Table 5.1.12 Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure

Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 2000

| Model | Variable | Parameter Estimate | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 2893.71003 | 63.43730 | 378334206 | 2080.75 | <. 0001 |
|  | $f{ }^{\text {f }}$ | 26.78225 | 5.26500 | 4704919 | 25.88 | <. 0001 |
|  | $\mathrm{fn}^{2}$ | -0.33327 | 0.08626 | 2713872 | 14.93 | 0.0002 |
|  | $f{ }^{2}$ | 0.28127 | 0.09369 | 1638880 | 9.01 | 0.0033 |
|  | $\mathrm{R}^{2}=0.7558$ |  | 0.06538 | 2879174 | 15.83 | 0.0001 |
| II | Intercept | 1265.28766 | 291.86840 | 2816574 | 18.79 | <. 0001 |
|  |  | 24.53193 | 4.80707 | 3903184 | 26.04 | <. 0001 |
|  | $\mathrm{fn}^{2}$ | -0.14848 | 0.06434 | 798119 | 5.33 | 0.0230 |
|  | $f p^{2}$ | 0.06904 | 0.02463 | 1177020 | 7.85 | 0.0060 |
|  | $f{ }^{2}$ | 0.16103 | 0.08863 | 494710 | 3.30 | 0.0721 |
|  | $\mathrm{SK}^{\mathbf{2}}=0.8006{ }^{15.85680}$ |  | 2.88434 | 4529546 | 30.22 | <. 0001 |
| III | Intercept | 927.88167 | 492.49260 | 543118 | 3.55 | 0.0624 |
|  |  | 35.05396 | 18.89109 | 526827 | 3.44 | 0.0663 |
|  | $\mathrm{fn}^{2}$ | -0.20777 | 0.08734 | 865887 | 5.66 | 0.0192 |
|  | $f p^{2}$ | 0.06987 | 0.02512 | 1183819 | 7.74 | 0.0064 |
|  | $f{ }^{2}$ | 0.47523 | 0.24157 | 592148 | 3.87 | 0.0518 |
|  | sk | 19.45120 | 4.94881 | 2363741 | 15.45 | 0.0002 |
|  | fnxsn | 0.15423 | 0.03607 | 2796980 | 18.28 | <. 0001 |
|  | fkxsk $\mathrm{R}^{2}=0.80$ | -0.40843 | 0.19090 | 700386 | 4.58 | 0.0347 |
| IV | Intercept | 2347.77052 | 251.38414 | 12051259 | 87.22 | <.0001 |
|  | $\mathrm{fn}^{2}$ | -0.50775 | 0.10276 | 3373260 | 24.41 | <.0001 |
|  | $f \mathrm{p}^{2}$ | -0.13777 | 0.05337 | 920551 | 6.66 | 0.0112 |
|  | $f{ }^{2}$ | 0.27100 | 0.08172 | 1519519 | 11.00 | 0.0013 |
|  | $\mathrm{sp}{ }_{2}$ | 48.43155 | 10.98369 | 2686317 | 19.44 | <. 0001 |
|  | $\mathrm{sn}^{2}$ | -0.03852 | 0.01848 | 600207 | 4.34 | 0.0396 |
|  | fnxsn | 0.19322 | 0.03821 | 3533691 | 25.58 | <. 0001 |
|  | $f n x f p$ | 0.43599 | 0.11915 | 1849927 | 13.39 | 0.0004 |
|  | $\mathrm{R}^{2}=0.8$ |  |  |  |  |  |

Table 5.1.13 Parameter estimates along with standard errors for response surface models using different number of variables (models include replication)

Centre: Bhubaneswar Crop: Paddy Year: Kharif 2000

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 2438.83276* | 106.12984 | -183.61741 | 2081.12434 | -11514* | 9013.69942 | -11601* | 8663.90633 |
| Replication | 172.95357* | 32.37424 | -261.19753 | 167.14327 | -389.26513 | 193.02937 | -439.97718 | 185.43250 |
| $f$ f | 20.63827* | 6.85329 | 14.23183 | 22.35444 | -47.62612 | 75.45006 | -46.28938 | 73.60385 |
| fp | 9.97022 | 6.11416 | -4.58540 | 10.24947 | -2.13294 | 17.92617 | 4.50160 | 17.28135 |
| $f \mathrm{f}$ | 4.88214 | 10.70690 | 23.76940 | 24.17127 | -5.34799 | 49.10802 | 3.20454 | 47.83683 |
| $\mathrm{fn}^{2}$ | -0.45531* | 0.13458 | -0.22773* | 0.12032 | -0.33043* | 0.16226 | -0.60969* | 0.19010 |
| $f p^{2}$ | -0.18297 | 0.11030 | 0.12746* | 0.07332 | 0.12931 | 0.08086 | -0.19526 | 0.12356 |
| $\mathrm{fk}^{2}$ | 0.21219 | 0.28605 | 0.49931* | 0.25101 | 0.46622* | 0.27360 | 0.35681 | 0.32782 |
| sn | - | ---- | -4.38629 | 13.72721 | 93.16501 | 121.79067 | 88.78428 | 118.03565 |
| sp | ------- | ------- | 46.54999 | 28.50820 | 21.30987 | 100.94563 | 53.38618 | 97.28551 |
| sk | ------ | ------- | 30.41159* | 14.23564 | 107.24115 | 98.17768 | 103.32608 | 94.77401 |
| $\mathrm{sn}^{2}$ | ------- | ------- | ------ | ------- | -0.30316 | 0.39366 | -0.28182 | 0.38186 |
| sp ${ }^{2}$ |  |  |  |  | 0.47490 | 1.73566 | 0.05995 | 1.66664 |
| sk ${ }^{2}$ | ------- | ------- | ------ | ------- | -0.34537 | 0.45827 | -0.32110 | 0.44265 |
| fn*sn | ------- | ------- | ------- | ------- | ------- | ------- | 0.40913 | 0.48271 |
| $f p^{*}$ sp | ------- | ------- | ------- | ------- | ------- | ------- | -0.13113 | 0.58665 |
| fk*sk | ------- | ------- | ------- | ------- | -- | ------- | -0.14416 | 0.47062 |
| $f n^{* f p}$ | 0.52543* | 0.20337 | 0.09336 | 0.17869 | 0.47967 | 0.49702 | 0.58193* | 0.20556 |
| $f n^{* f k}$ | 0.12570 | 0.19786 | -0.17515 | 0.33182 | -0.28171 | 0.60837 | 0.14809 | 0.20447 |
| fp*fk | -0.16611 | 0.27542 | -0.36966 | 0.25639 | -0.10838 | 0.48936 | -0.18617 | 0.27893 |
| $\mathrm{R}^{2}$ | 0.8140 |  | 0.8117 |  | 8156 | 0 |  |  |

Table 5.1.14 Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure

## Centre: Bhubaneswar Crop: Paddy (Konark) Year: Kharif 2000

| Model | Variable | Parameter Estimate | Standard Error | Type II SS F | F Value P | Pr > F |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 2461.32610 | 98.07090 | 90723708 | 629.88 | <. 0001 |
|  | rep | 172.95357 | 32.07505 | 4187811 | 29.08 | <. 0001 |
|  | fn | 26.78225 | 4.68600 | 4704919 | 32.67 | <. 0001 |
|  | $\mathrm{fn}^{2}$ | -0.33327 | 0.07678 | 2713872 | 18.84 | <. 0001 |
|  | fk2 | 0.28127 | 0.08339 | 1638880 | 11.38 | 0.0010 |
|  | $\mathbf{R}^{2}=0.8083$ |  | 0.05819 | 2879174 | 19.99 | <. 0001 |
| II | Intercept | 1265.28766 | 291.86840 | 2816574 | 18.79 | <. 0001 |
|  | $f{ }^{\text {f }}$ | 24.53193 | 4.80707 | 3903184 | 26.04 | <. 0001 |
|  | $\mathrm{fn}^{2}$ | -0.14848 | 0.06434 | 798119 | 5.33 | 0.0230 |
|  | $f p^{2}$ | 0.06904 | 0.02463 | 1177020 | 7.85 | 0.0060 |
|  | $f \mathrm{k}^{2}$ | 0.16103 | 0.08863 | 494710 | 3.30 | 0.0721 |
|  | $\mathrm{R}^{2}=0.8006$ |  | 2.88434 | 4529546 | 30.22 | <. 0001 |
| III | Intercept | -4942.37941 | 2088.55048 | 850219 | 5.60 | 0.0198 |
|  | rep | -191.60711 | 78.82696 | 897061 | 5.91 | 0.0168 |
|  | $f \mathrm{n}^{2}$ | -0.17866 | 0.08287 | 705727 | 4.65 | 0.0334 |
|  | $f p_{2}$ | 0.05813 | 0.02671 | 718809 | 4.73 | 0.0318 |
|  | sk | 126.78973 | 36.53602 | 1828412 | 12.04 | 0.0008 |
|  | sk ${ }^{2}$ | -0.43455 | 0.14742 | 1319152 | 8.69 | 0.0039 |
|  | $\begin{aligned} & \text { fnxsn } \\ & R^{2}=0.799 \end{aligned}$ | 0.13895 | 0.03452 | 2459508 | 16.20 | 0.0001 |
| IV | Intercept | -6066.31160 | 1970.14039 | 1245583 | 9.48 | 0.0027 |
|  | rep | -399.55640 | 105.39683 | 1888073 | 14.37 | 0.0003 |
|  | $\mathrm{fn}^{2}$ | -0.45261 | 0.10205 | 2584190 | 19.67 | <. 0001 |
|  | $f p^{2}$ | -0.20288 | 0.06646 | 1224339 | 9.32 | 0.0029 |
|  | sp | 51.02541 | 18.28155 | 1023446 | 7.79 | 0.0063 |
|  | sk | 132.23219 | 34.03036 | 1983622 | 15.10 | 0.0002 |
|  | sk ${ }^{2}$ | -0.46554 | 0.13737 | 1508931 | 11.49 | 0.0010 |
|  | fnxsn | 0.10797 | 0.03300 | 1405938 | 10.70 | 0.0015 |
|  | fnxfp | 0.50989 | 0.12317 | 2251510 | 17.14 | <. 0001 |

Table 5.1.15 Estimated ridge of maximum yield Centre: Bhubaneswar Crop: Paddy Year: Kharif 2000

## Average STV* of the Site: $\mathrm{SN}=165.60 \mathrm{Kg}$; $\mathrm{SP}=\mathbf{3 4 . 5 1 \mathrm { Kg } ; \mathrm { SK } = 1 0 8 . 4 3 \mathrm { Kg } .}$

| Coded | Estimated | Standard | Uncoded |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Radius | yield | Error | fn | fn Values |  |  |
| 0.0 | 4042.991388 | 108.100649 | 37.500000 | 40.000000 | 20.000000 |  |
| 0.1 | 4106.848796 | 108.511274 | 39.649687 | 42.937445 | 20.726906 |  |
| 0.2 | 4169.894423 | 108.246806 | 41.739753 | 45.893769 | 21.484196 |  |
| 0.3 | 4232.153786 | 107.312996 | 43.791428 | 48.847513 | 22.274088 |  |
| 0.4 | 4293.646673 | 105.771137 | 45.813970 | 51.785945 | 23.100238 |  |
| 0.5 | 4354.392096 | 103.728883 | 47.811141 | 54.699359 | 23.967389 |  |
| 0.6 | 4414.410649 | 101.339839 | 49.783659 | 57.578767 | 24.881332 |  |
| 0.7 | 4473.726072 | 98.806429 | 51.730173 | 60.414695 | 25.848989 |  |
| 0.8 | 4532.366681 | 96.382841 | 53.647631 | 63.196377 | 26.878537 |  |
| 0.9 | 4590.366895 | 94.374524 | 55.531324 | 65.911084 | 27.979530 |  |
| 1.0 | 4647.769038 | 93.129945 | 57.374766 | 68.543499 | 29.162958 |  |

* STV- Soil Test Value

Table 5.2.1: Parameter estimates along with standard errors for response surface models using different number of variables Centre: Hyderabad Crop: Sunflower Year: Rabi- 1993

| Models |  | 1 |  |  |  | III |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error |
| Intercept | 740.67470 | 52. 47508 | 572.48037 | 387.90244 | -646.45073 | 1720.40134 | -832.04654 | 1734.08631 |
| $f 0$ | 13.50872 | 1.28110 | 8.75395 | 3.63183 | 5,79765 | 6.37837 | 6.78457 | 6.50202 |
| fp | 1.96191 | 1.64270 | 0.63621 | 2.01861 | 0.47315 | 1.99573 | 0.23788 | 2.01400 |
| fk | 0.14721 | 1.62007 | -3.19157 | 3.26921 | -4.45835 | 3.23642 | -4.86907 | 3.26148 |
| $f n^{2}$ | -0.05922 | 0.00898 | -0.05220 | 0.01334 | -0.04926 | 0.01505 | -0.04553 | 0.01546 |
| $f p^{2}$ | -0.02139 | 0.01744 | -0.01674 | 0.01639 | -0.01885 | 0.01618 | -0.01706 | 0.01629 |
| $f \mathrm{k}^{2}$ | 0.00059 | 0.01713 | 0.00247 | 0.01619 | 0.00258 | 0.01591 | 0.00257 | 0.01598 |
| sn | ---.-.-. |  | -0.11809 | 1.48203 | 1.43932 | 13.07375 | 1.64074 | 13.17814 |
| sp | -----.-- | -.--. - | 0.84786 | 3.05122 | 31.02999 | 12.00071 | 28.05288 | 12.46520 |
| sk | ---.-.-- | - - | 0.75573 | 0.55014 | 4.23370 | 4.48280 | 5.24615 | 4.57094 |
| $\mathrm{sn}^{2}$ | -------- |  | ------ | --.--- | -0.00391 | 0.02830 | -0.00404 | 0.02857 |
| $s p^{2}$ |  |  | ------ | -.-.-. | -0.48237 | 0.19048 | -0.42905 | 0.19636 |
| $s \mathrm{k}^{2}$ | .-----. |  |  | ...-.- | -0.00462 | 0.00609 | -0.00623 | 0.00622 |
| fn*s! | --.---. - |  | 0.01017 | 0.01653 | 0.01945 | 0.02874 | 0.01596 | 0.02922 |
| fp*sp | ----.---- |  | 0.03067 | 0.04942 | 0.04171 | 0.04906 | 0.05515 | 0.05792 |
| fk*sk | -...-.-.-. |  | 0.00676 | 0.00870 - | 0.01031 | 0.00861 | 0.01425 | 0.00910 |
| fn*fp | -0.00192 | 0.00996 | --.-.-. | ------ | --.-.- | --. - - | -0.00328 | 0.01073 |
| fn* $\ddagger$ k | -0.00682 | 0.01002 | ----. | - .-. --. | ----.-. | --. - . | -0.01418 | 0.01017 |
| fp*fk | 0.00495 | 0.01193 | -. --- - | --.-. - | -----. | --.-. | -0.00207 | 0.01153 |
| $\mathrm{H}^{2}$ | 0.7339 0.7766 |  |  |  | 0.7921 |  | 0.7965 |  |

Table 5.2.2 Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure Centre: Hyderabad Crop: Sunflower Year: Rabi- 1993

| Model | Variable | Parameter Estimate | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 770.28409 | 36.98861 | 8244270 | 433.68 | <. 0001 |
|  | $f \mathrm{n}$ | 13.32749 | 1.21251 | 2296762 | 120.82 | <. 0001 |
|  | fn2 | -0.06019 | 0.00866 | 918225 | 48.30 | <. 0001 |
|  | $\mathrm{R}^{2}=0.7264$ |  |  |  |  |  |
| II | Intercept | 439.39668 | 115.82435 | 237897 | 14.39 | 0.0002 |
|  | $f \mathrm{n}$ | 10.45566 | 1.46677 | 839945 | 50.81 | <.0001 |
|  | $f \mathrm{f} 2$ | -0.04320 | 0.01018 | 297437 | 17.99 | <. 0001 |
|  | fp2 | -0.01752 | 0.01056 | 45533 | 2.75 | 0.0997 |
|  | sk | 1.09486 | 0.37759 | 138981 | 8.41 | 0.0045 |
|  | fpsp | 0.05244 | 0.02745 | 60307 | 3.65 | 0.0586 |
|  | $\mathrm{R}^{2}=0.7682$ |  |  |  |  |  |
| III | Intercept | -71.49933 | 225.06627 | 1616.64053 | 0.10 | 0.7513 |
|  | $f \mathrm{n}$ | 9.99236 | 1.48698 | 723361 | 45.16 | <. 0001 |
|  | fn2 | -0.04054 | 0.01064 | 232485 | 14.51 | 0.0002 |
|  | sp | 28.84053 | 11.43482 | 101901 | 6.36 | 0.0130 |
|  | sk | 1.27353 | 0.42063 | 146839 | 9.17 | 0.0030 |
|  | $\mathrm{R}^{2}=0.7754$ |  |  |  |  |  |
| IV | Intercept | -62.56971 | 222.91849 | 1237.44008 | 0.08 | 0.7795 |
|  | fn | 10.15944 | 1.47533 | 744815 | 47.42 | <. 0001 |
|  | fn2 | -0.04015 | 0.01054 | 227910 | 14.51 | 0.0002 |
|  | sp | 26.96939 | 11.37018 | 88368 | 5.63 | 0.0194 |
|  | sk | 1.31211 | 0.41707 | 155462 | 9.90 | 0.0021 |
|  | sp2 | -0.36341 | 0.17750 | 65840 | 4.19 | 0.0429 |
|  | fnfk | -0.00824 | 0.00456 | 51275 | 3.26 | 0.0735 |
|  | $\mathrm{R}^{2}=0.7817$ |  |  |  |  |  |

Table 5.2.3 : Parameter estimates along with standard errors for response surface models using different number of Variables (models include replication)

Centre: Hyderabad Crop: Sunflower Year: Rabi- 1993

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 582.19884 | 52.42237 | 436.27424 | 344.43589 | -2698.43970 | 1560.04346 | -3042.73491 | 1560.99622 |
| Replication | 61.12290 | 10.02634 | 56.62947 | 10.26889 | 57.91092 | 10.40707 | 59.88060 | 10.46087 |
| fn | 13.50248 | 1.11137 | 8.65258 | 3.21661 | 0.65715 | 5.69535 | 0.93710 | 5.76233 |
| fp | 1.79037 | 1.42534 | 1.82449 | 1.80074 | 1.41101 | 1.76648 | 1.13336 | 1.76356 |
| fk | 0.81929 | 1.40975 | -1.80617 | 2.90628 | -3.02989 | 2.86312 | -3.44876 | 2.85546 |
| fn2 | -0.05872 | 0.00779 | -0.04264 | 0.01195 | -0.04178 | 0.01333 | -0.03880 | 0.01353 |
| fp2 | -0.02216 | 0.01513 | -0.01901 | 0.01452 | -0.01817 | 0.01425 | -0.01580 | 0.01421 |
| fk2 | -0.00148 | 0.01486 | 0.00226 | 0.01434 | 0.00425 | 0.01402 | 0.00413 | 0.01394 |
| sn | ------- | - | -0.62763 | 1.31582 | 15.64988 | 11.79888 | 17.21692 | 11.81167 |
| sp | ------- | ------- | 0.32069 | 2.70403 | 19.94071 | 10.75990 | 17.31945 | 11.03265 |
| sk | ------ | ------- | 1.14185 | 0.49224 | 6.65188 | 3.97360 | 7.71073 | 4.00995 |
| sn2 | ------- | ------- | 0.00731 | 0.01465 | -0.03530 | 0.02557 | -0.03870 | 0.02564 |
| sp2 | ------- | ------- | -0.00901 | 0.04436 | -0.30011 | 0.17100 | -0.23338 | 0.17465 |
| sk2 | ------- |  | 0.00354 | 0.00773 | -0.00749 | 0.00539 | -0.00920 | 0.00545 |
| fnsn | ------- | ------- | ------- | ------- | 0.03715 | 0.02552 | 0.03657 | 0.02574 |
| fpsp | ------- | ------- | ------- | ------- | 0.00530 | 0.04372 | -0.00205 | 0.05149 |
| fksk | ------- | ------- | ------- | ------- | 0.00627 | 0.00762 | 0.01065 | 0.00797 |
| fnfp | 0.00053 | 0.00865 | ------- | ------- | ------- | ------- | 0.00297 | 0.00942 |
| fnfk | -0.01104 | 0.00872 | ------- | ------- | ------- | ------- | -0.01838 | 0.00890 |
| fpfk | 0.00203 | 0.01036 | ------- | ------- | ------- | ------- | 0.00214 | 0.01008 |
| $\mathrm{R}^{2}$ | 0.8015 |  | 8264 |  | 8401 | 0 |  |  |

Table 5.2.4 Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure
Centre: Hyderabad Crop: Sunflower Year: Rabi- 1993

Model
I

II

III

IV

| Variable | Parameter <br> Estimate |
| :--- | ---: |
| Intercept | 619.15909 |
| rep | 60.45000 |
| fn | 13.32749 |
| fn2 | -0.06019 |
| $R^{2}=0.7938$ |  |
| Intercept | 255.05988 |
| rep | 57.38223 |
| fn | 10.15884 |
| fn2 | -0.04007 |
| sk | 1.25386 |
| R2 $=0.8211$ |  |
| Intercept | -1732.52994 |
| rep | 58.16108 |
| fn2 | -0.04891 |
| sn | 15.75487 |
| sp | 19.48615 |
| sk | 1.34103 |
| sn2 | -0.03678 |
| sp2 | -0.30427 |
| fnsn | 0.04458 |
| $R^{2}=0.8314$ |  |


| Standard <br> Error | Type II SS | F Value | Pr $>$ F |
| ---: | ---: | ---: | :--- |
| 40.52048 | 3373550 | 233.48 | $<.0001$ |
| 9.81455 | 548130 | 37.94 | $<.0001$ |
| 1.05708 | 2296762 | 158.96 | $<.0001$ |
| 0.00755 | 918225 | 63.55 | $<.0001$ |
|  |  |  |  |
| 94.89420 | 91374 | 7.22 | 0.0083 |
| 9.21173 | 490781 | 38.80 | $<.0001$ |
| 1.24594 | 840336 | 66.44 | $<.0001$ |
| 0.00855 | 278047 | 21.98 | $<.0001$ |
| 0.29958 | 221561 | 17.52 | $<.0001$ |
|  |  |  |  |
| 914.11610 | 44361 | 3.59 | 0.0607 |
| 9.86426 | 429321 | 34.76 | $<.0001$ |
| 0.01128 | 232142 | 18.80 | $<.0001$ |
| 7.29658 | 57575 | 4.66 | 0.0330 |
| 10.48351 | 42666 | 3.45 | 0.0657 |
| 0.37314 | 159505 | 12.92 | 0.0005 |
| 0.01404 | 84749 | 6.86 | 0.0100 |
| 0.16440 | 42300 | 3.43 | 0.0669 |
| 0.00597 | 687690 | 55.69 | $<.0001$ |
|  |  |  |  |
| 904.43439 | 62473 | 5.12 | 0.0256 |
| 9.59695 | 499623 | 40.91 | $<.0001$ |
| 0.01110 | 214490 | 17.56 | $<.0001$ |
| 6.88401 | 107212 | 8.78 | 0.0037 |
| 0.33130 | 212517 | 17.40 | $<.0001$ |
| 0.01305 | 150407 | 12.32 | 0.0006 |
| 0.00583 | 71815 | 58.28 | $<.0001$ |
| 0.00390 | 45883 | 3.76 | 0.0551 |

Table 5.2.5 : Estimated ridge of maximum yield

## Centre: Hyderabad Crop: Sunflower Year: Rabi-1993



| Coded | Estimated | Standard | Uncoded Factor Values |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Radius | yield | Error | fn | fp | $f \mathrm{f}$ |
| 0.0 | 1352.907834 | 33.536170 | 60.000000 | 40.000000 | 40.000000 |
| 0.1 | 1380.655736 | 33.323255 | 65.982142 | 40.107061 | 39.710795 |
| 0.2 | 1405.250713 | 32.858784 | 71.938680 | 40.232173 | 39.226367 |
| 0.3 | 1426.747707 | 32.169029 | 77.840959 | 40.378932 | 38.454097 |
| 0.4 | 1445.242206 | 31.333335 | 83.627629 | 40.549439 | 37.246746 |
| 0.5 | 1460.906359 | 30.474620 | 89.169257 | 40.739280 | 35.384819 |
| 0.6 | 1474.047466 | 29.719423 | 94.226235 | 40.927584 | 32.617471 |
| 0.7 | 1485.154702 | 29.133644 | 98.497247 | 41.073003 | 28.857061 |
| 0.8 | 1494.834558 | 28.739894 | 101.844439 | 41.139193 | 24.363533 |
| 0.9 | 1503.635231 | 28.634233 | 104.402053 | 41.122844 | 19.542772 |
| 1.0 | 1511.941638 | 29.015876 | 106.402736 | 41.041936 | 14.663650 |

Table 5.2.6 : Parameter estimates along with standard errors for response surface models using different number of variables Centre: Hyderabad Crop: Groundnut Year: Rabi 1997-98

|  | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 1514.49542 | 18.22951 | 1452.67797 | 129.52802 | 2848.48921 | 972.40612 | 1957.75290 | 737.28950 |
| fn | 4.39738 | 2.35580 | -8.41342 | 5.51750 | -4.41815 | 5.73632 | -5.56166 | 4.27842 |
| $f p$ | 3.85008 | 1.17790 | 5.04775 | 0.81576 | 5.95437 | 0.91015 | 5.35547 | 0.69638 |
| fk | 0.84568 | 1.17790 | -3.38522 | 2.54446 | 1.38416 | 3.47276 | 1.82972 | 2.98264 |
| fn2 | 0.18969 | 0.07288 | 0.16389 | 0.04582 | 0.17620 | 0.05293 | 0.17653 | 0.03958 |
| fp2 | -0.02600 | 0.01822 | -0.01674 | 0.01131 | -0.02592 | 0.01189 | -0.01971 | 0.00874 |
| fk2 | 0.00580 | 0.01822 | 0.01237 | 0.01217 | 0.01451 | 0.01217 | 0.01160 | 0.00940 |
| sn | - | ----- | -0.49033 | 0.45219 | 2.54460 | 4.31438 | -2.18743 | 3.22743 |
| sp | ------- | ------- | 7.91547 | 0.73519 | 4.39700 | 2.51299 | 8.67728 | 1.89281 |
| sk | ------- | ------- | -0.16356 | 0.33048 | -10.91783 | 5.14106 | -2.39805 | 3.93268 |
| sn2 | ------- | ------- | ------ | ------- | -0.00522 | 0.00870 | 0.00401 | 0.00651 |
| sp2 | ------- | ------- | ------- | ------- | 0.05289 | 0.03640 | 0.01357 | 0.02703 |
| sk2 | ------- | ------- | ------ | ------- | 0.01631 | 0.00780 | 0.00369 | 0.00594 |
| fnsn | ------ | ------- | 0.06098 | 0.02354 | 0.04134 | 0.02540 | 0.03074 | 0.01895 |
| fpsp | ------ | ------ | -0.06039 | 0.01762 | -0.07414 | 0.02069 | -0.09520 | 0.01538 |
| fksk | ------ | ------- | 0.01045 | 0.00771 | -0.00367 | 0.01052 | -0.00444 | 0.00963 |
| fnfp | 0.06764 | 0.02473 |  | ------- | ------- | ------ | 0.10412 | 0.01161 |
| fnfk | 0.03611 | 0.02473 |  | ------- | ------- | ------- | 0.03887 | 0.01485 |
| fpfk | -0.01153 | 0.01237 | ------ | ------ | ------ | ------ | -0.01167 | 0.00630 |
| $\mathrm{R}^{2}$ | 0.8613 |  | 0.9522 |  | 9552 |  |  |  |

# Table 5.2.7 Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure 

## Centre: Hyderabad Crop: Groundnut Year: Rabi 1997-98

| Models | Variable | Parameter <br> Estimate | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 1514.59058 | 16.27260 | 57558160 | 8663.17 | <. 0001 |
|  | fn | 5.48555 | 2.28574 | 38266 | 5.76 | 0.0180 |
|  | fp | 1.94547 | 0.44789 | 125354 | 18.87 | <.0001 |
|  | $f \mathrm{k}$ | 1.39032 | 0.30597 | 137187 | 20.65 | <.0001 |
|  | fn2 | 0.18962 | 0.07287 | 44992 | 6.77 | 0.0105 |
|  | fnfp $\mathbf{R}^{2}=0.8552$ | $\mathrm{R}^{2}=0.8552$ | 0.02438 | 51064 | 7.69 | 0.0065 |
| II | Intercept | 1280.20559 | 22.23305 | 7864059 | 3315.60 | <. 0001 |
|  | fp | 4.04634 | 0.59888 | 108275 | 45.65 | <. 0001 |
|  | fn2 | 0.16599 | 0.04406 | 33667 | 14.19 | 0.0003 |
|  | sp | 7.96976 | 0.72492 | 286681 | 120.87 | <.0001 |
|  | fnsn | 0.02619 | 0.00544 | 54934 | 23.16 | <.0001 |
|  | fpsp | -0.05982 | 0.01693 | 29609 | 12.48 | 0.0006 |
|  | $R^{2}=0.9488$ |  | 0.00050144 | 83556 | 35.23 | <.0001 |
| III | Intercept | 2939.94133 | 604.93954 | 52349 | 23.62 | <. 0001 |
|  | fp | 5.46819 | 0.80021 | 103499 | 46.70 | <. 0001 |
|  | fn2 | 0.17095 | 0.04327 | 34587 | 15.60 | 0.0001 |
|  | fp2 | -0.02668 | 0.01135 | 12253 | 5.53 | 0.0205 |
|  | fk2 | 0.01577 | 0.00362 | 42038 | 18.97 | <.0001 |
|  | sp | 8.02111 | 0.71245 | 280942 | 126.75 | <. 0001 |
|  | sk | -9.90238 | 3.59996 | 16770 | 7.57 | 0.0070 |
|  | sk2 | 0.01468 | 0.00534 | 16773 | 7.57 | 0.0070 |
|  | fnsn | $0.02485$ | 0.00573 | 41727 | 18.83 | <.0001 |
|  | $\begin{aligned} & \text { fpsp } \\ & R^{R^{2}}=0.953 \end{aligned}$ | $-0.05779$ | 0.01679 | 26249 | 11.84 | 0.0008 |
| IV |  |  | 15.90160 | $7422029$ |  |  |
|  | fn | $-3.79885$ | $2.17765$ | 3526.89999 | 3.04 | $0.0839$ |
|  | fp | 5.16264 | 0.57570 | 93200 | 80.42 | <.0001 |
|  | fn2 | 0.16194 | 0.03136 | 30910 | 26.67 | <.0001 |
|  | fp2 | -0.01961 | 0.00781 | 7311.65508 | 6.31 | 0.0135 |
|  | fk2 | 0.01543 | 0.00355 | 21949 | 18.94 | <.0001 |
|  | sp | 9.38610 | 0.53810 | 352626 | 304.26 | <.0001 |
|  | fnsn | 0.02541 | 0.00898 | 9291.19676 | 8.02 | 0.0055 |
|  | fpsp | -0.08988 | 0.01274 | 57691 | 49.78 | <.0001 |
|  | $f \mathrm{ffp}$ | 0.10452 | 0.01082 | 108064 | 93.24 | <. 0001 |
|  | $f n f k$ | 0.03977 | 0.01018 | 17667 | 15.24 | 0.0002 |
|  | fpfk $\mathrm{R}^{2}=0.97$ | -0.01074 | 0.00507 | 5199.62381 | 4.49 | 0.0365 |
|  | $\mathrm{R}^{2}=0.9761$ |  |  |  |  |  |

Table 5.2.8: Parameter estimates along with standard errors for response surface models using different number of variables (models include replication)
Centre: Hyderabad Crop: Groundnut Year: Rabi 1997-98

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 1367.34542 | 13.19164 | 1619.58398 | 129.42285 | 3289.79612 | 870.72347 | 2252.72018 | 721.31271 |
| Replication | 58.86000 | 3.55043 | 36.34740 | 9.45716 | 50.56648 | 9.57102 | 23.47708 | 8.39142 |
| fn | 4.39738 | 1.26113 | -10.65695 | 5.22611 | -6.68884 | 5.13083 | -6.74952 | 4.16247 |
| fp | 3.85008 | 0.63056 | 4.78196 | 0.77095 | 6.36235 | 0.81489 | 5.59520 | 0.67940 |
| fk | 0.84568 | 0.63056 | -2.37030 | 2.40952 | 3.12470 | 3.11277 | 3.10328 | 2.92234 |
| $\mathrm{fn}^{2}$ | 0.18969 | 0.03901 | 0.15162 | 0.04324 | 0.17561 | 0.04718 | 0.17481 | 0.03831 |
| $f p^{2}$ | -0.02600 | 0.00975 | -0.01411 | 0.01067 | -0.02356 | 0.01061 | -0.01921 | 0.00846 |
| $\mathrm{fk}^{2}$ | 0.00580 | 0.00975 | 0.01416 | 0.01146 | 0.01644 | 0.01086 | 0.01390 | 0.00913 |
| sn | - | ------- | -0.92500 | 0.44040 | 2.39623 | 3.84552 | -1.70394 | 3.12836 |
| sp | ------ | ------- | 3.80950 | 1.27286 | -5.97135 | 2.97795 | 3.37499 | 2.63584 |
| sk | ------- | ------- | -0.31405 | 0.31353 | -12.43197 | 4.59119 | -4.03555 | 3.85088 |
| sn2 | ------- | ------- | ------- | ------- | -0.00586 | 0.00775 | 0.00260 | 0.00632 |
| sp2 | ------ | ------- | ------- | ------- | 0.12488 | 0.03519 | 0.05095 | 0.02938 |
| sk2 | ------- | ------- | ------- | ------- | 0.01834 | 0.00697 | 0.00608 | 0.00581 |
| fn*sn | ------- | ------- | 0.07648 | 0.02252 | 0.05614 | 0.02281 | 0.03994 | 0.01863 |
| $f p^{*}$ p | ------- | ------- | -0.04171 | 0.01728 | -0.06978 | 0.01846 | -0.08985 | 0.01501 |
| fk*sk | ------- | ------- | 0.00787 | 0.00729 | -0.00818 | 0.00942 | -0.00836 | 0.00942 |
| fn*fp | 0.06764 | 0.01324 | ------ | ------- | ------ | ------- | 0.08961 | 0.01237 |
| $f n^{*} \mathrm{fk}$ | 0.03611 | 0.01324 | ------- | ------- | ------- | ------- | 0.03885 | 0.01437 |
| $f{ }^{\text {f*fk }}$ | -0.01153 | 0.00662 | ------- | ------- | ------- | - | -0.00939 | 0.00615 |
| $\mathrm{R}^{2}$ | 0.9606 |  | 0.9581 |  | . 9647 |  | 785 |  |

Table 5.2.9 Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure

| $\begin{aligned} & \text { Models } \\ & \text { I } \end{aligned}$ | Centre: Hyderabad C |  | Crop: Groundnut Year: Rabi 1997-98 <br> Parameter Standard |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Variable | Estimate | Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
|  | Intercept | 1366.64120 | 13.09980 | 20458588 | 10883.80 | <. 0001 |
|  | rep | 58.86000 | 3.53999 | 519675 | 276.46 | <. 0001 |
|  | fn | 4.35043 | 1.25496 | 22589 | 12.02 | 0.0008 |
|  | fp | 3.82660 | 0.62748 | 69908 | 37.19 | <. 0001 |
|  | $f \mathrm{k}$ | 1.17823 | 0.29111 | 30793 | 16.38 | <. 0001 |
|  | fn2 | 0.19022 | 0.03889 | 44972 | 23.92 | <. 0001 |
|  | fp2 | -0.02587 | 0.00972 | 13311 | 7.08 | 0.0090 |
|  | fnfp | 0.06803 | 0.01318 | 50050 | 26.63 | <. 0001 |
|  | $f \mathrm{ffk}$ | 0.03650 | 0.01318 | 14410 | 7.67 | 0.0066 |
|  | fpfk | -0.01133 | 0.00659 | 5553 | 2.95 | 0.0885 |
|  | $\mathrm{R}^{2}=0.960$ |  |  |  |  |  |
| II | Intercept | 1553.93200 | 100.23961 | 493339 | 240.32 | <. 0001 |
|  | rep | 36.66289 | 9.20108 | 32594 | 15.88 | 0.0001 |
|  | $f \mathrm{f}$ | -12.59307 | 4.88357 | 13651 | 6.65 | 0.0112 |
|  | $f p$ | 4.00154 | 0.56717 | 102184 | 49.78 | <. 0001 |
|  | fn2 | 0.14857 | 0.04237 | 25242 | 12.30 | 0.0007 |
|  | fk2 | 0.01971 | 0.00280 | 102002 | 49.69 | <. 0001 |
|  | sn | -1.06743 | 0.42018 | 13249 | 6.45 | 0.0125 |
|  | sp | 3.83163 | 1.24061 | 19582 | 9.54 | 0.0025 |
|  | fnsn | 0.08440 | 0.02124 | 32402 | 15.78 | 0.0001 |
|  | fpsp | -0.04409 | 0.01676 | 14203 | 6.92 | 0.0098 |
|  | $\mathrm{R}^{2}=0.9568$ |  |  |  |  |  |
| III | Intercept | 3294.19380 | 547.93082 | 64718 | 36.14 | <. 0001 |
|  | rep | 46.35348 | 9.09190 | 46541 | 25.99 | <. 0001 |
|  | $f p$ | 6.56269 | 0.79086 | 123294 | 68.86 | <. 0001 |
|  | fn2 | 0.19351 | 0.03943 | 43119 | 24.08 | <. 0001 |
|  | fp2 | -0.02584 | 0.01020 | 11496 | 6.42 | 0.0127 |
|  | fk2 | 0.01935 | 0.00335 | 59900 | 33.45 | <. 0001 |
|  | sp | -4.96817 | 2.89385 | 5277.37104 | 2.95 | 0.0889 |
|  | sk | -10.98829 | 3.24231 | 20565 | 11.49 | 0.0010 |
|  | sp2 | 0.11934 | 0.03467 | 21215 | 11.85 | 0.0008 |
|  | sk2 | 0.01603 | 0.00480 | 19933 | 11.13 | 0.0012 |
|  | fnsn | 0.02570 | 0.00530 | 42027 | 23.47 | <. 0001 |
|  | $\begin{aligned} & \text { fpsp } \\ & R^{2}=0.963 \end{aligned}$ | -0.07331 | 0.01771 | 30681 | 17.14 | <. 000 |
| IV | Intercept | 1538.59282 | 71.10050 | 517695 | 468.28 | <. 0001 |
|  | rep | 29.88696 | 5.54109 | 32162 | 29.09 | <. 0001 |
|  | fn | -9.50767 | 3.63444 | 7565.60746 | 6.84 | 0.0102 |
|  | $f \mathrm{p}$ | 5.67328 | 0.59888 | 99213 | 89.74 | <. 0001 |
|  | fn2 | 0.16626 | 0.03139 | 31007 | 28.05 | <. 0001 |
|  | fp2 | -0.01673 | 0.00771 | 5201.52535 | 4.70 | 0.0323 |
|  | fk2 | 0.01645 | 0.00346 | 24916 | 22.54 | <. 0001 |
|  | sn | -0.67354 | 0.31262 | 5131.73450 | 4.64 | 0.0335 |
|  | sp2 | 0.08764 | 0.01141 | 65225 | 59.00 | <. 0001 |
|  | fnsn | 0.05352 | 0.01603 | 12317 | 11.14 | 0.0012 |
|  | fpsp | -0.09284 | 0.01446 | 45562 | 41.21 | <. 0001 |
|  | $f \mathrm{ffp}$ | 0.08481 | 0.01063 | 70402 | 63.68 | <. 0001 |
|  | $f \mathrm{ffk}$ | 0.03681 | 0.00994 | 15152 | 13.71 | 0.0003 |
|  | fpfk | -0.00841 | 0.00496 | 3171.05335 | 2.87 | 0.0933 |
|  | $\mathrm{R}^{2}=0.977$ |  |  |  |  |  |

## Table 5.2.10 Estimated ridge of maximum yield

## Centre: Hyderabad Crop: Groundnut Year: 199

Average STV* of the Site: $\mathbf{S N}=240.45 \mathbf{K g} ; \mathbf{S P}=33.56 \mathbf{K g} ; \mathbf{S K}=346.84 \mathbf{~ K g}$

| Coded | Estimated | Standard | Uncoded Factor Values |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Radius | yield | Error | fn | $f p$ | fk |
| 0.0 | 1782.147131 | 20.418236 | 15.000000 | 30.000000 | 30.000000 |
| 0.1 | 1804.682032 | 20.297740 | 16.352773 | 31.168540 | 30.560830 |
| 0.2 | 1828.101016 | 20.060524 | 17.720389 | 32.271697 | 31.112352 |
| 0.3 | 1852.413794 | 19.724917 | 19.099955 | 33.319481 | 31.656058 |
| 0.4 | 1877.628104 | 19.321658 | 20.489238 | 34.320079 | 32.193171 |
| 0.5 | 1903.750175 | 18.896744 | 21.886496 | 35.280219 | 32.724694 |
| 0.6 | 1930.785065 | 18.514376 | 23.290361 | 36.205458 | 33.251453 |
| 0.7 | 1958.736921 | 18.258641 | 24.699744 | 37.100410 | 33.774129 |
| 0.8 | 1987.609173 | 18.231424 | 26.113772 | 37.968935 | 34.293291 |
| 0.9 | 2017.404676 | 18.543523 | 27.531741 | 38.814277 | 34.809410 |
| 1.0 | 2048.125826 | 19.298247 | 28.953074 | 39.639181 | 35.322885 |

Table 5.2.11 Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure
(With New Variables FNFP,FNFK AND FPFK)
CENTRE: HYDERABAD CROP: GROUNDNUT YEAR :RABI 1997-98

| Models | Variable | Parameter <br> Estimate | Standard Error Type | II SS F Valu | $\mathrm{Pr}>\mathrm{F}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III(b) | Intercept | 1272.53139 | 15.90160 | 7422029 | 6404.06 | <. 0001 |
|  | fn | -3.79885 | 2.17765 | 3526.89999 | 3.04 | 0.0839 |
|  | $f \mathrm{p}$ | 5.16264 | 40.57570 | 93200 | 80.42 | <. 0001 |
|  | fn2 | 0.16194 | 0.03136 | 30910 | 26.67 | <.0001 |
|  | fp2 | -0.01961 | 0.00781 | 7311.65508 | 6.31 | 0.0135 |
|  | fk2 | 0.01543 | 0.00355 | 21949 | 18.94 | <. 0001 |
|  | sp | 9.38610 | 0.53810 | 352626 | 304.26 | <.0001 |
|  | fnsn | 0.02541 | 0.00898 | 9291.19676 | 8.02 | 0.0055 |
|  | fpsp | -0.08988 | 0.01274 | 57691 | 49.78 | <. 0001 |
|  | $f \mathrm{ffp}$ | 0.10452 | 20.01082 | 108064 | 93.24 | <. 0001 |
|  | $f \mathrm{ffk}$ | 0.03977 | 0.01018 | 17667 | 15.24 | 0.0002 |
|  | $\mathrm{R}^{2}=0.9761$ |  | $4 \quad 0.00507$ | 5199.62381 | 4.49 | 0.0365 |
| III(b) (with repl.) | Intercept | 1418.35789 | 76.08580 | 388946 | 347.51 | <. 0001 |
|  | rep | 14.92075 | 7.20201 | 4803.94971 | 4.29 | 0.0407 |
|  | fn | -8.79548 | 3.66917 | 6431.42552 | 5.75 | 0.0183 |
|  | fp | 4.96704 | 0.57275 | 84175 | 75.21 | <. 0001 |
|  | fn2 | 0.15109 | 0.03144 | 25849 | 23.09 | <. 0001 |
|  | fp2 | -0.01752 | 0.00776 | 5710.45413 | 5.10 | 0.0259 |
|  | fk2 | 0.01582 | 20.00349 | 22975 | 20.53 | <. 0001 |
|  | sn | -0.59052 | 0.31713 | 3880.65470 | 3.47 | 0.0654 |
|  | sp | 7.65813 | 1.01454 | 63772 | 56.98 | <. 0001 |
|  | fnsn | 0.05016 | 0.01623 | 10688 | 9.55 | 0.0026 |
|  | fpsp | -0.07972 | 20.01340 | 39582 | 35.36 | <. 0001 |
|  | $f \mathrm{ffp}$ | 0.09646 | - 0.01127 | 82050 | 73.31 | <. 0001 |
|  | $f \mathrm{ffk}$ | 0.03942 | 20.01001 | 17360 | 15.51 | 0.0001 |
|  | $\mathbf{R}^{\mathbf{2}}=0.9773{ }^{-0.00988}$ |  | 0.00500 | 4380.67609 | 3.91 | 0.0505 |
|  |  |  |  |  |  |  |

Table 5.2.12: Parameter estimates along with standard errors for response surface models using different number of variables
Centre: Maruteru Crop- Rice Year: Rabi-1994


Table 5.2.13 : Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure

Centre: Maruteru Crop- Rice Year: Rabi-1994


Table 5.2.14: Parameter estimates along with standard errors for response surface models using different number of Variables (models include replication)

Centre: Maruteru Crop- Rice Year: Rabi-1994

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 2312.04700 | 136.34159 | 4438.04982 | 1106.40188 | 4354.36440 | 4146.44114 | 4914.73600 | 4224.55148 |
| Replication | -93.35333 | 32.58865 | -122.66207 | 58.35131 | -123.52856 | 59.01695 | -121.94818 | 59.67559 |
| fn | 37.62341 | 3.48287 | 12.05322 | 8.14538 | 18.80344 | 16.66643 | 20.53019 | 17.15358 |
| fp | 4.48754 | 5.08077 | -2.25110 | 4.81408 | -2.30226 | 4.94995 | 0.38190 | 5.74549 |
| fk | 14.24206 | 5.08077 | 14.41097 | 9.03550 | 13.91691 | 9.14814 | 14.65878 | 9.77755 |
| $\mathrm{fn}^{2}$ | -0.10337 | 0.02176 | -0.15537 | 0.02172 | -0.14782 | 0.02512 | -0.13804 | 0.02757 |
| $\mathrm{fp}^{2}$ | 0.03002 | 0.05078 | 0.08728 | 0.04843 | 0.08964 | 0.04911 | 0.08609 | 0.04967 |
| $\mathrm{fk}^{2}$ | -0.10214 | 0.05078 | -0.10898 | 0.04803 | -0.11431 | 0.04888 | -0.11134 | 0.04960 |
| sn | ------- | --- | -5.76489 | 3.41233 | -13.86675 | 25.21412 | -16.55538 | 25.75826 |
| sp | ------- |  | 8.56396 | 4.19771 | 5.01924 | 9.67433 | 5.55517 | 9.80632 |
| sk | ------- | ------ | -2.12495 | 1.41760 | 4.88814 | 8.45974 | 3.33556 | 8.70236 |
| $\mathrm{sn}{ }^{2}$ | ------- | ------- | ------- | ------- | 0.01553 | 0.04330 | 0.02036 | 0.04431 |
| sp ${ }^{2}$ | ------- | ------- | ------- | ------ | 0.03419 | 0.08717 | 0.02458 | 0.08902 |
| sk ${ }^{2}$ | ------- | ------- | -- | ---- | -0.01005 | 0.01206 | -0.00720 | 0.01245 |
| $f n^{*}$ n | ------- | ------- | 0.09671 | 0.02911 | 0.07202 | 0.05808 | 0.06371 | 0.05959 |
| fp*sp | ------- | ------- | -0.07757 | 0.05853 | -0.07934 | 0.06467 | -0.07361 | 0.06609 |
| fk*sk | ------- | ------- | 0.00479 | 0.02508 | 0.00748 | 0.02551 | 0.00159 | 0.03202 |
| $f n^{* f p}$ | -0.06859 | 0.02733 | ------- | ------- | ------- | ------- | -0.03142 | 0.02781 |
| $f n^{* f k}$ | 0.02478 | 0.02733 | ------- | ------- | ------- | ------- | 0.00830 | 0.02932 |
| fp*fk | -0.01725 | 0.03555 | ------ | -- | --- | ------- | 0.00593 | 0.04019 |
| $\mathrm{R}^{2}$ | 0.8930 |  | 0.9110 |  | 0.9119 |  | 130 |  |

Table 5.2.15: Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure
Centre: Maruteru Crop- Rice Year: Rabi-1994

| Model | Variable | Parameter Estimate | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 2302.01125 | 134.63073 | 45902519 | 292.37 | <. 0001 |
|  | rep | -93.35333 | 32.35262 | 1307227 | 8.33 | 0.0047 |
|  | $f \mathrm{f}$ | 37.10933 | 3.20897 | 20996443 | 133.73 | <. 0001 |
|  | $f p$ | 5.90616 | 2.87473 | 662714 | 4.22 | 0.0423 |
|  | $f \mathrm{k}$ | 15.90472 | 4.18127 | 2271668 | 14.47 | 0.0002 |
|  | fn2 | -0.09668 | 0.01949 | 3861774 | 24.60 | <. 0001 |
|  | fk2 | -0.10110 | 0.05039 | 631997 | 4.03 | 0.0472 |
|  | fnfp | -0.06608 | 0.02691 | 947064 | 6.03 | 0.0156 |
|  | $\mathrm{R}^{2}=0.8916$ |  |  |  |  |  |
| II | Intercept | 5489.29173 | 657.98108 | 9414055 | 69.60 | <. 0001 |
|  | rep | -127.35869 | 57.37587 | 666453 | 4.93 | 0.0285 |
|  | $f \mathrm{k}$ | 16.23044 | 3.87577 | 2371999 | 17.54 | <. 0001 |
|  | fn2 | -0.15944 | 0.02051 | 8176936 | 60.45 | <. 0001 |
|  | fp2 | 0.08340 | 0.03243 | 894804 | 6.62 | 0.0115 |
|  | fk2 | -0.11166 | 0.04699 | 763768 | 5.65 | 0.0192 |
|  | sn | -9.70584 | 1.99334 | 3206829 | 23.71 | <. 0001 |
|  | sp | 10.57695 | 3.93072 | 979370 | 7.24 | 0.0083 |
|  | sk | -1.84200 | 1.03681 | 426927 | 3.16 | 0.0784 |
|  | $\begin{aligned} & \text { fnsn } \\ & R^{2}=0.9091 \end{aligned}$ | 0.13480 | 0.01180 | 17661474 | 130.57 | <. 0001 |
| III | Intercept | 5155.17043 | 578.09304 | 10734960 | 79.52 | <. 0001 |
|  | rep | -127.09327 | 57.30428 | 664020 | 4.92 | 0.0286 |
|  | $f \mathrm{f}$ | 16.28110 | 3.87160 | 2387239 | 17.68 | <. 0001 |
|  | fn2 | -0.15864 | 0.02048 | 8102635 | 60.02 | <. 0001 |
|  | fp2 | 0.08320 | 0.03240 | 890293 | 6.60 | 0.0116 |
|  | fk2 | -0.11210 | 0.04691 | 770929 | 5.71 | 0.0186 |
|  | sn | -9.61496 | 1.98522 | 3166574 | 23.46 | <. 0001 |
|  | sp | 10.52420 | 3.92763 | 969233 | 7.18 | 0.0085 |
|  | sk2 | -0.00269 | 0.00147 | 456130 | 3.38 | 0.0688 |
|  | fnsn | 0.13430 | 0.01174 | 17653392 | 130.77 | <. 0001 |
|  |  | -0.10485 | 0.04733 | 662341 | 4.91 | 0.0288 |
|  | $\mathrm{R}^{2}=0.9093$ |  |  |  |  |  |
| IV | Intercept | 2432.25543 | 151.08088 | 35027117 | 259.18 | <. 0001 |
|  | rep | -55.57075 | 32.75439 | 389008 | 2.88 | 0.0926 |
|  | fn | 24.70646 | 4.46736 | 4133557 | 30.59 | <. 0001 |
|  | $f \mathrm{k}$ | 16.14938 | 3.87793 | 2343776 | 17.34 | <.0001 |
|  | fn2 | -0.13325 | 0.01805 | 7361943 | 54.47 | <. 0001 |
|  | fp2 | 0.06197 | 0.02763 | 679692 | 5.03 | 0.0269 |
|  | fk2 | -0.10747 | 0.04704 | 705520 | 5.22 | 0.0242 |
|  | sk2 | -0.00249 | 0.00144 | 405195 | 3.00 | 0.0862 |
|  | fnsn | 0.04997 | 0.01196 | 2359065 | 17.46 | <. 0001 |
|  | fnfp | -0.04288 | 0.02191 | 517433 | 3.83 | 0.0529 |
|  | $\mathrm{R}^{2}=0.9084$ |  |  |  |  |  |

Table 5.2.16 : Estimated ridge of maximum yield Centre: Maruteru (Hyderabad) Crop: Rice Year: 1994

Average STV* of the Site: $\mathrm{SN}=334.82 \mathrm{Kg} ; \mathrm{SP}=54.30 \mathrm{Kg} ; \mathrm{SK}=346.37 \mathrm{Kg}$

| Coded | Estimated | Standard | Uncoded Factor Values |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Radius | Yield | Error | fn | fp | fk |
| 0.0 | 4816.166011 | 92.983229 | 75.000000 | 40.000000 | 40.000000 |
| 0.1 | 4959.066187 | 91.659901 | 82.306326 | 40.175470 | 40.885936 |
| 0.2 | 5089.543958 | 90.680606 | 89.555785 | 40.296774 | 41.909562 |
| 0.3 | 5207.759986 | 89.907002 | 96.728358 | 40.343527 | 43.096714 |
| 0.4 | 5313.925126 | 89.349541 | 103.796470 | 40.284766 | 44.477402 |
| 0.5 | 5408.319691 | 89.151290 | 110.722201 | 40.071809 | 46.084588 |
| 0.6 | 5491.321773 | 89.551571 | 117.453557 | 39.625232 | 47.950096 |
| 0.7 | 5563.451148 | 90.820730 | 123.918995 | 38.810728 | 50.094093 |
| 0.8 | 5625.443701 | 93.159009 | 130.016843 | 37.397431 | 52.500203 |
| 0.9 | 5678.388127 | 96.555567 | 135.590960 | 35.013582 | 55.062034 |
| 1.0 | 5723.945073 | 100.648392 | 140.401762 | 31.243843 | 57.511417 |

Table 5.3.1: Parameter estimates along with standard errors for response surface models using different number of variables
Centre: Kalyani Crop: Rape Year: Rabi 1998

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 343.80097 | 47.58357 | -347.82375 | 248.56684 | 26.93311 | 995.37689 | 60.69267 | 1037.95129 |
| fn | 7.05765 | 2.21874 | 5.89325 | 3.71692 | 7.17790 | 3.74138 | 7.33274 | 3.83392 |
| fp | 7.43661 | 4.01841 | 9.16856 | 2.49668 | 9.81957 | 2.50608 | 10.31630 | 2.82640 |
| $f \mathrm{f}$ | 0.83494 | 6.89677 | 4.90971 | 4.06540 | 5.20279 | 4.05996 | 3.55462 | 5.28043 |
| $\mathrm{fn}^{2}$ | -0.02136 | 0.02343 | -0.01420 | 0.01101 | -0.01405 | 0.01101 | -0.01817 | 0.01498 |
| $f p^{2}$ | -0.03190 | 0.06568 | -0.05227 | 0.02975 | -0.06192 | 0.03033 | -0.03854 | 0.04326 |
| $\mathrm{fk}^{2}$ | -0.01210 | 0.12503 | -0.00833 | 0.05724 | -0.02369 | 0.05751 | -0.03083 | 0.08037 |
| sn | ------- | ------- | 1.09830 | 1.16664 | -1.42477 | 8.38998 | -1.70749 | 8.72944 |
| sp | ------- | ------- | 10.66345 | 3.60289 | 33.74077 | 10.68614 | 33.90575 | 10.81718 |
| sk | - | ------- | 0.79134 | 0.55115 | -2.62186 | 1.98025 | -2.50393 | 2.01267 |
| $\mathrm{sn}^{2}$ | - | -- | ------- | ------- | 0.00711 | 0.01628 | 0.00743 | $0.01691$ |
| sp ${ }^{2}$ | - | ------- | --- |  | -0.45803 | 0.19187 | $-0.45556$ | 0.19458 |
| sk ${ }^{2}$ | ------- | ------- | ------- | ------ | 0.00617 | 0.00361 | 0.00592 | 0.00366 |
| $f n^{*}$ sn | ------- | ------- | 0.00268 | 0.01343 | -0.00337 | 0.01356 | -0.00324 | 0.01383 |
| $f p * s p$ | ------ | ------ | -0.07201 | 0.06003 | -0.06024 | 0.06012 | -0.05917 | 0.06106 |
| fk*sk | ------- | ------- | -0.01090 | 0.01175 | -0.00788 | 0.01166 | -0.00824 | 0.01179 |
| $f n^{*} \mathrm{fp}$ | -0.00809 | 0.05089 | ------- | ------- | ------- | ------- | -0.01777 | 0.03280 |
| $f n^{* f k}$ | 0.04193 | 0.09729 | ------- | ------- | ------- | ------- | 0.04960 | 0.06227 |
| fp*fk | -0.03853 | 0.09600 | - | ------ | ------- | ------- | -0.04493 | 0.06236 |
| $\mathrm{R}^{2}$ | 0.6674 |  | 0.8702 |  | . 8776 |  | 789 |  |

Table 5.3.2: Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure Centre: Kalyani Crop: Rape Year: Rabi 1998

| Model | Variable | Parameter <br> Estimates | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 351.09283 | 42.76633 | 4253061 | 67.40 | <. 0001 |
|  | fn | 5.40743 | 0.70910 | 3669728 | 58.15 | <. 0001 |
|  | fp | 9.18525 | 3.03397 | 578393 | 9.17 | 0.0031 |
|  | fp2 | -0.07132 | 0.03998 | 200863 | 3.18 | 0.0772 |
|  | $\mathrm{R} 2=0.6608$ |  |  |  |  |  |
| II | ```Intercept fn fp fp2``` | -398.74846 | 163.24555 | 157672 | 5.97 | 0.0162 |
|  |  | 5.34067 | 0.46114 | 3544530 | 134.13 | <.0001 |
|  |  | 11.63473 | 2.12843 | 789652 | 29.88 | <. 0001 |
|  |  | -0.07738 | 0.02615 | 231483 | 8.76 | 0.0038 |
|  | sn | 1.77373 | 0.73593 | 153512 | 5.81 | 0.0177 |
|  | sp | 14.08767 | 2.46787 | 861143 | 32.59 | <. 0001 |
|  | fpsp | -0.08948 | 0.04431 | 107767 | 4.08 | 0.0460 |
|  | R2 = 0.8619 |  |  |  |  |  |
| III | Intercept | -149.03267 | 66.58413 | 130669 | 5.01 | 0.0273 |
|  | fn | 5.16203 | 0.45745 | 3321205 | 127.33 | <. 0001 |
|  | fp | 11.61397 | 2.11353 | 787583 | 30.20 | <. 0001 |
|  | fp2 | -0.07227 | 0.02577 | 205096 | 7.86 | 0.0060 |
|  | sp | 32.90673 | 5.81538 | 835151 | 32.02 | <. 0001 |
|  | sp2 | -0.31151 | 0.11553 | 189618 | 7.27 | 0.0082 |
|  | fpsp | -0.10374 | 0.04343 | 148837 | 5.71 | 0.0187 |
|  | $\mathrm{R} 2=0.8637$ |  |  |  |  |  |
| IV | Intercept | -149.03267 | 66.58413 | 130669 | 5.01 | 0.0273 |
|  | $f \mathrm{f}$ | 5.16203 | 0.45745 | 3321205 | 127.33 | <.0001 |
|  |  | 11.61397 | 2.11353 | 787583 | 30.20 | <.0001 |
|  | ${ }_{\text {fp }}$ | -0.07227 | 0.02577 | 205096 | 32.02 | 0.0060 |
|  | sp | 32.90673 | 5.81538 | 835151 |  | <.0001 |
|  | $\begin{aligned} & \text { sp2 } \\ & \text { fpsp } \\ & \text { R2 }=0.8637 \end{aligned}$ | $\begin{aligned} & -0.31151 \\ & -0.10374 \end{aligned}$ | $\begin{aligned} & 0.11553 \\ & 0.04343 \end{aligned}$ | 189618 | 7.27 | $\begin{aligned} & 0.0082 \\ & 0.0187 \end{aligned}$ |
|  |  |  |  | $148837$ | 5.71 |  |
|  |  |  |  |  |  |  |

Table 5.3.3: Parameter estimates along with standard errors for response surface models using different number of Variables (models include replication)
Centre: Kalyani Crop: Rape Year: Rabi 1998

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | -79.98630 | 45.89924 | -312.46419 | 245.82168 | 60.62145 | 993.93133 | 121.96456 | 1037.32088 |
| Replication | 169.19298 | 13.77231 | 165.60829 | 85.17398 | 114.62808 | 98.26403 | 116.61069 | 100.22594 |
| fn | 6.93728 | 1.41184 | 6.17856 | 3.66874 | 6.92234 | 3.74079 | 7.16608 | 3.82933 |
| fp | 8.15385 | 2.55761 | 8.93886 | 2.46517 | 9.66445 | 2.50492 | 10.33922 | 2.82111 |
| fk | -0.10652 | 4.38914 | 4.48692 | 4.01538 | 4.91059 | 4.06009 | 2.80735 | 5.30941 |
| $\mathrm{fn}^{2}$ | -0.02057 | 0.01491 | -0.01429 | 0.01086 | -0.01369 | 0.01100 | -0.01846 | 0.01495 |
| $f p^{2}$ | -0.02649 | 0.04179 | -0.05017 | 0.02936 | -0.06045 | 0.03029 | -0.03710 | 0.04320 |
| $\mathrm{fk}^{2}$ | -0.01542 | 0.07956 | -0.00741 | 0.05645 | -0.02070 | 0.05746 | -0.03557 | 0.08032 |
| sn | ----- | ----- | 0.96573 | 1.15261 | -1.51117 | 8.37459 | -2.03143 | 8.71734 |
| sp | -- | ------ | 3.96929 | 4.94769 | 22.75775 | 14.22710 | 22.65144 | 14.49603 |
| sk | ------ | ------ | -0.38990 | 0.81520 | -3.04905 | 2.01018 | -2.93727 | 2.04309 |
| $\mathrm{sn}^{2}$ | ------ | ------ | 0.3899 | 0.81520 | 0.00704 | 0.01625 | 0.00786 | 0.01688 |
| sp ${ }^{2}$ |  | ------ | ------- | ------- | -0.34689 | 0.21391 | -0.34298 | 0.21698 |
| sk ${ }^{2}$ | ------ | ------ | ------ | ------ | 0.00568 | 0.00363 | 0.00544 | 0.00368 |
| fn*sn |  |  | 0.00199 | 0.01325 | -0.00202 | 0.01358 | -0.00189 | 0.01385 |
| $f p * s p$ |  |  | -0.06878 | 0.05923 | -0.05970 | 0.06001 | -0.05833 | 0.06095 |
| fk*sk |  |  | -0.00889 | 0.01163 | -0.00728 | 0.01165 | -0.00760 | 0.01178 |
| $f n^{* f p}$ | -0.01838 | 0.03239 | ------ | ------ | ------ | ------ | -0.02081 | 0.03284 |
| $f n^{*} \mathrm{fk}$ | 0.05897 | 0.06192 |  |  | ------ | ------ | 0.05518 | 0.06234 |
| fp*fk | -0.04761 | 0.06109 | ------ | ------ | ------ | ------ | -0.03832 | 0.06250 |
| $\mathrm{R}^{2}$ | 0.8667 |  | 0.8750 |  | 8794 | 0 |  |  |

Table 5.3.4: Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure
Centre: Kalyani Crop: Rape Year: Rabi 1998

| Model | Variable | Parameter Estimates | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | -76.45960 | 44.39470 | 76431 | 2.97 | 0.0880 |
|  | rep | 168.90123 | 13.56883 | 3992523 | 154.95 | <.0001 |
|  | $f \mathrm{f}$ | 6.95271 | 1.23839 | 812193 | 31.52 | <.0001 |
|  | $f p$ | 7.95343 | 2.08385 | 375356 | 14.57 | 0.0002 |
|  | fn2 | -0.01966 | 0.01167 | 73158 | 2.84 | 0.0950 |
|  | fp2 | -0.05393 | 0.02795 | 95934 | 3.72 | 0.0564 |
|  | fnfk | 0.02132 | 0.01217 | 79136 | 3.07 | 0.0826 |
|  | $\mathrm{R} 2=0.8653$ |  |  |  |  |  |
| II | Intercept | -146.77631 | 55.22253 | 179377 | 7.06 | 0.0091 |
|  | rep | 198.62906 | 19.08184 | 2751273 | 108.35 | <.0001 |
|  | $f \mathrm{f}$ | 5.39013 | 0.45055 | 3634120 | 143.12 | <.0001 |
|  | $f p$ | 11.13507 | 2.06996 | 734765 | 28.94 | <.0001 |
|  | fp2 | -0.07069 | 0.02540 | 196766 | 7.75 | 0.0064 |
|  | fpsp | -0.08846 | 0.04050 | 121106 | 4.77 | 0.0312 |
|  | $\mathrm{R} 2=0.8660$ |  |  |  |  |  |
| III | Intercept | -149.03267 | 66.58413 | 130669 | 5.01 | 0.0273 |
|  | fn | 5.16203 | 0.45745 | 3321205 | 127.33 | <.0001 |
|  | $f p$ | 11.61397 | 2.11353 | 787583 | 30.20 | <.0001 |
|  | fp2 | -0.07227 | 0.02577 | 205096 | 7.86 | 0.0060 |
|  | sp | 32.90673 | 5.81538 | 835151 | 32.02 | <.0001 |
|  | sp2 | -0.31151 | 0.11553 | 189618 | 7.27 | 0.0082 |
|  | fpsp | -0.10374 | 0.04343 | 148837 | 5.71 | 0.0187 |
|  | $\mathbf{R 2}=0.8637$ |  |  |  |  |  |
| IV | Intercept | -149.03267 | 66.58413 | 130669 | 5.01 | 0.0273 |
|  | $f \mathrm{n}$ | 5.16203 | 0.45745 | 3321205 | 127.33 | <.0001 |
|  | $f p$ | 11.61397 | 2.11353 | 787583 | 30.20 | <.0001 |
|  | fp2 | -0.07227 | 0.02577 | 205096 | 7.86 | 0.0060 |
|  | sp | 32.90673 | 5.81538 | 835151 | 32.02 | <.0001 |
|  | sp2 | -0.31151 | 0.11553 | 189618 | 7.27 | 0.0082 |
|  | fpsp | -0.10374 | 0.04343 | 148837 | 5.71 | 0.0187 |
|  | $\mathrm{R} 2=0.8637$ |  |  |  |  |  |

## Table 5.3.5: Estimated ridge of maximum yield

## Centre: Kalyani Crop: Rape Year: Rabi 1998



| Coded | Estimated | Standard | Uncoded Factor Values |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Radiu | Yield | Error | fn | fp | fk |
| 0.0 | 959.091901 | 40.222034 | 62.500000 | 37.500000 | 25.000000 |
| 0.1 | 992.574239 | 39.796506 | 68.169518 | 39.012873 | 25.299687 |
| 0.2 | 1024.629643 | 39.181230 | 73.854284 | 40.457513 | 25.696658 |
| 0.3 | 1055.305767 | 38.377886 | 79.552343 | 41.814449 | 26.204873 |
| 0.4 | 1084.661400 | 37.475157 | 85.259027 | 43.060089 | 26.839687 |
| 0.5 | 1112.768842 | 36.649472 | 90.965644 | 44.166779 | 27.617132 |
| 0.6 | 1139.716224 | 36.163232 | 96.658036 | 45.103711 | 28.552517 |
| 0.7 | 1165.609186 | 36.348545 | 102.315456 | 45.839161 | 29.658254 |
| 0.8 | 1190.571136 | 37.564163 | 107.910513 | 46.344265 | 30.941106 |
| 0.9 | 1214.741192 | 40.130065 | 113.411014 | 46.597832 | 32.399600 |
| 1.0 | 1238.269388 | 44.272421 | 118.783902 | 46.590747 | 34.022746 |
| * STV- | Test Value |  |  |  |  |

Table 5.4.1 : Parameter estimates along with standard errors for response surface models using different number of variables

Centre: Coimbatore Crop: Onion Year: Kharif 1998

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error |
| Intercept | 9671.87137 | 332.42879 | 221.64644 | 3361.13837 | -32874.000 | 20684 | -35431.0000 | 20460.000 |
| fn | 89.78812 | 21.90000 | 144.44157 | 44.61604 | 144.20536 | 44.70592 | 161.83035 | 45.03223 |
| fp | 35.54210 | 26.74540 | 50.54445 | 17.54069 | 48.72301 | 17.32145 | 9.86097 | 24.48064 |
| fk | 41.78605 | 28.96532 | 30.27220 | 53.80214 | 34.21688 | 54.50805 | 59.25698 | 55.52279 |
| $\mathrm{fn}^{2}$ | -0.51638 | 0.30968 | -0.22709 | 0.08876 | -0.25863 | 0.08868 | -0.60592 | 0.26810 |
| $f p^{2}$ | -0.76869 | 0.25968 | -0.48976 | 0.15081 | -0.47696 | 0.14883 | -0.83662 | 0.22030 |
| $\mathrm{fk}^{2}$ | -0.10443 | 0.50258 | -0.15826 | 0.31041 | -0.18399 | 0.30637 | -0.07936 | 0.42892 |
| sn | ------- | -------- | 38.96059 | 21.51933 | 277.30729 | 195.31711 | 258.79753 | 193.18736 |
| sp | -------- | -------- | -17.93141 | 34.03324 | -45.92910 | 95.54974 | -67.72576 | 94.94738 |
| sk | --------- | -------- | 5.88459 | 10.06137 | 69.56207 | 80.26440 | 102.36337 | 80.83089 |
| sn ${ }^{2}$ | -------- | -------- | -------- | ------- | -0.59002 | 0.45479 | -0.54364 | 0.44968 |
| sp ${ }^{2}$ | ------- | -------- | ------- | ------- | 0.33277 | 1.20005 | 0.47418 | 1.19523 |
| sk ${ }^{2}$ | -------- | ------- | --------- | - | -0.09830 | 0.13970 | -0.15246 | 0.14066 |
| $f n^{*}$ n | -------- | ------- | -0.33947 | 0.19956 | -0.31435 | 0.19979 | -0.27975 | 0.19984 |
| fp*sp | -------- | ------- | 0.54724 | 0.33650 | 0.55810 | 0.33350 | 0.53653 | 0.33093 |
| fk*sk | ------ | -------- | -0.01256 | 0.18603 | -0.02164 | 0.18927 | -0.03758 | 0.18744 |
| fn*fp | 0.72290 | 0.49678 | -------- | -------- | -------- | -------- | 0.87803 | 0.42598 |
| $f n^{* f k}$ | -0.20525 | 0.52386 | -------- | -------- | ------- | -------- | -0.34725 | 0.44406 |
| fp*fk | -0.02342 | 0.42628 | ------- | ------- | ------- | ------- | 0.00782 | 0.36033 |
| $\mathbf{R}^{2}$ | 0.8248 |  | 0.8757 |  | 0.8839 |  | 912 |  |

Table 5.4.2: Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure

Centre: Coimbatore Crop: Onion Year: Kharif 1998

| $\begin{aligned} & \text { Model } \\ & \text { I } \end{aligned}$ | Variable | Parameter Estimates | Standard Error | Type II SS | F Value | Pr > F |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Intercept | 2404.76465 | 46.31781 | 215894182 | 2695.56 | <. 0001 |
|  | fn | 8.90327 | 3.75365 | 450592 | 5.63 | 0.0195 |
|  | fp | 8.75776 | 1.48434 | 2788125 | 34.81 | <. 0001 |
|  | fk | 6.03265 | 2.60169 | 430622 | 5.38 | 0.0223 |
|  | fn2 | 0.12365 | 0.04856 | 519289 | 6.48 | 0.0123 |
|  | $\mathrm{R}^{2}=0.8868$ |  |  |  |  |  |
| II | Intercept | 1255.16960 | 2103.54181 | 488280 | 0.36 | 0.5523 |
|  | fn | 148.26011 | 37.88252 | 21005697 | 15.32 | 0.0002 |
|  | fp | 51.00616 | 16.64173 | 12882920 | 9.39 | 0.0029 |
|  | fk | 17.19944 | 7.14902 | 7937828 | 5.79 | 0.0183 |
|  | fn2 | -0.22331 | 0.08503 | 9460078 | 6.90 | 0.0102 |
|  | fp2 | -0.49031 | 0.14732 | 15191424 | 11.08 | 0.0013 |
|  | sn | 39.17665 | 9.66233 | 22545341 | 16.44 | 0.0001 |
|  | fnsn | -0.35765 | 0.16654 | 6324484 | 4.61 | 0.0345 |
|  |  | $\mathrm{R}^{2}=0.8746$ |  |  |  | 0.0811 |
| III | Intercept | -21483 | 11753 | 4435984 | 3.34 | 0.0710 |
|  | fn | 154.31179 | 37.40121 | 22601281 | 17.02 | <.0001 |
|  | $f p$ | 48.17629 | 16.43770 | 11404875 | 8.59 | 0.0043 |
|  | fk | 16.80601 | 7.03708 | 7572701 | 5.70 | 0.0191 |
|  | fn2 | -0.23905 | 0.08404 | 10742272 | 8.09 | 0.0056 |
|  | fp2 | -0.48405 | 0.14499 | 14798744 | 11.15 | 0.0012 |
|  | sn | 255.65397 | 110.55564 | 7099855 | 5.35 | 0.0231 |
|  | sn2 | -0.50938 | 0.25918 | 5128529 | 3.86 | 0.0526 |
|  | fnsn | -0.37113 | 0.16401 | 6798242 | 5.12 | 0.0262 |
|  | $\mathrm{R}^{2}=0.8800$ |  |  |  |  |  |
| IV | Intercept | -21962 | 11626 | 4651011 | 3.57 | 0.0622 |
|  | fn | 189.85173 | 33.61970 | 41560768 | 31.89 | <.0001 |
|  | fk | 19.00104 | 6.85704 | 10007440 | 7.68 | 0.0068 |
|  | fn2 | -0.72569 | 0.15107 | 30073535 | 23.08 | <.0001 |
|  | fp2 | -0.76837 | 0.20998 | 17451515 | 13.39 | 0.0004 |
|  | sn | 260.13379 | 109.35922 | 7374371 | 5.66 | 0.0196 |
|  | sn2 | -0.52042 | 0.25638 | 5370212 | 4.12 | 0.0455 |
|  | fnsn | -0.37277 | 0.16077 | 7006602 | 5.38 | 0.0228 |
|  | fpsp | 0.60763 | 0.27293 | 6459983 | 4.96 | 0.0286 |
|  |  | 0.88631 | 0.27533 | 13505475 | 10.36 | 0.0018 |
|  | $R^{2}=0.8822$ |  |  |  |  |  |

Table 5.4.3 : Parameter estimates along with standard errors for response surface models using different number of Variables (models include replication)

Centre: Coimbatore Crop: Onion Year: Kharif 1998

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 8147.71512 | 395.86434 | -930.73821 | 4260.01240 | -32733 | 20826 | -35172.000 | 20523.000 |
| Replication | 609.66250 | 109.40949 | -291.92041 | 657.65775 | -128.72182 | 744.92301 | -578.00296 | 777.95215 |
| fn | 89.78812 | 18.85254 | 149.13182 | 46.06179 | 146.39335 | 46.72774 | 172.29671 | 47.30975 |
| fp | 35.54210 | 23.02368 | 50.36217 | 17.63094 | 48.72836 | 17.42747 | 6.76850 | 24.90247 |
| $f \mathrm{f}$ | 41.78605 | 24.93469 | 25.47247 | 55.13504 | 31.04413 | 57.83359 | 48.64010 | 57.48924 |
| $\mathrm{fn}^{2}$ | -0.51638 | 0.26659 | -0.23127 | 0.08969 | -0.26029 | 0.08974 | -0.60928 | 0.26892 |
| $f p^{2}$ | -0.76869 | 0.22355 | -0.48631 | 0.15174 | -0.47618 | 0.14981 | -0.85312 | 0.22205 |
| $\mathrm{fk}^{2}$ | -0.10443 | 0.43264 | -0.16414 | 0.31220 | -0.18522 | 0.30833 | -0.01901 | 0.43777 |
| sn | ------ | ------- | 42.42323 | 22.98823 | 282.31779 | 198.64001 | 280.54614 | 195.95054 |
| sp | ------- | ------- | -8.01231 | 40.85265 | -37.44050 | 107.95836 | -32.37659 | 106.44897 |
| sk | ------- | ------- | 8.91511 | 12.19971 | 63.13070 | 88.91962 | 77.04402 | 87.93853 |
| $\mathrm{sn}^{2}$ | ------- | ------- | ------- | 12.1991 | -0.59836 | 0.46011 | -0.57903 | 0.45350 |
| sp ${ }^{2}$ | ------- | ------- | ------- | ------- | 0.28512 | 1.23847 | 0.30103 | 1.22117 |
| sk ${ }^{2}$ | ------- | ------- | ------- | ------- | -0.08466 | 0.16120 | -0.09767 | 0.15918 |
| $f n^{*}$ n | ------- | ------- | -0.35990 | 0.20575 | -0.32381 | 0.20832 | -0.32509 | 0.20951 |
| fp*sp | ------- | ------- | 0.53817 | 0.33875 | 0.55149 | 0.33771 | 0.51126 | 0.33364 |
| fk*sk | ------- | -------- | 0.00793 | 0.19255 | -0.00873 | 0.20457 | 0.02160 | 0.20416 |
| $f n^{* f p}$ | 0.72290 | 0.42765 | ------- | ------- | ------- | ------ | 0.93324 | 0.43363 |
| fn*fk | -0.20525 | 0.45097 | ------- | ------- | ------- | ------- | -0.44338 | 0.46377 |
| fp*fk | -0.02342 | 0.36696 | --- | ---- | ------- | ------- | 0.00059366 | 0.36152 |
| $\mathrm{R}^{2}$ | 0.8717 |  | 0.8760 |  | 8839 |  | 920 |  |

Table 5.4.4: Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure

## Centre: Coimbatore Crop: Onion Year: Kharif 1998

| Model | Variable | Parameter Estimates | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 1829.54647 | 29.19511 | 46491594 | 3927.05 | <. 0001 |
|  | rep | 228.06071 | 9.19581 | 7281637 | 615.07 | <.0001 |
|  | fn | 7.84231 | 1.54195 | 306237 | 25.87 | <.0001 |
|  | fp | 8.73036 | 0.57085 | 2769038 | 233.90 | <.0001 |
|  | $f \mathrm{k}$ | 10.68243 | 2.58167 | 202697 | 17.12 | <.0001 |
|  | fn2 | 0.13632 | 0.01976 | 563203 | 47.57 | <. 0001 |
|  | $\begin{aligned} & \mathrm{fk} 2 \\ & \mathrm{R}^{2}=0.9874 \end{aligned}$ | -0.11698 | 0.05988 | 45187 | 3.82 | 0.0534 |
| II | Intercept | 1255.16960 | 2103.54181 | 488280 | 0.36 | 0.5523 |
|  | fn | 148.26011 | 37.88252 | 21005697 | 15.32 | 0.0002 |
|  | fp | 51.00616 | 16.64173 | 12882920 | 9.39 | 0.0029 |
|  | fk | 17.19944 | 7.14902 | 7937828 | 5.79 | 0.0183 |
|  | fn2 | -0.22331 | 0.08503 | 9460078 | 6.90 | 0.0102 |
|  | fp2 | -0.49031 | 0.14732 | 15191424 | 11.08 | 0.0013 |
|  | sn | 39.17665 | 9.66233 | 22545341 | 16.44 | 0.0001 |
|  | fnsn | -0.35765 | 0.16654 | 6324484 | 4.61 | 0.0345 |
|  | $\begin{aligned} & \text { fpsp } \\ & \mathbf{R}^{2}=0.8746 \end{aligned}$ | 0.51435 | 0.29147 | 4270614 | 3.11 | 0.0811 |
| III | Intercept | -21483 | 11753 | 4435984 | 3.34 | 0.0710 |
|  | fn | 154.31179 | 37.40121 | 22601281 | 17.02 | <. 0001 |
|  | fp | 48.17629 | 16.43770 | 11404875 | 8.59 | 0.0043 |
|  | $f \mathrm{f}$ | 16.80601 | 7.03708 | 7572701 | 5.70 | 0.0191 |
|  | fn2 | -0.23905 | 0.08404 | 10742272 | 8.09 | 0.0056 |
|  | fp2 | -0.48405 | 0.14499 | 14798744 | 11.15 | 0.0012 |
|  | sn | 255.65397 | 110.55564 | 7099855 | 5.35 | 0.0231 |
|  | sn2 | -0.50938 | 0.25918 | 5128529 | 3.86 | 0.0526 |
|  | fnsn | -0.37113 | 0.16401 | 6798242 | 5.12 | 0.0262 |
|  | fpsp | 0.57020 | 0.28820 | 5197363 | 3.91 | 0.0511 |
|  | $\mathrm{R}^{2}=0.8800$ |  |  |  |  |  |
| IV | Intercept | -21962 | 11626 | 4651011 | 3.57 | 0.0622 |
|  | fn | 189.85173 | 33.61970 | 41560768 | 31.89 | <. 0001 |
|  | $f \mathrm{f}$ | 19.00104 | 6.85704 | 10007440 | 7.68 | 0.0068 |
|  | fn2 | -0.72569 | 0.15107 | 30073535 | 23.08 | <.0001 |
|  | fp2 | -0.76837 | 0.20998 | 17451515 | 13.39 | 0.0004 |
|  | sn | 260.13379 | 109.35922 | 7374371 | 5.66 | 0.0196 |
|  | sn2 | -0.52042 | 0.25638 | 5370212 | 4.12 | 0.0455 |
|  | fnsn | -0.37277 | 0.16077 | 7006602 | 5.38 | 0.0228 |
|  | fpsp | 0.60763 | 0.27293 | 6459983 | 4.96 | 0.0286 |
|  | fnfp $R^{2}=0.8822$ | 0.88631 | 0.27533 | 13505475 | 10.36 | 0.0018 |

Table 5.4.5 : Estimated ridge of maximum yield

## Centre: Coimbatore Crop: Onion Year: Kharif 1998

Average STV* of the Site: $\mathrm{SN}=216.01 \mathrm{Kg} ; \mathrm{SP}=32.39 \mathrm{Kg} ; \mathrm{SK}=270.15 \mathrm{Kg}$

| Coded | Estimated | Standard | Uncoded | Factor Values |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Radius | Response | Error | fn | fp | fk |
| 0.0 | 16012 | 310.533314 | 60.000000 | 45.000000 | 30.000000 |
| 0.1 | 16342 | 317.470890 | 65.804823 | 45.633220 | 30.630712 |
| 0.2 | 16638 | 320.626028 | 71.458712 | 46.838119 | 31.293382 |
| 0.3 | 16904 | 319.532193 | 76.916227 | 48.536876 | 31.974977 |
| 0.4 | 17142 | 315.310475 | 82.163855 | 50.631653 | 32.663661 |
| 0.5 | 17358 | 309.445952 | 87.211786 | 53.029752 | 33.350114 |
| 0.6 | 17551 | 303.394669 | 92.082417 | 55.655395 | 34.027225 |
| 0.7 | 17724 | 298.554359 | 96.801937 | 58.451323 | 34.689074 |
| 0.8 | 17879 | 296.323437 | 101.395931 | 61.375986 | 35.329751 |
| 0.9 | 18015 | 298.127011 | 105.887805 | 64.399877 | 35.942082 |
| 1.0 | 18134 | 305.374024 | 110.298817 | 67.502470 | 36.515969 |

Table 5.5.1 : Parameter estimates along with standard errors for response surface models using different number of variables
Centre: Hisar Crop: Wheat Year: Rabi-1993-94

| Models |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error |
| Intercept | 2439.64385 | 58.08713 | 648.23376 | 156.50099 | -363.83481 | 717.10385 | -377.17101 | 726.25693 |
| fn | 32.02411 | 2.32920 | 33.89944 | 1.73260 | 33.91798 | 1.76944 | 34.96536 | 1.99931 |
| fp | 21.33543 | 6.34733 | 28.76400 | 2.48277 | 28.91607 | 2.53137 | 27.44319 | 3.35095 |
| fk | 1.37267 | 6.71666 | 0.95261 | 4.21942 | 0.98006 | 4.23378 | 0.95432 | 4.52462 |
| $\mathrm{fn}^{2}$ | -0.09936 | 0.01751 | -0.08433 | 0.00402 | -0.08286 | 0.00417 | -0.09211 | 0.00831 |
| $f p^{2}$ | -0.21262 | 0.08671 | -0.15534 | 0.02098 | -0.15906 | 0.02146 | -0.18758 | 0.04081 |
| $\mathrm{fk}^{2}$ | -0.05730 | 0.12895 | -0.03960 | 0.04081 | -0.04910 | 0.04144 | -0.06449 | 0.06052 |
| sn | ------ | ------ | 7.51056 | 1.63404 | 22.31978 | 10.17250 | 22.08820 | 10.33625 |
| sp | ------ | ------ | 29.00744 | 4.12444 | 13.69272 | 12.58847 | 14.02952 | 12.79377 |
| sk | ------ | ------ | 0.51785 | 0.25295 | 0.94089 | 1.17575 | 1.11229 | 1.18991 |
| $\mathrm{sn}{ }^{2}$ | ------ | ------ |  | 㖪 | -0.04786 | 0.03253 | -0.04654 | 0.03303 |
| sp ${ }^{2}$ | ------ | ------ | ------ | ------ | 0.29985 | 0.29291 | 0.27621 | 0.29653 |
| sk ${ }^{2}$ | ------ | ------ | ------ | ------ | -0.00051974 | 0.00148 | -0.00075248 | 0.00150 |
| fn*sn | ------ | ------ | -0.02231 | 0.01162 | -0.02439 | 0.01198 | -0.02569 | 0.01210 |
| fp*sp | ------ | ------ | -0.32602 | 0.07407 | -0.31740 | 0.07523 | -0.31121 | 0.07596 |
| fk*sk | ------ | ------ | 0.00193 | 0.01031 | 0.00281 | 0.01041 | 0.00349 | 0.01051 |
| $f n^{* f p}$ | 0.04813 | 0.07706 | ------ | ------ | ------ | ------ | 0.02993 | 0.03605 |
| $f{ }^{\text {f*fk }}$ | 0.00163 | 0.07438 | ------ | ------ | ------ | ------ | 0.00321 | 0.03493 |
| fp*fk | 0.02479 | 0.10056 | ------ | ------ | ------ | ------ | 0.00415 | 0.04791 |
| $\mathbf{R}^{2}$ | 0.9456 |  | 0.9889 |  | 0.9892 |  | 0.9894 |  |

## Table 5.5.2: Parameter estimates along with standard errors for remaining significant variables in different models using backward elimination procedure

Centre: Hisar Crop: Wheat Year: Rabi-1993-94

| Model | Variable | Parameter Estimates | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 2433.89778 | 56.20241 | 239239611 | 1875.40 | $<.0001$ |
|  | fn | 30.60213 | 1.65781 | 43468110 | 340.75 | <.0001 |
|  | $f p$ | 23.55276 | 3.76863 | 4982587 | 39.06 | <.0001 |
|  | fn2 | -0.08489 | 0.00842 | 12972419 | 101.69 | <.0001 |
|  | $\begin{aligned} & f p 2 \\ & R^{2}=0.9451 \end{aligned}$ | -0.16425 | 0.04116 | 2031084 | 15.92 | 0.0001 |
| II | Intercept | 659.92883 | 154.66163 | 495937 | 18.21 | $<.0001$ |
|  | fn | 33.97010 | 1.70399 | 10825703 | 397.43 | <.0001 |
|  | $f p$ | 28.48057 | 2.19811 | 4572957 | 167.88 | <.0001 |
|  | fn2 | -0.08501 | 0.00391 | 12883070 | 472.96 | $<.0001$ |
|  | fp2 | -0.15513 | 0.01914 | 1789668 | 65.70 | <.0001 |
|  | sn | 7.34116 | 1.59902 | 574145 | 21.08 | <.0001 |
|  | sp | 29.25642 | 4.07550 | 1403714 | 51.53 | $<.0001$ |
|  | sk | 0.54214 | 0.22154 | 163119 | 5.99 | 0.0160 |
|  | fnsn | -0.02214 | 0.01136 | 103428 | 3.80 | 0.0539 |
|  | $\begin{aligned} & \text { fpsp } \\ & R^{2}=0.9888 \end{aligned}$ | -0.32079 | 0.07016 | 569449 | 20.91 | <.0001 |
| III | Intercept | 659.92883 | 154.66163 | 495937 | 18.21 | <.0001 |
|  | fn | 33.97010 | 1.70399 | 10825703 | 397.43 | <.0001 |
|  | $f p$ | 28.48057 | 2.19811 | 4572957 | 167.88 | <.0001 |
|  | fn2 | -0.08501 | 0.00391 | 12883070 | 472.96 | <.0001 |
|  | fp2 | -0.15513 | 0.01914 | 1789668 | 65.70 | <.0001 |
|  | sn | 7.34116 | 1.59902 | 574145 | 21.08 | $<.0001$ |
|  | sp | 29.25642 | 4.07550 | 1403714 | 51.53 | $<.0001$ |
|  | sk | 0.54214 | 0.22154 | 163119 | 5.99 | 0.0160 |
|  | fnsn | -0.02214 | 0.01136 | 103428 | 3.80 | 0.0539 |
|  | $\begin{aligned} & \text { fpsp } \\ & \mathrm{R}^{2}=0.9888 \end{aligned}$ | -0.32079 | 0.07016 | 569449 | 20.91 | <.0001 |
| IV | Intercept | 659.92883 | 154.66163 | 495937 | 18.21 | <.0001 |
|  | fn | 33.97010 | 1.70399 | 10825703 | 397.43 | <.0001 |
|  | $f p$ | 28.48057 | 2.19811 | 4572957 | 167.88 | <.0001 |
|  | fn2 | -0.08501 | 0.00391 | 12883070 | 472.96 | <.0001 |
|  | fp2 | -0.15513 | 0.01914 | 1789668 | 65.70 | <.0001 |
|  | sn | 7.34116 | 1.59902 | 574145 | 21.08 | <.0001 |
|  | sp | 29.25642 | 4.07550 | 1403714 | 51.53 | <.0001 |
|  | sk | 0.54214 | 0.22154 | 163119 | 5.99 | 0.0160 |
|  | fnsn | -0.02214 | 0.01136 | 103428 | 3.80 | 0.0539 |
|  | ```fpsp R2=0.9888``` | -0.32079 | 0.07016 | 569449 | 20.91 | <.0001 |

Table 5.5.3: Parameter estimates along with standard errors for response surface models using different number of Variables (models include replication)

Centre: Hisar Crop: Wheat Year: Rabi-1993-94

| Models | I |  | II |  | III |  | IV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameters | Parameter estimates | Standard Error | Parameter estimates |
| Intercept | 1765.67718 | 47.24937 | 1074.95414 | 143.35722 | 985.04757 | 633.60528 | 1036.96075 | 633.12061 |
| Replication | 269.58667 | 14.87930 | 222.00872 | 31.58863 | 222.80781 | 33.17738 | 229.49825 | 33.04496 |
| fn | 32.02411 | 1.16823 | 34.57588 | 72.04672 | 34.49341 | 1.48525 | 36.01041 | 1.65717 |
| $f \mathrm{p}$ | 21.33543 | 3.18355 | 28.44670 | 61.82094 | 28.25399 | 2.12355 | 26.46565 | 2.76960 |
| fk | 1.37267 | 3.36879 | 3.80571 | 105.74216 | 3.82846 | 3.57313 | 3.64407 | 3.75485 |
| $\mathrm{fn}^{2}$ | -0.09936 | 0.00878 | -0.08548 | 8.35024 | -0.08519 | 0.00351 | -0.09763 | 0.00690 |
| $\mathrm{fp}^{2}$ | -0.21262 | 0.04349 | -0.15747 | 15.67407 | -0.15600 | 0.01799 | -0.19759 | 0.03372 |
| $\mathrm{fk}^{2}$ | -0.05730 | 0.06468 | -0.02770 | 30.51447 | -0.02776 | 0.03487 | -0.05913 | 0.04996 |
| sn |  | ----- | 3.72360 | 1.45906 | 6.00725 | 8.86378 | 4.68582 | 8.89233 |
| sp | ----- | ----- | 13.03545 | 4.10827 | 13.73398 | 10.54902 | 14.80402 | 10.56113 |
| sk | ----- | ----- | 0.09080 | 0.21852 | -0.33924 | 1.00353 | -0.13062 | 0.99837 |
|  | ----- | ----- | --- | ----- | -0.00774 | 0.02791 | -0.00312 | 0.02797 |
| sp ${ }^{2}$ | ----- |  | ----- | ----- | -0.02771 | 0.25025 | -0.07960 | 0.25007 |
| sk ${ }^{2}$ | ----- | ----- | ----- | ----- | . 00055900 | 0.00125 | 0.00025003 | 0.00125 |
| fn*sn | ---- | ----- | -0.02758 | 0.48360 | -0.02739 | 0.01005 | -0.02944 | 0.01001 |
| fp*sp | ----- | ----- | -0.27583 | 1.85640 | -0.27248 | 0.06340 | -0.26080 | 0.06312 |
| fk*sk | ---- |  | -0.00761 | 0.25999 | -0.00747 | 0.00885 | -0.00721 | 0.00881 |
| $\mathrm{fn}^{*} \mathrm{fp}$ | 0.04813 | 0.03865 | - | ----- | ,00747 | ----- | 0.03831 | 0.02978 |
| $\mathrm{fn} * \mathrm{fk}$ | 0.00163 | 0.03731 | ----- | ----- | ----- | ----- | 0.00358 | 0.02883 |
| $\mathrm{fp}^{*} \mathrm{fk}$ | 0.02479 | 0.05044 | ----- | ----- | ----- | ----- | 0.02428 | 0.03965 |
| $\mathrm{R}^{2}$ | 0.9864 |  | 0.9924 |  |  | 0 |  |  |

Table 5.5.4: Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure

Centre: Hisar Crop: Wheat Year: Rabi-1993-94

I

II

III

IV

|  | Parameter |
| :--- | ---: |
| Variable | Estimate |
| Intercept | 1767.48275 |
| rep | 269.58667 |
| fn | 31.89192 |
| fp | 21.28940 |
| fn2 | -0.09841 |
| fp2 | -0.20752 |
| fnfp | 0.04738 |
| $R^{2}=0.9863$ |  |

Standard

| Type II SS | F Value | Pr $\rangle$ F |
| ---: | ---: | :--- |
| 46674873 | 1442.90 | $<.0001$ |
| 10901546 | 337.01 | $<.0001$ |
| 28080065 | 868.07 | $<.0001$ |
| 2895524 | 89.51 | $<.0001$ |
| 4468575 | 138.14 | $<.0001$ |
| 1445148 | 44.68 | $<.0001$ |
| 113346 | 3.50 | 0.0638 |
|  |  |  |
| 1109357 | 59.62 | $<.0001$ |
| 1112499 | 59.78 | $<.0001$ |
| 11422530 | 613.83 | $<.0001$ |
| 4712449 | 253.24 | $<.0001$ |
| 13022955 | 699.83 | $<.0001$ |
| 1904439 | 102.34 | $<.0001$ |
| 144511 | 7.77 | 0.0063 |
| 212802 | 11.44 | 0.0010 |
| 179433 | 9.64 | 0.0024 |
| 470369 | 25.28 | $<.0001$ |
|  |  |  |
| 1109357 | 59.62 | $<.0001$ |
| 1112499 | 59.78 | $<.0001$ |
| 11422530 | 613.83 | $<.0001$ |
| 4712449 | 253.24 | $<.0001$ |
| 13022955 | 699.83 | $<.0001$ |
| 1904439 | 102.34 | $<.0001$ |
| 144511 | 7.77 | 0.0063 |
| 212802 | 11.44 | 0.0010 |
| 179433 | 9.64 | 0.0024 |
| 470369 | 25.28 | $<.0001$ |

fpsp
$\mathbf{R}^{2}=0.9923$

| Intercept | 1098.06797 |
| :--- | ---: |
| rep | 224.92344 |
| fn | 35.99033 |
| fp | 26.86803 |
| fn2 | -0.09680 |
| fp2 | -0.19652 |
| sn | 3.82432 |
| sp | 12.78537 |
| fnsn | -0.03002 |
| fpsp | -0.28379 |
| fnfp | 0.03965 |
| $\mathbf{R}^{2}=0.9926$ |  |

138.48378
28.14704
1.49864
2.03285
0.00629
0.02343
1.36438
3.95241
0.00923
0.05737
0.01902

| 1135455 | 62.87 | $<.0001$ |
| ---: | ---: | ---: |
| 1153223 | 63.86 | $<.0001$ |
| 10415684 | 576.74 | $<.0001$ |
| 3154788 | 174.69 | $<.0001$ |
| 4277551 | 236.86 | $<.0001$ |
| 1270406 | 70.34 | $<.0001$ |
| 141888 | 7.86 | 0.0060 |
| 188978 | 10.46 | 0.0016 |
| 191043 | 10.58 | 0.0015 |
| 441933 | 24.47 | $<.0001$ |
| 78449 | 4.34 | 0.0395 |

Table: 5.5.5 Estimated ridge of maximum yield Centre: Hisar Crop: Wheat Year: Rabi-1993-94

Average STV* of the Site: SN= $137.70 \mathrm{Kg} ; \mathrm{SP}:=20.27 \mathrm{Kg} ; \mathrm{SK}=331.67 \mathrm{Kg}$

| Coded | Estimated | Standard <br> Error | fn | Uncoded Factor Values |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Radius | Yield | fp | fk |  |  |
| 0.0 | 5401.438046 | 48.958948 | 100.000000 | 45.000000 | 30.000000 |
| 0.1 | 5541.459641 | 49.458616 | 109.681823 | 46.121442 | 29.931752 |
| 0.2 | 5664.193615 | 49.675660 | 119.194678 | 47.517234 | 29.843218 |
| 0.3 | 5770.091672 | 49.680028 | 128.477221 | 49.226726 | 29.727582 |
| 0.4 | 5859.703752 | 49.640775 | 137.455329 | 51.285349 | 29.574792 |
| 0.5 | 5933.681962 | 49.776325 | 146.046431 | 53.717754 | 29.369190 |
| 0.6 | 5992.772459 | 50.311884 | 154.168179 | 56.529955 | 29.084374 |
| 0.7 | 6037.793964 | 51.458929 | 161.748949 | 59.702232 | 28.670758 |
| 0.8 | 6069.611599 | 53.448771 | 168.731725 | 63.181600 | 28.021306 |
| 0.9 | 6089.140597 | 56.707448 | 175.045837 | 66.854655 | 26.861083 |
| 1.0 | 6097.528577 | 62.536906 | 180.420476 | 70.381790 | 24.378396 |
|  |  |  |  |  |  |

Table 5.5.6 : Parameter estimates along with standard errors for response surface models using different number of variables
Centre: Hisar Crop: Wheat Year: Rabi-1995-96

| Models |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parameters | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error | Parameter estimates | Standard Error |
| Intercept | 2609.20927 | 61.44498 | 550.70568 | 340.99890 | -861.08405 | 1459.85183 | -615.34151 | 1459.73674 |
| fn | 22.20269 | 2.46384 | 25.15121 | 3.84737 | 24.50073 | 3.99011 | 26.74772 | 4.35697 |
| fp | 9.78231 | 6.71425 | 17.83929 | 5.00121 | 18.01759 | 5.06157 | 13.06778 | 6.71118 |
| fk | -0.54060 | 7.10493 | 3.04739 | 8.36058 | 3.27001 | 8.48048 | 5.45507 | 9.04856 |
| $\mathrm{fn}^{2}$ | -0.08527 | 0.01852 | -0.05231 | 0.00733 | -0.05218 | 0.00741 | -0.07907 | 0.01524 |
| $\mathrm{fp}^{2}$ | -0.17625 | 0.09172 | -0.10057 | 0.03915 | -0.09910 | 0.04016 | -0.17294 | 0.07361 |
| $\mathrm{fk}^{2}$ | -0.03918 | 0.13641 | 0.00344 | 0.07452 | 0.00384 | 0.07571 | -0.01996 | 0.10892 |
| sn | ------ | ------ | 9.42531 | 3.00847 | 23.35858 | 17.31709 | 22.41667 | 17.32096 |
| sp | -- | ------ | 9.93505 | 9.57965 | 3.31233 | 25.67774 | 12.85430 | 25.91846 |
| sk | -- | ------ | 1.84231 | 0.64425 | 5.05444 | 4.90218 | 3.97383 | 4.90026 |
| sn ${ }^{2}$ | ------ | ------ |  | ----- | -0.05196 | 0.06462 | -0.05325 | 0.06472 |
| sp ${ }^{2}$ | ------ | ------ | ------ | ------ | 0.22854 | 0.66603 | 0.02686 | 0.66868 |
| sk ${ }^{2}$ | ------ | ------ | ------ | ------ | -0.00458 | 0.00698 | -0.00296 | 0.00698 |
| fn*sn | ------ | ------ | -0.04917 | 0.02672 | ------ | ------ | -0.04285 | 0.02815 |
| fp*sp | ------ | ------ | -0.18351 | 0.19183 | ------ | ------ | -0.18754 | 0.19651 |
| fk*sk | - |  | -0.00995 | 0.01964 | ---- | ------ | -0.01382 | 0.01982 |
| $f{ }^{\text {f }} \mathrm{fp}$ | 0.09168 | 0.08152 | ------ | ------ | -0.04504 | 0.02779 | 0.09043 | 0.06645 |
| $f n^{*} \mathrm{fk}$ | 0.02115 | 0.07868 | ------ | ------ | -0.19183 | 0.19552 | 0.00669 | 0.06356 |
| fp*fk | -0.00400 | 0.10637 | ------ | ------ | -0.01114 | 0.01988 | -0.01352 | 0.08639 |
| $\mathbf{R}^{2}$ | 0.8566 |  | 0.9133 |  | 0.9141 |  | 0.9178 |  |

$\begin{array}{ll}\text { Table 5.5.7: } & \text { Parameter estimates along with standard errors for remaining significant } \\ \text { variables in different models using backward elimination procedure }\end{array}$

## Centre: Hisar Crop: Wheat Year: Rabi-1995-96

| Models | Variable | Parameter Estimate | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 2608.67908 | 60.04529 | 269360370 | 1887.48 | $<.0001$ |
|  | fn | 22.35977 | 2.27356 | 13802931 | 96.72 | $<.0001$ |
|  | $f p$ | 8.57187 | 4.72634 | 469409 | 3.29 | 0.0724 |
|  | fn2 | -0.08610 | 0.01759 | 3420667 | 23.97 | $<.0001$ |
|  | fp2 | -0.18764 | 0.06521 | 1181501 | 8.28 | 0.0048 |
|  | $\begin{aligned} & \text { fnfp } \\ & R^{2}=0.8564 \end{aligned}$ | 40.10662 | 0.05316 | 574060 | 4.02 | 0.0473 |
| II | Intercept | 400.48579 | 286.12311 | 175001 | 1.96 | 0.1644 |
|  | fn | 27.78781 | 2.98121 | 7760574 | 86.88 | $<.0001$ |
|  | $f p$ | 15.28842 | 3.16018 | 2090612 | 23.40 | $<.0001$ |
|  | fn2 | -0.05208 | 0.00710 | 4809284 | 53.84 | <.0001 |
|  | fp2 | -0.10401 | 0.03453 | 810581 | 9.07 | 0.0032 |
|  | sn | 11.90713 | 2.28767 | 2419900 | 27.09 | $<.0001$ |
|  | sk | 1.74286 | 0.44865 | 1347992 | 15.09 | 0.0002 |
|  | $\begin{aligned} & \text { fnsn } \\ & R^{2}=0.9117 \end{aligned}$ | -0.06936 | 0.01971 | 1106494 | 12.39 | 0.0006 |
| III | Intercept | 400.48579 | 286.12311 | 175001 | 1.96 | 0.1644 |
|  | fn | 27.78781 | 2.98121 | 7760574 | 86.88 | $<.0001$ |
|  | $f p$ | 15.28842 | 3.16018 | 2090612 | 23.40 | <.0001 |
|  | fn2 | -0.05208 | 0.00710 | 4809284 | 53.84 | $<.0001$ |
|  | fp2 | -0.10401 | 0.03453 | 810581 | 9.07 | 0.0032 |
|  | sn | 11.90713 | 2.28767 | 2419900 | 27.09 | $<.0001$ |
|  | sk | 1.74286 | 0.44865 | 1347992 | 15.09 | 0.0002 |
|  | $\begin{aligned} & \text { fnsn } \\ & R^{2}=0.9117 \end{aligned}$ | -0.06936 | 0.01971 | 1106494 | 12.39 | 0.0006 |
| IV | Intercept | 463.22853 | 283.73028 | 231422 | 2.67 | 0.1054 |
|  | fn | 29.99271 | 3.12858 | 7979251 | 91.90 | $<.0001$ |
|  | $f p$ | 11.13683 | 3.71242 | 781329 | 9.00 | 0.0033 |
|  | fn2 | -0.07687 | 0.01394 | 2641525 | 30.42 | $<.0001$ |
|  | fp2 | -0.18225 | 0.05105 | 1106551 | 12.75 | 0.0005 |
|  | sn | 11.34111 | 2.27212 | 2163090 | 24.91 | <. 0001 |
|  | sk | 1.81951 | 0.44388 | 1458806 | 16.80 | $<.0001$ |
|  | fnsn | -0.06798 | 0.01944 | 1061799 | 12.23 | 0.0007 |
|  | $\begin{aligned} & \text { fnfp } \\ & R^{2}=0.9150 \end{aligned}$ | 0.08610 | 0.04187 | 367199 | 4.23 | 0.0421 |

Table 5.5.8 : Parameter estimates along with standard errors for response surface models using different number of Variables (models include replication)

Centre: Hisar Crop: Wheat Year: Rabi-1995-96


Table 5.5.9: Parameter estimates along with standard errors for remaining significant variables in different models(replication included) using backward elimination procedure

Centre: Hisar Crop: Wheat Year: Rabi-1995-96

| Models | Variable | Parameter Estimate | Standard Error | Type II SS | F Value | $\mathrm{Pr}>\mathrm{F}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | Intercept | 2105.68741 | 77.71516 | 66246140 | 734.14 | $<.0001$ |
|  | rep | 201.19667 | 24.52712 | 6072015 | 67.29 | $<.0001$ |
|  | fn | 22.35977 | 1.80790 | 13802931 | 152.96 | $<.0001$ |
|  | fp | 8.57187 | 3.75830 | 469409 | 5.20 | 0.0244 |
|  | fn2 | -0.08610 | 0.01398 | 3420667 | 37.91 | <. 0001 |
|  | $\begin{aligned} & f p 2 \\ & R^{2}=0.9100 \end{aligned}$ | -0.18764 | 0.05186 | 1181501 | 13.09 | 0.0004 |
| II | Intercept | 1163.06515 | 307.15597 | 1213198 | 14.34 | 0.0002 |
|  | rep | 182.71970 | 38.80930 | 1875602 | 22.17 | <. 0001 |
|  | fn | 29.10171 | 2.91775 | 8417467 | 99.48 | $<.0001$ |
|  | fp | 13.97009 | 3.08569 | 1734340 | 20.50 | <. 0001 |
|  | fn2 | -0.05530 | 0.00697 | 5326685 | 62.95 | $<.0001$ |
|  | fp2 | -0.08978 | 0.03372 | 599743 | 7.09 | 0.0089 |
|  | sn | 7.28744 | 2.67757 | 626774 | 7.41 | 0.0075 |
|  | $\begin{aligned} & \text { fnsn } \\ & R^{2}=0.9164 \end{aligned}$ | -0.07349 | 0.01919 | 1240481 | 14.66 | 0.0002 |
| III | Intercept | 1540.09135 | 347.93925 | 1596881 | 19.59 | $<.0001$ |
|  | rep | 307.11947 | 65.80474 | 1775362 | 21.78 | $<.0001$ |
|  | fn | 30.17055 | 2.91148 | 8752375 | 107.38 | $<.0001$ |
|  | $f p$ | 14.48257 | 3.09088 | 1789428 | 21.95 | <. 0001 |
|  | fn2 | -0.05789 | 0.00692 | 5706813 | 70.02 | $<.0001$ |
|  | fp2 | -0.09153 | 0.03364 | 603248 | 7.40 | 0.0076 |
|  | sn | 7.50356 | 2.64475 | 656073 | 8.05 | 0.0054 |
|  | sp | -74.44938 | 30.16283 | 496552 | 6.09 | 0.0151 |
|  | sp2 | 1.48391 | 0.66640 | 404144 | 4.96 | 0.0280 |
|  | $\begin{aligned} & \text { fnsn } \\ & R^{2}=0.9209 \end{aligned}$ | -0.07765 | 0.01904 | 1355977 | 16.64 | <. 0001 |
| IV | Intercept | 1598.70978 | 343.76406 | 1709466 | 21.63 | <. 0001 |
|  | rep | 300.86953 | 64.86946 | 1700271 | 21.51 | $<.0001$ |
|  | $f$ | 32.31304 | 3.04234 | 8916256 | 112.81 | <. 0001 |
|  | $f p$ | 10.18921 | 3.66376 | 611321 | 7.73 | 0.0064 |
|  | fn2 | -0.08241 | 0.01350 | 2947393 | 37.29 | $<.0001$ |
|  | fp2 | -0.16811 | 0.04920 | 922735 | 11.67 | 0.0009 |
|  | sn | 6.57193 | 2.64175 | 489151 | 6.19 | 0.0144 |
|  | sp | -64.75695 | 30.05764 | 366864 | 4.64 | 0.0334 |
|  | sp2 | 1.29731 | 0.66219 | 303359 | 3.84 | 0.0527 |
|  | fnsn | -0.07604 | 0.01876 | 1298179 | 16.42 | $<.0001$ |
|  | fnfp $R^{2}=0.9240$ | 0.08566 | 0.04069 | 350331 | 4.43 | 0.0376 |

Table 5.5.10: Estimated ridge of maximum yield

## Centre: Hisar Crop: Wheat Year: Rabi-1995-96

Average STV* of the Site: $\mathrm{SN}=135.38 \mathrm{Kg} ; \mathbf{S P}=15.67 \mathrm{Kg} ; \mathrm{SK}=347.92 \mathrm{Kg}$

| Coded <br> Radius | Estimated <br> Yield | Standard <br> Error | Uncoded |  | Factor Values <br> $f p$ |
| :--- | :--- | :--- | :---: | :---: | :---: |
| 0.0 | 4464.553023 | 75.972117 | 100.000000 | 45.000000 | 30.000000 |
| 0.1 | 4554.311896 | 76.691646 | 109.786609 | 45.921675 | 29.950443 |
| 0.2 | 4630.522495 | 76.953861 | 119.312888 | 47.336433 | 29.929827 |
| 0.3 | 4694.099252 | 76.855313 | 128.452450 | 49.279369 | 29.954018 |
| 0.4 | 4746.057973 | 76.616326 | 137.090453 | 51.739089 | 30.047523 |
| 0.5 | 4787.432722 | 76.426167 | 145.154232 | 54.655602 | 30.250463 |
| 0.6 | 4819.194496 | 76.368770 | 152.624427 | 57.934481 | 30.635892 |
| 0.7 | 4842.214437 | 76.385943 | 159.513504 | 61.458784 | 31.355210 |
| 0.8 | 4857.316500 | 76.154537 | 165.791977 | 65.058313 | 32.758885 |
| 0.9 | 4865.533808 | 74.764141 | 171.160391 | 68.340143 | 35.580439 |
| 1.0 | 4868.643040 | 71.345309 | 174.922609 | 70.610266 | 40.163142 |
|  |  |  |  |  |  |

Table: 5.7 Comparison of optimum fertilizes doses by targeted yield approach and Response Surface Methodology

| S.No. | Centre | Crop/Season/ <br> Variety | Year | Mean Soil Test Value |  |  | Targeted Yield* (Kg/ ha ${ }^{-1}$ ) | Optimal Fertilizer Doses |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Targeted Yield Approach | Response Surface Methodology |  |  |
|  |  |  |  | SN | SP | SK |  | FN | FP | FK | FN | FP | FK |
| 1. | Bhubaneswar | Rice /Kharif / Konark | 1998 | 147.87 | 26.72 | 97.83 |  | 4098 | 63 | 58 | 35 | 70 | 58 | 23 |
| 2. | ---do------- | Rice /Kharif /Konark | 1999 | 157.42 | 33.55 | 109.54 | 4038 | 56 | 56 | 33 | 70 | 60 | 19 |
| 3. | ----do------ | Rice / Kharif /Konark | 2000 | 165.60 | 31.51 | 108.13 | 4648 | 68 | 66 | 42 | 57 | 68 | 29 |
| 4. | ----do----- | Rice / Kharif /Lalat | 1999 | 186.17 | 26.02 | 181.69 | 4911 | 117 | 52 | 41 | 114 | 41 | 31 |
| 5. | Hyderabad | Sunflower /Rabi / | 1993 | 259.43 | 30.71 | 370.77 | 1511 | 106 | 79 | 57 | 106 | 41 | 14 |
| 6. | Hyderabad (Maruteru) | Rice /Rabi | 1994 | 334.82 | 54.30 | 346.37 | 5723 | 119 | 73 | 72 | 140 | 31 | 58 |
| 7. | Hyderabad | Groundnut /Rabi - | 1997 | 240.45 | 33.56 | 346.84 | 2048 | 28 | 47 | 83 | 29 | 39 | 35 |
| 8. | Hisar | Wheat /Rabi /542 | 1993 | 137.70 | 20.27 | 331.67 | 6097 | 153 | 67 | 52 | 180 | 70 | 24 |
| 9. | Hisar | Wheat/Rabi /896 | 1995 | 135.38 | 15.67 | 347.92 | 4808 | 159 | 66 | 46 | 175 | 71 | 40 |
| 10 | Hisar | Wheat/Rabi /CVSonak | 1997 | 135.07 | 18.21 | 400.43 | 5059 | 159 | 65 | 51 | 179 | 71 | 35 |
| 11. | Kalyani | Rape/Rabi | 1998 | 252.88 | 21.31 | 237.06 | 1238 | 109 | 58 | 39 | 119 | 47. | 34 |
| 12. | Coimbatore | Onion/Rabi | 1998 | 216.16 | 32.4 | 270.16 | 18134 | 111 | 68 | 56 | 110 | 68 | 36 |

* Targeted yield has been taken as the maximum response achievable by Response surface methodology. This has been done only to compare and verify the targeted yield approach.


## SUMMARY

The balanced application of fertilizer nutrients particularly the major nutrients, N P and K in optimum quantity, based on soil test and crop requirement is one of the most vital aspects for sustaining higher agricultural production. This requires the application of optimally balanced quantity of fertilizers in right proportion through correct method and time of application for a specific soil-crop-climate situation. It ensures increased quantity of produce, maintenance of soil productivity and the most efficient and judicious use of applied fertilizers. Thus in this content the soil fertility evolution and refined fertilizer prescription for sustained agricultural production is of great importance to any country of the world in general and farming community in particular. Hence the soils have to be tested precisely for their available nutrient status for making fertilizer recommendation based on crop response and economic circumstances.

The determination of the amount of fertilizer that should be applied to a crop would be delightfully simple if a chemist could analyze the soil, and then use the analyses to measure the amount of plant nutrients in the soil and to calculate the amounts that should be applied to correct deficiencies. It is unfortunate that the determination of fertilizer requirements is not as simple as this. As every soil chemist knows, there are basic problems in interpreting soil test values in terms of nutrient availability to crops due to the interacting effects of other soil constituents, surface reactions, the changes that may occur in test values both laterally across farmers’ fields and vertically down the soil profile, and to all these factors may be added the uncertainties of weather, effects of crop variety, disease, pests etc. Any suggestion therefore that fertilizer requirement can be determined solely on the basis of a simple laboratory analysis of a few grams of soil, represents a vast oversimplification of a highly complex system. Nevertheless soil analysis can provide useful information on the effect that fertilizers are likely to have on yields, and it is important to use this information for the estimation of fertilizer requirements. Soil tests can provide a valuable piece of information and as such should be used in conjunction with such other information that is available for the estimation of fertilizer requirements.
Soil test crop-response studies has been going on for a quite a long period of time both in India and abroad. the All India Coordinated Research Project on Soil Test Crop Response Correlation was initiated during the year 1967-68. Currently, STCR project is having seventeen cooperating centres.

Under the STCR project multiple regression approach is being used to calculate the dose of nutrient (s) required to obtain the maximum yield of crops under given set of experimental conditions. It can further be used to calculate the economic dose of fertilizer nutrients by incorporating a constant factor i.e. per unit cost of input (fertilizer) in the original equation. In this approach yield is regressed with soil nutrients, fertilizer nutrients, their quadratic terms and the interaction term of soil and fertilizer nutrients. For this the following criteria should be fulfilled.
(a) Soil test crop response calibration for economic yield of a crop is possible only when the response to added nutrients follow the law of diminishing returns. i.e. the signs of partial regression coefficients of linear, quadratic terms of nutrients and their interaction with available soil nutrients should in general be positive, negative and negative (+,-,-) respectively.
(b) The coefficient of determination $\left(\mathrm{R}^{2}\right)$ should be high.
(c) The partial regression coefficients should be statistically significant.
(d) The experiment should have sufficient design points i.e. the number of treatments should be at least two or more than the number of variables in the model.

The above criterions are seldom fulfilled under the STCR project data. In such cases the optimum values of the nutrients cannot be derived or if they could be derived, they are either too high or too low.
Keeping in view of the above problems and for better analysis of data, their interpretation and improvement in soil test calibration, the projector coordinator (STCR) Indian Institute of Soil Science, Bhopal, formally approached IASRI, New Delhi for collaboration. As large amount of data have also been gathered under the project, the creation of a database under the project was also solicited.
Consequently a project entitled Planning, designing and analysis of experiments relating to AICRP on soil test crop response correlation was under taken at IASRI w.e.f. $1^{\text {st }}$ march 2000 with the following objectives:

1. To improve the existing methodology for analysis of data of ongoing STCR experiments.

2 To carry out planning, design for the conduct of new set of experiments and subsequently to carry out the analysis of data.
3. To develop a database for the project.

In this report, the first two chapters contain introduction and review of literature. In the third chapter Analytical techniques has been discussed along with a method, which has been developed at IASRI based on Response surface methodology has been discussed. In this method, the optimal values of $\mathrm{N}, \mathrm{P}$ and K fertilizer nutrients can be derived if the soil test values for a particular site is available.
Chapter four deals with designs for future STCR experimentation. In this, a number of designs have been proposed with different designs points, based on the requirements of STCR project, from designs of type ( $5 \times 4 \times 3$ ), ( $4 \times 4 \times 3$ ), ( $4 \times 4 \times 4$ ) etc.
Chapter five deals with results and discussion. Although we have received the data from a number of centres but due to pending query for discrepancies, only data of seven centres (totaling about 12 experiments) have been discussed in detail.
The common result is that in almost all the cases the response surface methodology produced the stationery point as saddle points i.e. neither maxima nor minima. In such cases exploration of the response surface in the vicinity of the stationery point has been attempted. The optimal values of the fertilizer nutrients N, P and K obtained by Response Surface Methodology, has been found to be closely related to that obtained by Targeted yield approach adopted by the STCR project. Thus one could advocate for the adoption of the Targeted yield approach as has been tested by sound statistical system of Response Surface Methodology. A number of models have been tried for all the experiments but the models with 15 variables and 18 variables have been mostly found to be better. One model with 15 variables, which includes the interactions (FN x FP), (FN x FK) and (FP x FK) also gives higher values of R-Square. In some cases it was possible to find the optimum values from the Multiple Regression equations.

Lastly, in Chapter six we have given the sketch of the database prepared for storing the STCR data. In this, number of queries can be prepared and the data can be retrieved.

## सारांश

मृदा परीक्षण और फसल की जरूरत के आधार पर प्रमुर्त उर्वरक पोषकों यानि एन.पी. और के. की अनकूल मात्रा अर्थात संतुलित उपयोग कृषि के उच्च उत्पादन को अक्षुण बनाए रखने का सर्वाधिक महत्वपूर्ण पहलू है । इसके लिए जरूरी है कि किसी विशिष्ट मृदा फसल जलवायवीय दशाओं में उचिते विधि और उचित समय पर उचित अनुपात में उर्वरकों की अवुकूल संतुलित मात्रा डाली जाए । ऐसा करने से उत्पाद अधिक मात्रों में मिलता है, मिट्टी कीे उर्ररता बबनी रहवी है और डाले गाए उर्वरकों का कुशल और विवेक्रण्ण इस्तेनाल सुणिश्चित होता है । विश्व के किसी शी देश में आमतौर पर और खासकर कृषि समुदाय के लिए अक्षूण कृषिथ उत्पादन लेने के लिए मृदा की उर्वरता का विकास और परिष्कृत उर्वरक के विर्धारण की बड़ी भारी महत्व है इसलिए मिट्टी में उपलब्ध पोषक वत्व का स्तर जानने के लिए मिट्टी का परीक्षण सटीकता से करना होगा वाकि उर्वरकों की सिफ्कारिश, फसल अनुकिया और आर्थिक परिरिथिति के आधार पर की जा सके ।

यदि कोई रसायनशास्ती मिट्टी का विश्लेषण कर सके और तब उस विश्लेषण का इस्तेमाल मिट्टी मुं पादप पोषकों की मात्रा मापने के साथथ-साथ सही कमी वाली मिट्टी में डाली जाने वाली मात्रा की गणना करता है तो किसी फसल में डाले जाने वाले उर्वरक की मात्रा का विर्धारण करना बहुत ही सरल होगा । यह बड़ा ही दुर्भाग्य पूर्ण है कि उर्वरकों की जरूरत का चिर्धारण करना इतना सरल नही है जितना समझा जाता है । क्योंकि एक गृदा रसायबशास्र्री भली-भांति जानता है कि फसलों की पोषण उपलब्धता के परिपेक्ष्य में मृदा परीक्षण गानों की व्याख्या करने में समस्याएं आती है जिसका कारण है-मिट्टी के दूसरे अव्योन्यकिया सांघटकों, अन्वरापृष्ठ किया, ऐसो परिवर्तनों का होना, जो परीक्षण मानों में दोबों ही प्रकार से यानि पार्शव रूप से और उर्घ्व रूप से किसानो के खेतों की मिट्टी में होते है ओर इबमें ऐसे सभी काराकों को भी जोड़ा जा सकता है जो मौसम की अनिश्चितता, फसल की किरम, रोग, बाशी पीड़क्क इत्यादि से संबंधित है, इसलिए किसी एक उच्च रुप सो जटिल प्रणाली के विस्टृत अति-सेरलीकरण का प्रतिनिधित्व करने वाली कुछ ग्राम मिट्टी के साधारण प्रयोगशाला विश्लेषण के आधार पर ऐसा कोई भी सुझाव जो केवल उर्वरकों की जरूरत को निर्धरित कर सक्रा है मान्य होगा । फिर भी गिट्टिटी के विश्लेषण से उर्वरकों के ऐसे प्रभावों पर उपयोगी सूचना मिल सकती जो उपज पर पड़ सकते हैं, और सबसे महत्वपूर्ण यह है कि उर्वरक की जरुरूत का आकलन करने के लिए इस सचना का भरपर उपयोग किया जा सतका है । गृदा परीक्षण बहुमल्य सूचनाएं प्रदाब करते है जिनका उपयोग ऐरी दूसरी सूचनाओं के साथ किएया जा सकतो है जो उउर्वरकों की जरूरत का आकलन करने के लिए उपलब्धि हैं।

भारत हीं बही विदेशों मो भी एक लम्बे अर्स से मृदा परीक्षण फसल अनुक्रिया पर अध्ययन चल रहे हैं। मृदा परीक्षण फसल अनुक्किया सहसम्बन्ध पर एक अरिवल भारतीय समन्वित अबुसंधााब परियोजना सब्त 1967-68 के दौरान श्रुरू की गई थी । इस समय मृदा परीक्षण फरसल अबुक्रिया सहरम्बन्ध पर एक अरिल भारतीय समन्वित अनुरांधान परियोजना के 17 सहटयोगी केन्द हैं।

गृदा परीक्षण फइसल अनुकिया सहसम्बन्ध पर एक अखिल भारतीय समन्वित अनुरांधान परिरोणनां के वहल किसीं दी हुई परीक्षणात्मक दशाओं में फसलों की अधिकाधिक उपज प्राप्त करने फे लिए जरूरी पोषककों की सुराक की गणना हेतु बहु समाश्रियण विधि का उपयोग किया जा रखकता है। इसके अलावा इसका उपयोग, त्रिथर कारकों जैसे-मूल समीकरण में प्रति

उकाई लितेशे (उर्वरक) को शामिल कर उर्वरक पोषकों की किफायती खुराक्क की गणना करने के लिए की क्रिया जा सकता है । इस विधि में उपज को मृदा पोषक तत्वों, उर्वरक पोषकों, उनकी द्विघाती पद और मिट्टी एवं उर्वरक पोषकों के अन्योन्यक्रिया पदों के साथ समाश्रीयित किया जाता है । इसके लिए निम्न मानदण्डों को पूरा किया जाना चहिए ।
(क) किरी फससल की लाभ्याद उपज का मृदा परीक्षण फसल अनुकिया अंशांकन केवल वभt संभव है जब डाले गए पोषकों की अनुक्रिया (ला आफ डिमिनीशंग रिटर्न) हासमान लाभ के कानून का अनुसरण करे, यानि रैखिवकता के आंशिक समाश्रियण गुणांकों (पारी़ियल रिग्रेशन कोएफिशिएन्टरा) के चिन्हों, पोषकाँ के द्विघातीय पदो, और उनकी उपलब्ध, मृद्धा पोषकों के साथ अनुक्रिया, आमतौर पर कमशः धनात्मक, ऋणात्मक और चछणात्मक (,,+-- ) होनी चाहिए ।
(खं) निर्धारण का गुणांक ( $\mathbf{R}^{2}$ ) उच्च होना चाहिए ।
(ग) अंशिक समाश्र्रयण गुणांक सांख्यित्यकी रूप से महत्वपूर्ण (सिर्गानफिकेन्ट) होना चाहिए।
(घ) परीक्षण मों पर्याप्त डिजाइन बिन्दु होने चाहिए याबि उपचारों की संख्या मॉडल में चरों की संख्या सो कम से कम 2 या अधिक हों।

मृद्ध परीक्षण फसल अनुक्किया परियोजना के आंकड़ों में उक्त माबदण्ड कम ही पूरे होते हैं। ऐस मामली में पोषकों के इष्टतम मान या वो निकाले ही नही जा सकते या फिर निकाले जा सकृते हैं तो दे या वो बहुत ज्यादा होते हैं या बहुत कम ।

उक्त समस्याओं को ध्याब में रखते हुए और आंकड़ों का बेहतर विश्लेषण करने के लिए, उनकी व्याज्ख्या करने के लिए तथा मृदा परीक्षण अंशांकन में सुधार लाने के लिए परियोजना समन्व्यक (मृदा परीक्षण फसल अनुक्किया) भारतीय मृदा विज्ञान संस्थान, भोपाल औपचारिक रुप से भाररवीय कृषि सांरिख्यकी अनुसंधान संस्थान, नई दिल्ली के पारा सहयोग की अपेक्षा से आय । क्योंकिं इस परियोजना के तहत बड़ी संख्या में आंकड़े भी एकत्रित किंए गए हैं इसलिए इस परियोजना में एक डाटा-बेस तैयार करने की भी जरूरत है ।
परिणाम स्वरूप "मृदा परीक्षण फसल अनुक्किया सह-सम्बन्ध पर अखिल भारवीय समन्वित अनुरंधान पर्रियोजना से सम्बंधित परीक्षणों का नियोजन, डिजाइनिंग और विश्लेषण नामक एकं परियोजबा 1 मार्च, 2000 से भारतीय कृष्थि सांख्यिकी अनुसंधान संसथान में शुरू की गई । इस परियोजना के प्रगुख उद्देश्य निम्नानुसार हैं :

1. चल रहे एस.टी.सी.आर. परीक्षणों के आंकड़ों का विश्लेषण करने के लिंट नौजूदा पछंति में सुधार करना ।
2. परीक्षणों के बएए सैट का नियोजन और डिजाइन तैयार करना और तदन्तर आंकड़ों का विश्लेषण करना ।
3. पट्रियोजना के लिए डाटाबेस का विकास करना ।

इस रिपोर्ट कें पहले 2 अध्याय प्रसतावना और साहित्य समीक्षा से सम्बंधित है । तीसरे अध्याय कों विश्लेषणात्मक तकरनीकों पर विचार किया गया है इसके अलावा एक बई विधि, जो अबुकिक्या अन्रापृष्ठ पद्धति पर आधारित है, भारवीय कृष्ठि सांखिख्यकी अनुसंधान संसभान में टिक्सित की गई हैं। इस विधि में बाइट्रोजन, फास्फोरस और पोटेशियन उर्वरक पोषकों के

इष्टतम माबों को निकाला जा सकता है बशर्त कि उस सथान के मृदा परीक्षण के मान उपलब्ध हों।

अध्याय 4 कों भावी एस.टी.सी.आर. परीक्षणों की डिजाइनों की व्याख्या की गई है । एस.टी.री.आर. परियोजबा की जरूरतों के आधार पर भिन्ब-भिन्न डिजाइन बिन्दुओ सहित $(5 \times 4 \times 3),(4 \times 4 \times 3),(4 \times 4 \times 4)$ इत्यादि डिजाइनों की किरम सो अनेक डिजाइनों का प्रस्ताव रख्या गया है ।

अध्याय 5 में परिणामों और विचारों की व्याख्या की गई है । हांलाकि हमें अंनेक केन्द्रो से आंकड़े प्वाप्त हुए परनु उनमें विरोधाभास सम्बन्धी जानकारी के रहते केवल 7 केन्द्रों (कुल लगभग 12 परीक्षणो) के आंकड़ों पर विस्तार से विचार किया गया है ।

सामान्ट्य परिणान यह निकला है कि सभी मानलों में जहां अनुक्किया अन्तरापृष्ठ पद्धति से पल्याण बिन्दु (सैडल प्वाइंट) के रूप में एक स्तब्ध बिन्दु (स्टेशनरी प्वाइंट) बना यानि यह न वो अधिकतनं था और ब ही न्यूनतम था। इन मामलों में अनुकिया अन्तरापृष्ठ पद्धति द्वारा प्राप्त उर्ररक पोषकों बाईद्रोजन, फोसफोरस और पोटैशियम के इष्टतम मान उन मानों के काफी करीब पाए गाए है जो एस.टी.सी.आर. परियोजबा द्वारा अपनाई गई लक्ष्य विधि सो प्राप्त हुए हैं। इस प्रकार कोई भी लक्षित उपज विधि की वकालत कर सकता है क्योंकि इसे अनुक्किया अन्तरापृष्ठ पद्धति की एक ठोस सांख्यिकी प्रणाली द्वारा परीक्षित किया गया है। सभी परीक्षणों के लिए अनेक मॉडल अपबाए गए । परन्तु 15 और 18 चरों वाले मॉडल श्रेष्ठ पाए गए हैं। 15 चरों वाला एक मॉडल जिसमें (FN $\mathbf{x}$ FP), ( $\mathrm{FN} \mathbf{x ~ F K \text { ) और ( } \mathrm { FP } \mathbf { x ~ F K ) ~ }}$ अन्योन्यकियायं शामिल हैं, से भी R-Square का उच्च माब प्राप्त होता है । कुछ मामलों में बहु समाश़रयण सान्मीकरणों से हष्टतव मान प्राप्त करना सांभव था।

अन्तवः छठे अध्याय में एस.टी.सी.आर. आंकड़ों को एकत्रित करने के लिए तैय़ार किए गए डाटाबेस का चित्रण किया है । इसमें अनेक जानकारियां तैयार की जा स़कीी हैं औऱ आंकड़ो को पुब: प्राप्त किया जा सकता है ।

# APPENDIX-I <br> Table: Calculation of Basic Data for Targetted yield equations 

Centre
: MARUTERU(HYDERABAD) Year:1994Crop:Rice Season :Rabi

| GRD | TRT | FN | FP | FK | YIELD | SN | UP-N | NR-N | CFN | CSN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
|  |  |  |  |  |  |  |  | $\begin{gathered} \hline \text { (Col } \\ 8 * 100) \\ \text { Icol 6) } \\ \hline \end{gathered}$ | $\begin{gathered} \text { (col 8- } \\ \text { av.CSN* } \\ \operatorname{col} 7) / \mathrm{col}^{4} \\ \hline \end{gathered}$ | $\begin{gathered} \text { (col } 8 \\ \text { /col 7) } \\ \hline \end{gathered}$ |
| 1 | 1 | 50 | 0 | 0 | 3753 | 286 | 72.04 | 1.9185 | 0.5485 |  |
| 1 | 2 | 50 | 0 | 40 | 4240 | 276 | 78.94 | 1.8608 | 0.7177 |  |
| 1 | 3 | 50 | 0 | 80 | 3892 | 295 | 101.7 | 2.6105 | 1.1124 |  |
| 1 | 4 | 50 | 40 | 0 | 3753 | 300 | 80.36 | 2.1396 | 0.6709 |  |
| 1 | 5 | 50 | 40 | 40 | 4170 | 331 | 76.19 | 1.8249 | 0.4902 |  |
| 1 | 6 | 50 | 40 | 80 | 4518 | 319 | 91.11 | 2.0164 | 0.8276 |  |
| 1 | 7 | 50 | 80 | 0 | 4240 | 348 | 93.3 | 2.2005 | 0.7812 |  |
| 1 | 8 | 50 | 80 | 40 | 4865 | 319 | 97.34 | 2 | 0.9516 |  |
| 1 | 9 | 50 | 80 | 80 | 4726 | 300 | 69.79 | 1.4748 | 0.4589 |  |
| 1 | 10 | 100 | 0 | 0 | 5352 | 322 | 81.01 | 1.5135 | 0.3081 |  |
| 1 | 11 | 100 | 0 | 40 | 5004 | 335 | 81.82 | 1.6347 | 0.2959 |  |
| 1 | 12 | 100 | 0 | 80 | 4865 | 322 | 84.03 | 1.7266 | 0.3381 |  |
| 1 | 13 | 100 | 40 | 0 | 5282 | 322 | 100.1 | 1.8951 | 0.4991 |  |
| 1 | 14 | 100 | 40 | 40 | 5143 | 324 | 91.49 | 1.7772 | 0.409 |  |
| 1 | 15 | 100 | 40 | 80 | 4728 | 312 | 80.84 | 1.709 | 0.3217 |  |
| 1 | 16 | 100 | 80 | 0 | 5560 | 376 | 97.28 | 1.7482 | 0.386 |  |
| 1 | 17 | 100 | 80 | 40 | 5352 | 342 | 120.6 | 2.2515 | 0.672 |  |
| 1 | 18 | 100 | 80 | 80 | 5128 | 386 | 87.38 | 1.7024 | 0.2714 |  |
| 1 | 19 | 150 | 0 | 0 | 4518 | 375 | 97.48 | 2.1558 | 0.2597 |  |
| 1 | 20 | 150 | 0 | 40 | 5421 | 362 | 100.4 | 1.8521 | 0.2932 |  |
| 1 | 21 | 150 | 0 | 80 | 7228 | 420 | 165.3 | 2.2856 | 0.6649 |  |
| 1 | 22 | 150 | 40 | 0 | 5699 | 429 | 114.8 | 2.0144 | 0.3196 |  |
| 1 | 23 | 150 | 40 | 40 | 6742 | 442 | 156.3 | 2.3168 | 0.5821 |  |
| 1 | 24 | 150 | 40 | 80 | 7089 | 420 | 140.6 | 1.9834 | 0.5009 |  |
| 1 | 25 | 150 | 80 | 0 | 5004 | 319 | 111.3 | 2.2222 | 0.4099 |  |
| 1 | 26 | 150 | 80 | 40 | 6742 | 342 | 141.4 | 2.0973 | 0.5873 |  |
| 1 | 27 | 150 | 80 | 80 | 5699 | 350 | 116.5 | 2.0425 | 0.4123 |  |
| 1 | 28 | 0 | 0 | 0 | 1946 | 285 | 56.96 | 2.9239 | - | 0.1996 |
| 1 | 29 | 0 | 0 | 0 | 2502 | 276 | 46.29 | 1.8465 | - | 0.1674 |
| 1 | 30 | 0 | 0 | 0 | 2085 | 291 | 46.04 | 2.2062 | - | 0.1581 |
| 2 | 1 | 50 | 0 | 0 | 4031 | 294 | 68.82 | 1.7068 | 0.4596 |  |
| 2 | 2 | 50 | 0 | 40 | 4726 | 310 | 93.69 | 1.9805 | 0.9057 |  |
| 2 | 3 | 50 | 0 | 80 | 4587 | 319 | 94.58 | 2.0602 | 0.8956 |  |
| 2 | 4 | 50 | 40 | 0 | 3545 | 322 | 75.93 | 2.141 | 0.5143 |  |
| 2 | 5 | 50 | 40 | 40 | 4070 | 348 | 75.53 | 1.855 | 0.4252 |  |
| 2 | 6 | 50 | 40 | 80 | 4726 | 308 | 87.85 | 1.8578 | 0.7959 |  |
| 2 | 7 | 50 | 80 | 0 | 4031 | 281 | 76.17 | 1.8879 | 0.6461 |  |
| 2 | 8 | 50 | 80 | 40 | 4448 | 315 | 76.06 | 1.7086 | 0.5381 |  |
| 2 | 9 | 50 | 80 | 80 | 4587 | 295 | 85.11 | 1.8552 | 0.7824 |  |
| 2 | 10 | 100 | 0 | 0 | 5630 | 342 | 136.4 | 2.421 | 0.83 |  |
| 2 | 11 | 100 | 0 | 40 | 5630 | 335 | 115.8 | 2.0551 | 0.6349 |  |
| 2 | 12 | 100 | 0 | 80 | 5699 | 388 | 130.4 | 2.2864 | 0.6983 |  |
| 2 | 13 | 100 | 40 | 0 | 4865 | 316 | 99.35 | 2.0411 | 0.5005 |  |
| 2 | 14 | 100 | 40 | 40 | 5074 | 335 | 109.9 | 2.164 | 0.5759 |  |
| 2 | 15 | 100 | 40 | 80 | 5004 | 346 | 100.4 | 2.0064 | 0.4647 |  |
| 2 | 16 | 100 | 80 | 0 | 4657 | 340 | 105.3 | 2.2611 | 0.5231 |  |
| 2 | 17 | 100 | 80 | 40 | 4865 | 356 | 98.91 | 2.0329 | 0.4342 |  |
| 2 | 18 | 100 | 80 | 80 | 4935 | 388 | 86.62 | 1.7548 | 0.2613 |  |
| 2 | 19 | 150 | 0 | 0 | 5421 | 342 | 125 | 2.3058 | 0.478 |  |
| 2 | 20 | 150 | 0 | 40 | 5769 | 359 | 119.7 | 2.0749 | 0.425 |  |


| 2 | 21 | 150 | 0 | 80 | 5838 | 376 | 112.1 | 1.9185 | 0.356 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 22 | 150 | 40 | 0 | 5560 | 362 | 110 | 1.9784 | 0.3572 |  |
| 2 | 23 | 150 | 40 | 40 | 5977 | 396 | 119.6 | 2.001 | 0.3859 |  |
| 2 | 24 | 150 | 40 | 80 | 5838 | 331 | 111.7 | 1.9133 | 0.4007 |  |
| 2 | 25 | 150 | 80 | 0 | 5143 | 374 | 104.1 | 2.0241 | 0.3054 |  |
| 2 | 26 | 150 | 80 | 40 | 5421 | 314 | 99.93 | 1.8428 | 0.3397 |  |
| 2 | 27 | 150 | 80 | 80 | 5838 | 385 | 118.1 | 2.0212 | 0.3866 |  |
| 2 | 28 | 0 | 0 | 0 | 2155 | 314 | 52.73 | 2.4455 | - | 0.1678 |
| 2 | 29 | 0 | 0 | 0 | 1946 | 314 | 39.7 | 2.0401 |  | 0.1264 |
| 2 | 30 | 0 | 0 | 0 | 2085 | 300 | 39.91 | 1.9137 | - | 0.133 |
| 3 | 1 | 50 | 0 | 0 | 3545 | 320 | 78.3 | 2.2087 | 0.5685 |  |
| 3 | 2 | 50 | 0 | 40 | 4309 | 318 | 102.6 | 2.3811 | 1.0608 |  |
| 3 | 3 | 50 | 0 | 80 | 4379 | 310 | 98.13 | 2.2402 | 0.9957 |  |
| 3 | 4 | 50 | 40 | 0 | 3753 | 281 | 84.37 | 2.2462 | 0.8101 |  |
| 3 | 5 | 50 | 40 | 40 | 3962 | 300 | 98.28 | 2.4785 | 1.0289 |  |
| 3 | 6 | 50 | 40 | 80 | 4170 | 315 | 89.52 | 2.1463 | 0.8081 |  |
| 3 | 7 | 50 | 80 | 0 | 4170 | 310 | 106.3 | 2.5492 | 1.1597 |  |
| 3 | 8 | 50 | 80 | 40 | 4309 | 300 | 106.3 | 2.4669 | 1.1909 |  |
| 3 | 9 | 50 | 80 | 80 | 4518 | 308 | 105.6 | 2.3351 | 1.1499 |  |
| 3 | 10 | 100 | 0 | 0 | 5004 | 340 | 104.8 | 2.0923 | 0.5171 |  |
| 3 | 11 | 100 | 0 | 40 | 5699 | 364 | 150.7 | 2.6426 | 0.9387 |  |
| 3 | 12 | 100 | 0 | 80 | 5421 | 322 | 130.5 | 2.4073 | 0.8031 |  |
| 3 | 13 | 100 | 40 | 0 | 4518 | 335 | 124.1 | 2.7446 | 0.7179 |  |
| 3 | 14 | 100 | 40 | 40 | 4726 | 308 | 118.7 | 2.5095 | 0.706 |  |
| 3 | 15 | 100 | 40 | 80 | 5143 | 348 | 137.7 | 2.6755 | 0.8336 |  |
| 3 | 16 | 100 | 80 | 0 | 4448 | 348 | 116.9 | 2.6281 | 0.6266 |  |
| 3 | 17 | 100 | 80 | 40 | 4935 | 335 | 114.4 | 2.3181 | 0.6219 |  |
| 3 | 18 | 100 | 80 | 80 | 5143 | 364 | 152.1 | 2.9574 | 0.9537 |  |
| 3 | 19 | 150 | 0 | 0 | 5352 | 326 | 128.5 | 2.3991 | 0.5173 |  |
| 3 | 20 | 150 | 0 | 40 | 6325 | 346 | 148.8 | 2.3526 | 0.6325 |  |
| 3 | 21 | 150 | 0 | 80 | 6533 | 400 | 167.5 | 2.5624 | 0.7004 |  |
| 3 | 22 | 150 | 40 | 0 | 5560 | 388 | 155.1 | 2.7896 | 0.6309 |  |
| 3 | 23 | 150 | 40 | 40 | 5699 | 362 | 150.6 | 2.6408 | 0.6272 |  |
| 3 | 24 | 150 | 40 | 80 | 5838 | 348 | 138.8 | 2.3758 | 0.5631 |  |
| 3 | 25 | 150 | 80 | 0 | 5143 | 318 | 127.6 | 2.481 | 0.5203 |  |
| 3 | 26 | 150 | 80 | 40 | 5421 | 364 | 118.8 | 2.1915 | 0.4138 |  |
| 3 | 27 | 150 | 80 | 80 | 6116 | 374 | 140.2 | 2.2907 | 0.5454 |  |
| 3 | 28 | 0 | 0 | 0 | 1946 | 239 | 55.04 | 2.8263 | - | 0.2301 |
| 3 | 29 | 0 | 0 | 0 | 1877 | 285 | 52.16 | 2.7757 | - | 0.1828 |
| 3 | 30 | 0 | 0 | 0 | 1738 | 310 | 49.39 | 2.8366 | - | 0.159 |
| 4 | 1 | 50 | 0 | 0 | 4031 | 295 | 74.98 | 1.8581 | 0.5784 |  |
| 4 | 2 | 50 | 0 | 40 | 4170 | 310 | 82.82 | 1.9856 | 0.6897 |  |
| 4 | 3 | 50 | 0 | 80 | 4865 | 307 | 93.81 | 1.9281 | 0.919 |  |
| 4 | 4 | 50 | 40 | 0 | 3545 | 293 | 72.48 | 2.0423 | 0.5347 |  |
| 4 | 5 | 50 | 40 | 40 | 4240 | 322 | 79.48 | 1.8726 | 0.5843 |  |
| 4 | 6 | 50 | 40 | 80 | 4518 | 348 | 93.95 | 2.0784 | 0.7932 |  |
| 4 | 7 | 50 | 80 | 0 | 3614 | 368 | 73.84 | 2.0421 | 0.3289 |  |
| 4 | 8 | 50 | 80 | 40 | 4031 | 295 | 79.62 | 1.9747 | 0.6724 |  |
| 4 | 9 | 50 | 80 | 80 | 4587 | 310 | 85.6 | 1.8661 | 0.7457 |  |
| 4 | 10 | 100 | 0 | 0 | 4587 | 362 | 94.16 | 2.0514 | 0.3768 |  |
| 4 | 11 | 100 | 0 | 40 | 5074 | 350 | 105.8 | 2.0832 | 0.5115 |  |
| 4 | 12 | 100 | 0 | 80 | 4865 | 331 | 95.56 | 1.963 | 0.4391 |  |
| 4 | 13 | 100 | 40 | 0 | 4516 | 326 | 91.58 | 2.0261 | 0.4069 |  |
| 4 | 14 | 100 | 40 | 40 | 4935 | 325 | 102.3 | 2.0709 | 0.5155 |  |
| 4 | 15 | 100 | 40 | 80 | 4726 | 348 | 87.95 | 1.8599 | 0.3366 |  |
| 4 | 16 | 100 | 80 | 0 | 5421 | 348 | 106.4 | 1.9627 | 0.5216 |  |
| 4 | 17 | 100 | 80 | 40 | 5560 | 324 | 117.4 | 2.1097 | 0.668 |  |
| 4 | 18 | 100 | 80 | 80 | 5838 | 350 | 116.9 | 2.0007 | 0.6225 |  |
| 4 | 19 | 150 | 0 | 0 | 4865 | 326 | 98.48 | 2.0226 | 0.3173 |  |
| 4 | 20 | 150 | 0 | 40 | 5769 | 375 | 108 | 1.8721 | 0.3304 |  |
| 4 | 21 | 150 | 0 | 80 | 5560 | 375 | 113.5 | 2.0414 | 0.367 |  |
| 4 | 22 | 150 | 40 | 0 | 4935 | 396 | 95.28 | 1.9291 | 0.2232 |  |


| 4 | 23 | 150 | 40 | 40 | 5630 | 363 | 113.3 | 2.0107 | 0.3775 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :--- |
| 4 | 24 | 150 | 40 | 80 | 6255 | 368 | 124.1 | 1.984 | 0.445 |  |
| 4 | 25 | 150 | 80 | 0 | 4101 | 320 | 81.93 | 1.9971 | 0.2135 |  |
| 4 | 26 | 150 | 80 | 40 | 5074 | 342 | 111.3 | 2.1935 | 0.3866 |  |
| 4 | 27 | 150 | 80 | 80 | 5560 | 364 | 111 | 1.9964 | 0.3618 |  |
| 4 | 28 | 0 | 0 | 0 | 1946 | 310 | 40.57 | 2.0812 | - | 0.1306 |
| 4 | 29 | 0 | 0 | 0 | 2433 | 310 | 45.9 | 1.8866 | - | 0.1481 |
| 4 | 30 | 0 | 0 | 0 | 1460 | 300 | 34.1 | 2.3356 | - | 0.1137 |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | MEAN |  | 2.1265 | 0.577 | 0.1597 |  |
|  |  |  |  |  |  | 0.301 | 0.2278 | 0.0322 |  |  |

Note: The basic data has been calculated for obtaining Nutrient requirement(NR), Contribution to fertilizers (CFN) and contribution to Soil(CSN) for Nitrogen only. For Phosphorus and Potassium the same method holds.

## APPENDEX-II



```
RESPONSE YARDSTICK ( KG/KG ) : 11.07
```


## GRADIENT 1X

| PARAMETER | N | $\mathrm{P}_{2} \mathrm{O}_{5}$ | $\mathrm{K}_{2} \mathrm{O}$ | FERTILISER ADJUSTMENT EQUATIONS | TARGET (Q/HA) | $\begin{gathered} \text { SOIL-TEST } \\ \text { (KG/HA) } \end{gathered}$ | $\begin{gathered} \text { FERT-DOSE } \\ \text { (KG/HA) } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NR(KG/Q) | :1.8123 | 1.1658 | 2.4599 | FN=3.37*T-0.29 SN | 80 | 442 | 142 |
| CS | :0.1549 | 0.4037 | 0.1536 | $F P=2.61 * T-2.07$ SP |  | 58 | 89 |
| CF | :0.5374 | 0.4465 | 1.3290 | FK=1.85*T-0.14 SK |  | 424 | 89 |

## RESPONSE YARDSTICK ( KG/KG ) : 12.77

GRADIENT 2X

| PARAMETER | N | $\mathrm{P}_{2} \mathrm{O}_{5}$ | $\mathrm{~K}_{2} \mathrm{O}$ | FERTILISER ADJUSTMENT | TARGET | SOIL-TEST | FERT-DOSE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | EQUATIONS | $(Q / H A)$ | $(K G / H A)$ | (KG/HA) |  |  |

NR (KG/Q) :1.7769 1.2009 2.4641 FN=3.49*T-0.30 SN 80

| CS | :0.1554 0.3369 | 0.1486 | FP=1.81*T-1.16 SP | 53 | 83 |
| :---: | :---: | :---: | :---: | :---: | :---: |

CF $\quad 0.50950 .6639$ 1.3418 FK=1.84*T-0.13 SK 464

RESPONSE YARDSTICK ( KG/KG ) : 14.02

OVERALL GRADIENTS

| PARAMETER | $N$ | $\mathrm{P}_{2} \mathrm{O}_{5}$ | $\mathrm{K}_{2} \mathrm{O}$ | FERTILISER ADJU EQUATIONS | STMENT | TARGET (Q/HA) | $\begin{aligned} & \text { SOIL-TEST } \\ & \text { (KG/HA) } \end{aligned}$ | FERT-DOSE (KG/HA) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NR(KG/Q) | :1.7789 | 1.1820 | 2.4427 | FN=3.72*T-0.36 |  | 80 | 442 | 138 |
| CS | :0.1728 | 0.4100 | 0.1607 | $\mathrm{FP}=2.68 * \mathrm{~T}-2.13$ |  |  | 58 | 92 |
| CF | :0.4777 | 0.4409 | 1.2073 | FK=2.02*T-0.16 |  |  | 424 | 94 |
| RESPONSE YARDSTICK ( KG/KG ) : 11.87 |  |  |  |  |  |  |  |  |
| Note: | FN- Fertilizer Nitrogen (added) <br> FP- Fertilizer Phosphorus(added) <br> FK- Fertilizer Potassium (added) <br> SN- Soil Available Nitrogen <br> SP- Soil Available Phosphorus <br> SK- Soil Available Potassium <br> T- Targeted Yield |  |  |  |  |  |  |  |

## APPENNDEX-III (SAS-PROGRAMME)

The following SAS programme has been developed from PROC REG, PROC RSREG, PROC GLM, PROC PLOT to carry out Regression, RSM and Graphic plots
data <file name>;
input cen yr sea rep trt fn fp fk oc sn sp sk yield un up uk ;
$f n 2=f n * f n$;
fn3 $=\mathrm{fn} 2 * \mathrm{fn}$;
$f p 2=f p^{*} f p ;$
fk2 = fk*fk;
$\mathrm{sn2}=\mathrm{sn}$ *sn;
$\mathrm{sp2}=\mathrm{sp}{ }^{*} \mathrm{sp}$;
sk2 = sk*sk;
fnsn $=f n^{*}$ sn;
fpsp $=f p^{*} s p ;$
fksk $=\mathrm{fk}{ }^{*} \mathrm{sk}$;
fnfp = fn*fp;
$f n f k=f n * f$;
fpfk $=f p^{*} f k$;
snsp $=s n^{*}$ sp;
snsk = sn*sk;
spsk = sp*sk;
cards ;
DATA
;
proc print;
run;
proc means;
var sn sp sk;

```
run;
proc glm ;
    class rep fn fp fk;
    model yield = rep fn fp fk fn*fp fn*fk fp*fk fn*fp*fk;
    means fn fp fk fn*fp fn*fk fp*fk;
    run;
    proc reg
    model yield = fn fp fk fn2 fp2 fk2 sn sp sk fnsn fpsp fksk/selection = backward;
    run;
    proc reg ;
    model yield = fn fp fk fn2 fp2 fk2 sn sp sk sn2 sp2 sk2 fnsn fpsp fksk fnfp fnfk fpfk/selection = backward;
    run;
    proc reg
model yield = rep fn fp fk fn2 fp2 fk2 sn sp sk sn2 sp2 sk2 fnsn fpsp fksk fnfp fnfk fpfk/selection =
backward;
run;
proc reg
model yield = fn fp fk fn2 fp2 fk2 sn sp sk sn2 sp2 sk2 fnsn fpsp fksk/selection = backward;
run;
proc reg
model yield = rep fn fp fk fn2 fp2 fk2 sn sp sk sn2 sp2 sk2 fnsn fpsp fksk/selection = backward;
run;
proc reg
model yield = fn fp fk fn2 fp2 fk2 fnfp fnfk fpfk/selection = backward;
run;
proc reg
model yield = rep fn fp fk fn2 fp2 fk2 fnfp fnfk fpfk/selection = backward;
run;
proc reg
model yield = sn sp sk sn2 sp2 sk2 snsp snsk spsk/selection = backward;
run;
proc reg
model yield = rep sn sp sk sn2 sp2 sk2 snsp snsk spsk/selection = backward;
run;
```

proc reg ;
model yield = rep fn fp fk fn2 fp2 fk2 sn sp sk fnsn fpsp fksk/selection = backward;
run;
proc reg
model yield $=f n f p f k f n 2 f p 2 f k 2$ sn sp sk fnsn fpsp fksk/influence;
run;
proc reg
model yield =fn fp fk fn2 fp2 fk2 sn sp sk fnsn fpsp fksk/p r;
run;
proc reg ;
model yield =fn fp fk fn2 fp2 fk2 sn sp sk fnsn fpsp fksk/selection=backward;
run;
proc reg
model yield $=f n f p f k f n 2$ fn3 fp2 fk2 sn sp sk fnsn fpsp fksk/selection=backward;
run;
PROC GLM;
CLASS fn fp fk;
MODEL YIELD= REP fn fp fk;
OUTPUT OUT= MAR2 PREDICTED = YPRED RESIDUAL=Z;
PROC STANDARD STD=1.0;
VAR Z;
PROC RANK NORMAL=BLOM ;
VAR Z;
RANKS NSCORE;
PROC PRINT:
;
PROC PLOT;
PLOT Z*YPRED/ VREF=0 VPOS=19 HPOS=50;
PLOT Z*NSCORE/VREF=0 HREF=0 VPOS=19 HPOS=50;
RUN;

PROC PLOT;
PLOT FN*YIELD/ VREF=0 VPOS=19 HPOS=50;
PLOT FP*YIELD/ VREF=0 VPOS=19 HPOS=50;
PLOT FK*YIELD/ VREF=0 VPOS=19 HPOS=50;
RUN;
proc rsreg;
model yield $=$ sn sp sk fn fp fk /covar=3 lackfit ;
ridge max outr=ridge;
run;

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[^0]:    R-Square $=0.9055$

